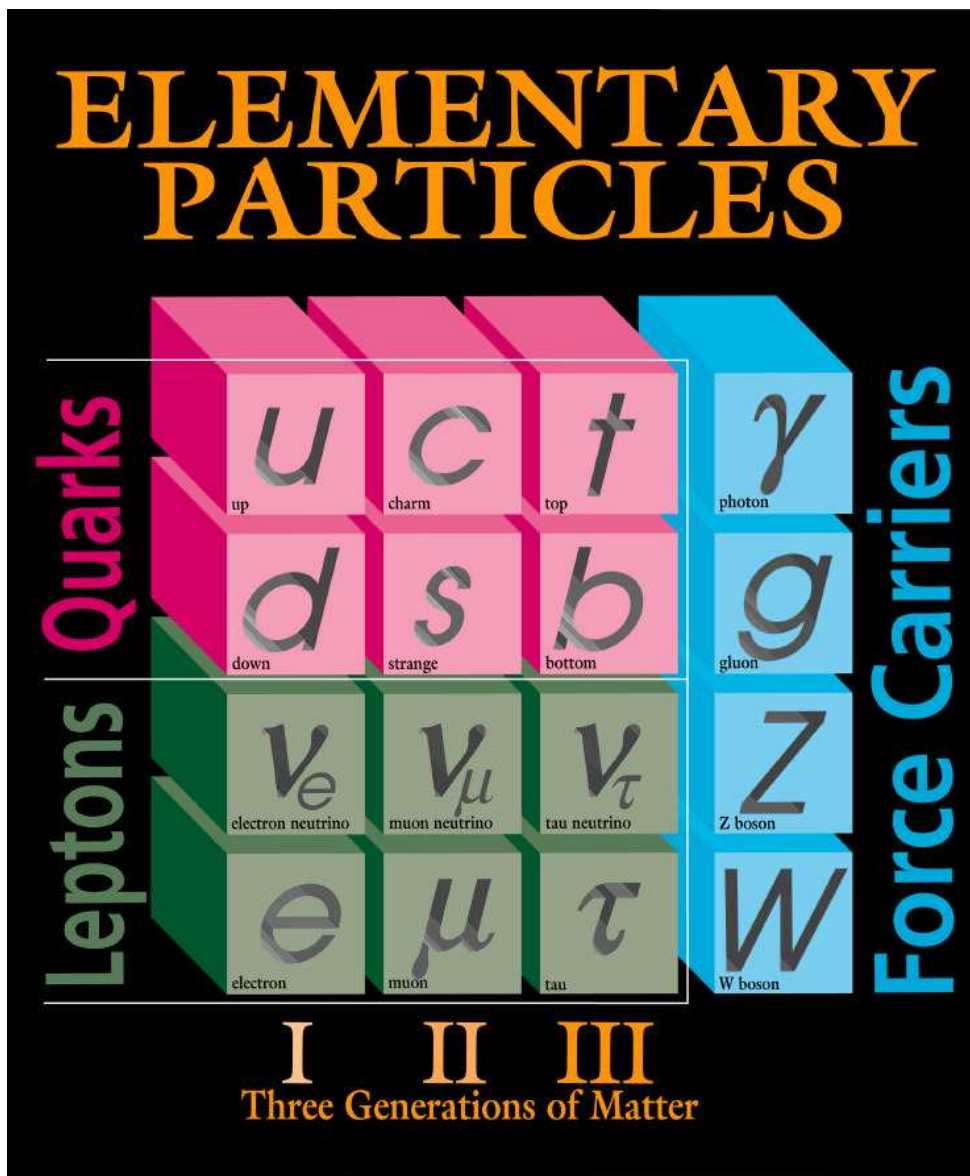
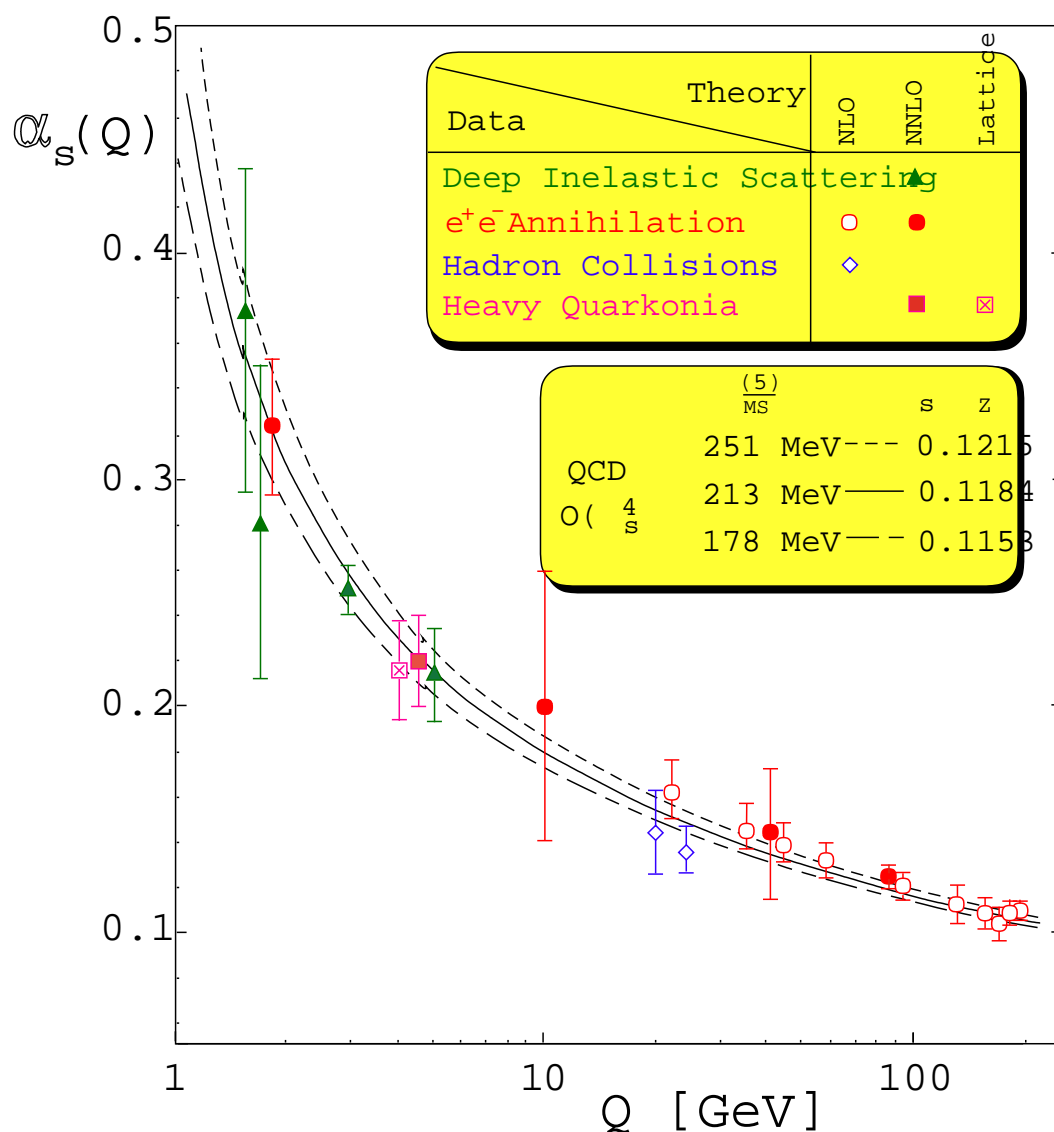


Standard Model



- Asymptotic freedom : the effective coupling vanishes at high energies



- Interactions of quarks and gluons visible at high energies
- Perturbation applicable, but parameters connecting quarks/gluons to hadrons need to be known
 - * structure functions (parton distributions)
 - * decay constants (f_π, \dots)
 - * wave functions (quarkonia)

⋮

- **Color confinement** : neither free quarks nor free gluons
 - Crucial to separate short- and long-distance physics
- **QCD Lagrangian**
 - Gauge group : SU(3)

gluons 8

quarks $(3_L + 3_R) \times n_f$

n_f : #(flavors)

- Parameters : masses generated by Higgs mechanism

gauge coupling $\alpha_s = \frac{g_s^2}{4\pi}$

quark masses $m_u, m_d, m_s, m_c, m_b, m_t$

$$\mathcal{L}_{\text{QCD}} = -\frac{1}{4} G_{\mu\nu}^a G^{a\mu\nu} + \sum_q \bar{q}(i\not{D} - m_q)q$$

Gauged Higgs System

- $SU(2)_L$ doublet : φ with hypercharge $Y = 1/2$

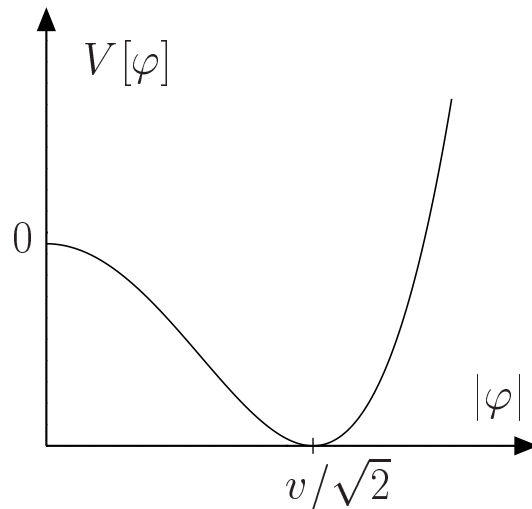
$$\varphi = \frac{1}{\sqrt{2}} \begin{pmatrix} i(\varphi_1 - i\varphi_2) \\ \varphi_0 - i\varphi_3 \end{pmatrix} \quad \begin{array}{l} SU(2) : \varphi \rightarrow \exp(iT_a \theta^a) \varphi \\ U(1) : \varphi \rightarrow \exp(iY\theta) \varphi \end{array}$$

- **Potential** : The gauge invariant and renormalizable Lagrangian

$$\mathcal{L}_{Higgs} = (D^\mu \varphi)^\dagger D_\mu \varphi - V(\varphi)$$

for the Higgs doublet is given by the most general potential

$$V(\varphi) = \mu^2 \varphi^\dagger \varphi + \lambda (\varphi^\dagger \varphi)^2$$



– $O(4) \equiv SU(2)_L \times SU(2)_R : \varphi^\dagger \varphi = \frac{1}{2} (\varphi_0^2 + \varphi_1^2 + \varphi_2^2 + \varphi_3^2) \equiv \frac{1}{2} \eta$

Spontaneous Breaking of $SU(2)_L \times U(1)_Y$

- $\mu^2 < 0$ and $\lambda > 0$ (vacuum stability) :

$$\frac{\partial V}{\partial \eta} = \frac{1}{2}\mu^2 + \frac{1}{2}\lambda\eta = 0 \Rightarrow \eta = -\frac{\mu^2}{\lambda} \equiv v^2$$

$$\varphi_0 = v, \quad \varphi_a = 0 \quad (a = 1, 2, 3)$$

with losing the generality leading to the vacuum expectation value (vev) of the Higgs doublet

$$\langle \varphi \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v \end{pmatrix}$$

- Unbroken gauge symmetry leaving $\langle \varphi \rangle$ invariant

$$Q = T_3 + Y = \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix} \Rightarrow SU(2)_L \times U(1)_Y \rightarrow U(1)_{EM}$$

- The potential itself has the custodial $SU(2)_D$ symmetry.

$$SU(2)_L \times SU(2)_R \rightarrow SU(2)_D$$

This group is the symmetry of the Higgs potential only; in the full theory $SU(2)_R$ and $SU(2)_D$ are explicitly broken by the $U(1)_Y$ gauge interactions.

Gauge Boson Masses

- $SU(2)_L \times U(1)_Y$ covariant derivative

$$D_\mu \varphi = \left(\partial_\mu + ig \frac{\tau_a}{2} W_\mu^a + ig' \frac{1}{2} B_\mu \right) \varphi$$

- Gauge boson mass terms come from the Higgs kinetic term :

$$\begin{aligned} \mathcal{L} &= (\mathcal{D}^\mu \langle \varphi \rangle)^\dagger \mathcal{D}_\mu \langle \varphi \rangle \Leftrightarrow \langle \varphi \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v \end{pmatrix} \\ &= \frac{v^2}{8} \left\{ g^2 [(W_\mu^1)^2 + (W_\mu^2)^2] + (gW_\mu^3 - g'B_\mu)^2 \right\} \\ &\quad W_\mu^\pm = \frac{1}{\sqrt{2}} (W_\mu^1 \mp iW_\mu^2) \\ &\quad Z_\mu = \frac{1}{\sqrt{g^2 + g'^2}} (gW_\mu^3 - g'B_\mu) \\ &= \frac{1}{4} g^2 v^2 W_\mu^\dagger W^\mu + \frac{1}{8} (g^2 + g'^2) v^2 Z^\mu Z_\mu \equiv m_W^2 W_\mu^\dagger W^\mu + \frac{1}{2} m_Z^2 Z^\mu Z_\mu \\ &\quad m_W = \frac{1}{2} g v \quad v \approx 246 \text{ GeV} \\ &\quad m_Z = \frac{1}{2} \sqrt{g^2 + g'^2} v > m_W \end{aligned}$$

- The state orthogonal to Z_μ

$$A_\mu = \frac{1}{\sqrt{g^2 + g'^2}} (g'W_\mu^3 + gB_\mu)$$

is massless so that it is nothing but the photon field.

– The weak mixing angle θ_W is defined as

$$\tan \theta_W = \frac{g'}{g} \Rightarrow \begin{cases} Z_\mu = W_\mu^3 \cos \theta_W - B_\mu \sin \theta_W \\ A_\mu = W_\mu^3 \sin \theta_W + B_\mu \cos \theta_W \end{cases}$$

- Among the four scalar fields $\varphi_i (i = 0, 1, 2, 3)$ the three fields $(\varphi_1, \varphi_2, \varphi_3)$ become the longitudinal components of the massive gauge bosons (W^\pm, Z) while $\varphi_0 = (v + H)/\sqrt{2}$ remains as a physical field - this is called the Higgs boson.
- The so-called ρ parameter

$$\rho \equiv \frac{m_W^2}{m_Z^2 \cos^2 \theta_W} = \frac{g_Z^2/m_Z^2}{g^2/m_W^2} = \frac{\text{NC Fermi coupling}}{\text{CC Fermi coupling}}$$

– SM Higgs : $\rho = 1$

– General Higgs :

$$\begin{aligned} m_W^2 &= \frac{1}{2} \langle I_3 | (I^+ I^- + I^- I^+) | I_3 \rangle g^2 \langle \varphi \rangle^2 \\ &= [I(I+1) - I_3^2] g^2 \langle \varphi \rangle^2 \quad I^\pm = I^1 \pm iI^2 \end{aligned}$$

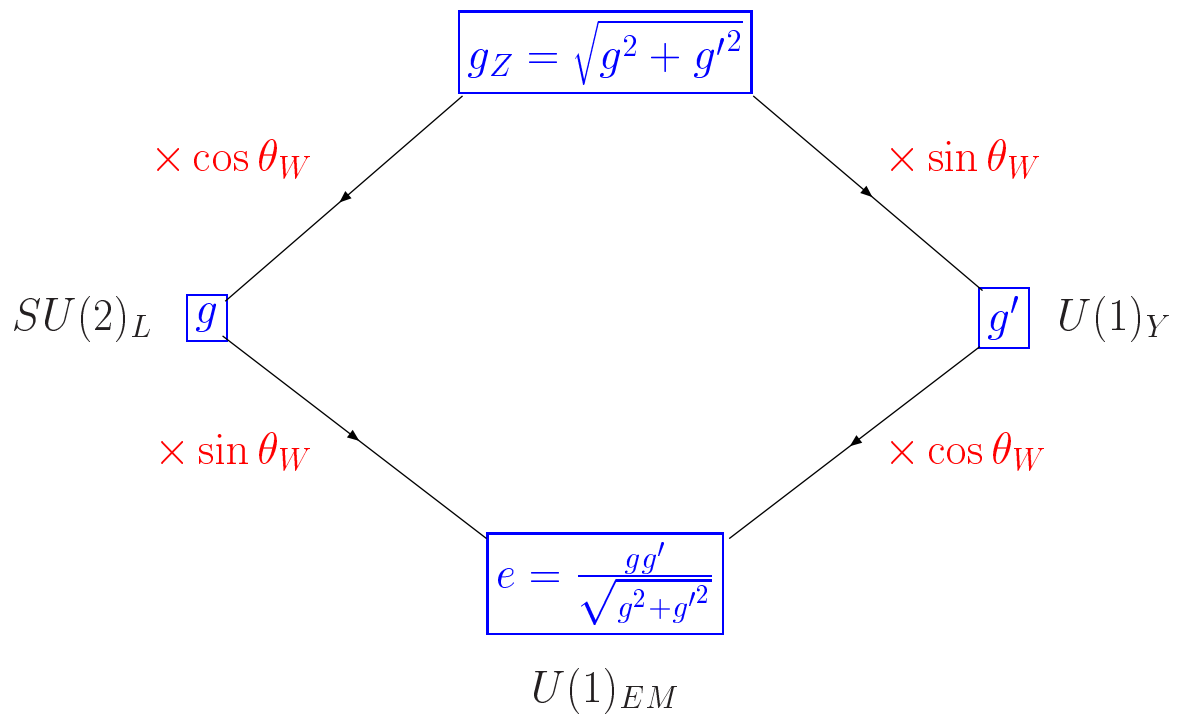
$$m_Z^2 = 2I_3^2 (g^2 + g'^2) \langle \varphi \rangle^2$$

$$\Rightarrow \rho = \frac{m_W^2}{m_Z^2 \cos^2 \theta_W} = \frac{I(I+1) - I_3^2}{2I_3^2}$$

$$\begin{aligned} (I, I_3) &= \left(\frac{1}{2}, \pm\frac{1}{2}\right) \rightarrow \rho = 1 & (1, \pm 1) &\rightarrow \rho = \frac{1}{2} \\ (1, 0) &\rightarrow \rho = \infty & \left(\frac{3}{2}, \pm\frac{3}{2}\right) &\rightarrow \rho = \frac{1}{3} \dots \end{aligned}$$

$$\tan \theta_W = \frac{g'}{g}$$

$$\sin / \cos \theta_W = \frac{g'/g}{\sqrt{g^2+g'^2}}$$



SU(2) × U(1) Gauge Interactions

- Covariant derivative in terms of physical gauge bosons

$$D_\mu = \partial_\mu + \frac{ig}{\sqrt{2}} (I^+ W_\mu + I^- W_\mu^\dagger) + ig I_3 W_\mu^3 + ig' Y B_\mu$$

$$Y = Q - I_3 \quad \{W^3, B\} \rightarrow \{Z, A\}$$

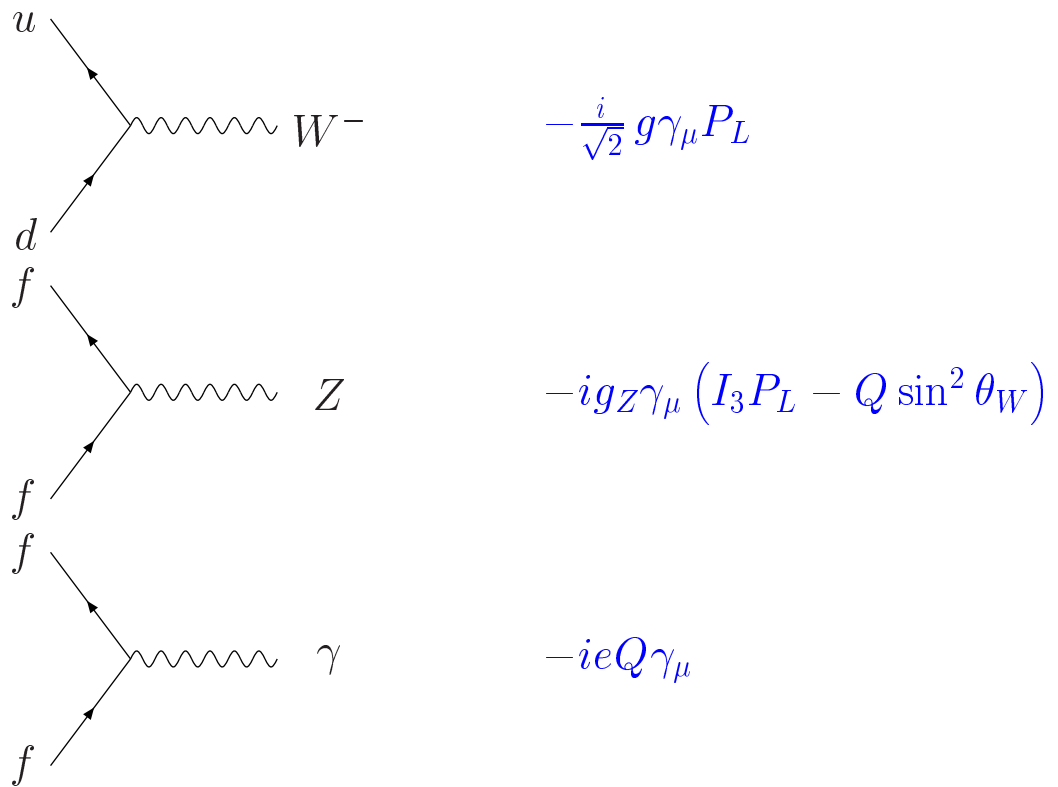
$$= \partial_\mu + \frac{ig}{\sqrt{2}} (I^+ W_\mu + I^- W_\mu^\dagger) + ig_Z (I_3 - Q \sin^2 \theta_W) Z_\mu + ieQ A_\mu$$

- W^\pm couples with pure SU(2) gauge coupling
- Z couples to a linear combination of SU(2) and EM charge
- γ couples to the electric charge $Q \Rightarrow$ QED

Particle Names	I	$Y = \langle Q \rangle$	SU(3) _C
$l_L = \begin{bmatrix} \nu \\ e \end{bmatrix}_L$	$\frac{1}{2}$	$-\frac{1}{2}$	1
e_R	0	-1	1
$q_L = \begin{bmatrix} u \\ d \end{bmatrix}_L$	$\frac{1}{2}$	$\frac{1}{6}$	3
u_R	0	$\frac{2}{3}$	3
d_R	0	$-\frac{1}{3}$	3
$\varphi = \begin{bmatrix} \varphi^+ \\ \varphi^0 \end{bmatrix}$	$\frac{1}{2}$	$\frac{1}{2}$	1
$\tilde{\varphi} = \begin{bmatrix} -\varphi^{0*} \\ \varphi^- \end{bmatrix}$	$\frac{1}{2}$	$-\frac{1}{2}$	1

- Fermion gauge interactions

$$\mathcal{L} = \sum_{\text{fermions}} \bar{\psi}_L i \not{D} \psi_L + \bar{\psi}_R i \not{D} \psi_R$$



- Yang–Mills Interactions

$$F_{\mu\nu}^a = \partial_\mu A_\nu^a - \partial_\nu A_\mu^a + g f^{abc} A_\mu^b A_\nu^c$$

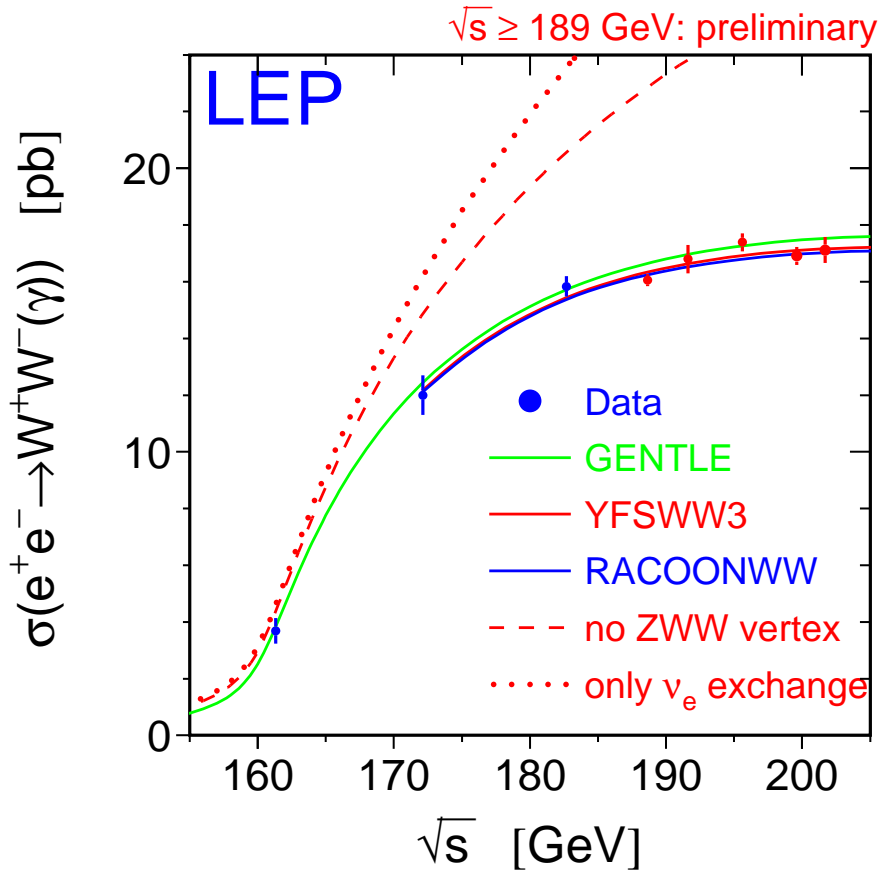
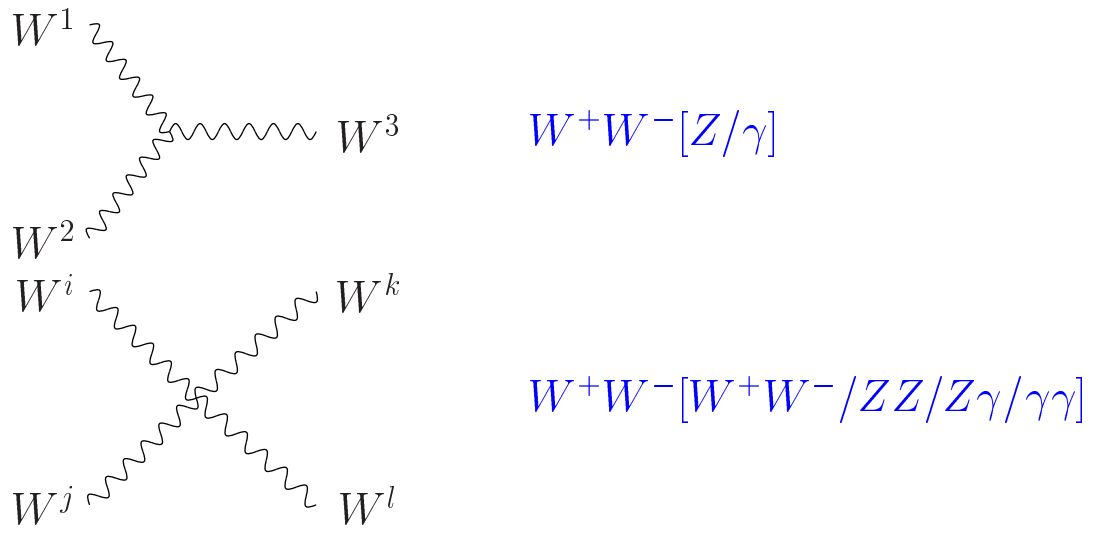
$$[T^a, T^b] = i f^{abc} T^c \quad \text{Tr}(T^a T^b) = \frac{1}{2} \delta^{ab}$$

$$\begin{aligned}
\mathcal{L} &= -\frac{1}{4} F_{\mu\nu}^a F^{a\mu\nu} \\
&= -\frac{1}{4} (\partial_\mu A_\nu^a - \partial_\nu A_\mu^a)^2 - g f^{abc} \partial_\mu A_\nu^a A^{b\mu} A^{c\nu} \\
&\quad - \frac{1}{4} g^2 f^{abe} f^{cde} A_\mu^a A_\nu^b A^{c\mu} A^{d\nu}
\end{aligned}$$

– SU(2) : $f^{abc} = \epsilon^{abc}$ [$a = 1, 2, 3$]

– Gauge boson self couplings*

*Higgs–gauge/Higgs–fermion interactions later



Fermion Masses

- Only Higgs doublets can give known fermion masses while any nontrivial Higgs representation can give gauge boson masses
- Fermions cannot have $SU(2) \times U(1)$ invariant mass term, i.e. quarks and leptons are massless before symmetry breaking
- A single doublet φ can generate masses of all quarks, leptons and W^\pm, Z
- Yukawa interactions [only one generation is considered] :

$$\begin{aligned} -\mathcal{L} &= f(\bar{q}_L \bar{d})\varphi - h(\bar{q}_L \bar{u})\tilde{\varphi} + \text{h.c.} \\ \langle \varphi \rangle &= \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v \end{pmatrix} & \langle \tilde{\varphi} \rangle &= \frac{1}{\sqrt{2}} \begin{pmatrix} -v \\ 0 \end{pmatrix} \\ &= \frac{1}{\sqrt{2}} f v (\bar{d}d) + \frac{1}{\sqrt{2}} h v (\bar{u}u) \equiv m_d \bar{d}d + m_u \bar{u}u \\ &\Rightarrow m_d = \frac{1}{\sqrt{2}} f v & m_u &= \frac{1}{\sqrt{2}} h v \end{aligned}$$

Minimal Model based on $SU(2) \times U(1) \times SU(3)$

- The only dimensionful parameter is v ; all other masses are secondary

$$\begin{aligned} m_W &= \frac{1}{2} g v & m_Z &= \frac{1}{2} g_Z v \\ m_u &= \frac{1}{\sqrt{2}} h_u v & m_d &= \frac{1}{\sqrt{2}} f_d v \\ m_l &= \frac{1}{\sqrt{2}} f_l v & m_H &= \sqrt{2} \lambda^{1/2} v \end{aligned}$$

- Neutrinos were exactly massless within the SM \Rightarrow **Not any more**
- Baryon and lepton numbers are automatically conserved (no renormalizable B/L-violating interactions) \Rightarrow **Probably not any more**

Quark Masses and Mixings

Complex fields

Consider n generations of quarks $\{ q_{L,i}^{\circ} = (u_{L,i}^{\circ}, d_{L,i}^{\circ}), u_{R,i}^{\circ}, d_{R,i}^{\circ} \}, i=1-m$

① Kinetic + gauge terms for these fields is symmetric under $U(m) \times U(m) \times U(m)$

$q_L^{\circ} \rightarrow U_1 q_L^{\circ}, u_R^{\circ} \rightarrow U_2 u_R^{\circ}, d_R^{\circ} \rightarrow U_3 d_R^{\circ}; U_{1,2,3} : \text{unitary}$
 $m \times m \qquad m \times m \qquad m \times m \qquad \text{i.e. } U_i^{\dagger} U_i = 1$

- Gauge bosons are blind of generations $q_L^{\circ} = \begin{pmatrix} q_{L,1}^{\circ} \\ \vdots \\ q_{L,m}^{\circ} \end{pmatrix}$ etc
- Every generation cannot be distinguished from one another

② Yukawa interactions break the symmetry (generally)

$-\mathcal{L}_Y = f_{ij} \bar{d}_{R,i}^{\circ} \phi^{\dagger} q_{L,j}^{\circ} + h_{ij} \bar{u}_{R,i}^{\circ} \tilde{\phi}^{\dagger} q_{L,j}^{\circ} + h.c.$

- Yukawa terms are the ONLY source of symmetry breaking in SM with $\langle \phi^{\circ} \rangle = \frac{v}{\sqrt{2}}$

③ f 's and h 's have $4m^2$ (real) parameters in total. But not all of them are physically observable. The symmetry of the kinetic term implies a kind of reparametrization invariance :

The transformation $f \rightarrow U_3^\dagger f U_1$, $h \rightarrow U_2^\dagger h U_1$ leaves the physics unchanged:

④ A $U(1)$ subgroup of $U(m)^3$, with $U_1 = U_2 = U_3 = e^{i\alpha}$ does NOT change f and h .

The effective reparametrization group is thus $U(m)^3 / U(1)$.

⑤ The space of physical parameters is therefore

$$\mathbb{R}^{4m^2} / (U(m)^3 / U(1))$$

• Dimension = $4m^2 - (3 \times m^2 - 1) = m^2 + 1$

• $m^2 + 1$	=	$2m$	+	$\frac{1}{2} m(m-1)$	+	$\frac{1}{2} (m-1)(m-2)$
		particle masses		mixing angles (flavor violation)		phases (CP violation)

$m =$	2	4	1	0 (no CP)	
	3	6	3	1 (CP)	realized in Nature
	4	8	6	3 (")	
	⋮	⋮	⋮	⋮	
	⋮	⋮	⋮	⋮	

(Cabibbo-)Kobayashi-Maskawa Matrix \equiv KM matrix

① Gauge symmetry breaking $\langle \phi^0 \rangle = \frac{v}{\sqrt{2}}$: $M_d = \frac{v}{\sqrt{2}} f$, $M_u = \frac{v}{\sqrt{2}} h$: $n \times n$

$-\mathcal{L}_m = \bar{d}_R^0 M_d d_L^0 + \bar{u}_R^0 M_u u_L^0 + h.c.$

Theorem: A complex $n \times n$ matrix M can be written as (SVD)
 $M = U^\dagger D U'$ with unitary U and U'
 D : diagonal with its diagonal elements ≥ 0

∇
 $M_u = U_R^\dagger M_u^D U_L$ with $U_{R,L} = U_{R,L} u_{R,L}^0$ and $d_{R,L} = V_{R,L} d_{R,L}^0$
 $M_d = V_R^\dagger M_d^D V_L$

$M_u^D = \text{diag}(m_{u_1}, \dots, m_{u_n})$
 $M_d^D = \text{diag}(m_{d_1}, \dots, m_{d_m})$

$\Rightarrow -\mathcal{L}_m = m_{u_i} (\bar{u}_{R_i} u_{L_i} + \bar{u}_{L_i} u_{R_i}) + m_{d_i} (\bar{d}_{R_i} d_{L_i} + \bar{d}_{L_i} d_{R_i})$: diagonal

$U_L \cdot \begin{pmatrix} u_L^0 \\ d_L^0 \end{pmatrix} = \begin{pmatrix} U_L u_L^0 \\ U_L d_L^0 \end{pmatrix} = \begin{pmatrix} u_L \\ U_L V_L^\dagger d_L \end{pmatrix} \equiv \begin{pmatrix} u_L \\ K d_L \end{pmatrix} = \begin{pmatrix} u_L \\ d_L' \end{pmatrix}$

\Rightarrow **KM matrix** $K \equiv U_L V_L^\dagger$ linking d_L' to d_L : $n \times n$ complex ∇

② Standard parameters : - three Euler angles ($\theta_{12}, \theta_{23}, \theta_{31}$) and one phase (δ_{13})

$$K = \begin{bmatrix} c_{12} c_{13} & s_{12} c_{13} & s_{13} e^{-i \delta_{13}} \\ -s_{12} c_{23} - c_{12} s_{23} s_{13} e^{i \delta_{13}} & c_{12} c_{23} - s_{12} s_{23} s_{13} e^{i \delta_{13}} & s_{23} c_{13} \\ s_{12} s_{23} - c_{12} c_{23} s_{13} e^{i \delta_{13}} & -c_{12} s_{23} - s_{12} c_{23} s_{13} e^{i \delta_{13}} & c_{23} c_{13} \end{bmatrix}$$

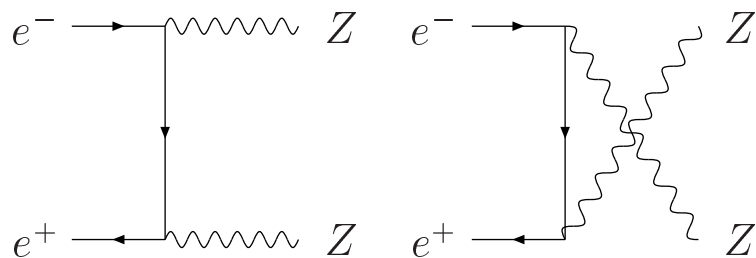
Higgs Phenomenology

Minimal Higgs Boson

Something needed in $J = 0$ sector

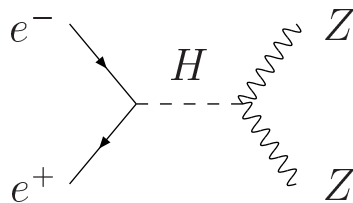
- Assume $SU(2) \times U(1)$ without Higgs and with W^\pm, Z masses put by hand

– $e^+e^- \rightarrow ZZ$

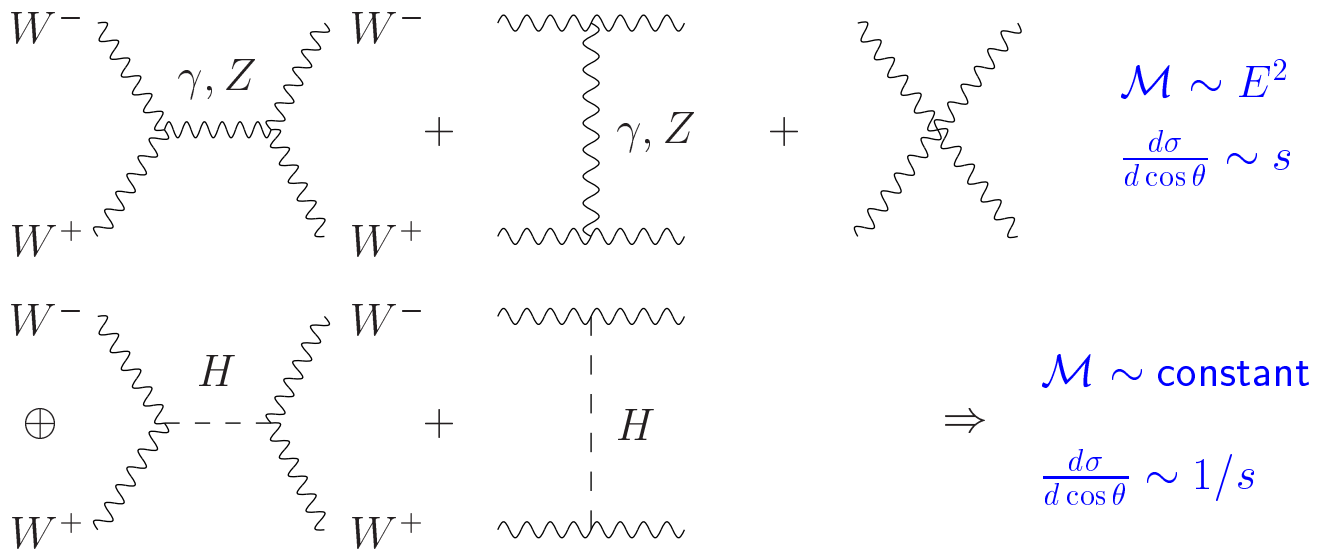


$$\frac{d\sigma}{d\cos\theta} \sim \frac{\pi\alpha}{16s_W^2 c_W^2} \frac{m_e^2}{m_Z^4}$$

This comes from $J = 0$ partial wave and eventually violates unitarity at high energies; so something is needed to cure the $J = 0$ part. Adding the standard Higgs cancels the ill behavior entirely. [Higgs-fermion coupling must be proportional to the fermion mass !]



– $W^+W^- \rightarrow W^+W^-$



- SU(2) doublet with 4 components - 1 physical $H \oplus$ 3 unphysical (W^\pm, Z)
- Higgs : vibration of the vacuum

$$J = 0, P = +, C = +, Q = 0, \dots$$

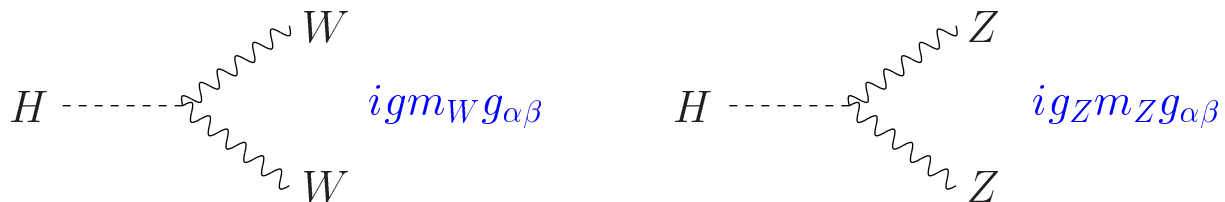
Higgs Couplings

Higgs couplings can be derived by replacing v by $v + H$

$$m \Rightarrow m \left(1 + \frac{g}{2m_W} H \right)$$

- With gauge bosons

$$\begin{aligned} \mathcal{L} &= m_W^2 W_\mu^\dagger W^\mu + \frac{1}{2} m_Z^2 Z^\mu Z_\mu \\ &\rightarrow m_W^2 \left(1 + \frac{g}{2m_W} H \right) W_\mu^\dagger W^\mu + \frac{1}{2} m_Z^2 \left(1 + \frac{g_Z}{2m_Z} H \right) Z^\mu Z_\mu \\ &= (\text{masses}) + gm_W H W_\mu^\dagger W^\mu + \frac{1}{2} g_Z m_Z H Z^\mu Z_\mu \\ &\quad + \frac{1}{4} g^2 H^2 W_\mu^\dagger W^\mu + \frac{1}{8} g_Z^2 H^2 Z^\mu Z_\mu \end{aligned}$$



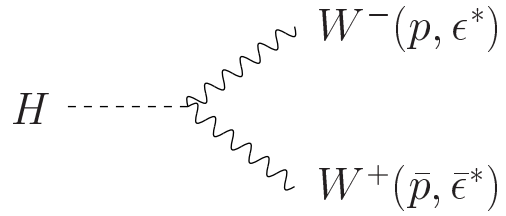
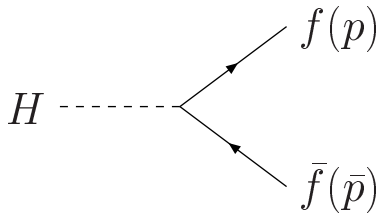
No $HZ\gamma$, $H\gamma\gamma$, Hgg at tree level

- With fermions

$$\begin{aligned} \mathcal{L} &= -m_f \bar{f} f \\ &\rightarrow -m_f \left(1 + \frac{g}{2m_W} H \right) \bar{f} f = (\text{mass}) - \frac{gm_f}{2m_W} H \bar{f} f \end{aligned}$$



Higgs Decays



$$\mathcal{M} = -\frac{gm_f}{2m_W} \bar{u}(p)v(\bar{p})$$

$$\mathcal{M} = gm_W \epsilon^* \cdot \bar{\epsilon}^*$$

Partial Decay Widths

$$\Gamma(H \rightarrow f\bar{f}) = \frac{\alpha m_f^2 m_H}{8m_W^2 \sin^2 \theta_W} N_C^f \beta_f^3$$

$$= \frac{G_F m_f^2 m_H}{4\sqrt{2}\pi} N_C^f \beta_f^3 \quad \beta_f = \sqrt{1 - \frac{4m_f^2}{m_H^2}}$$

$$\Gamma(H \rightarrow W_T^+ W_T^-) = \frac{\alpha m_W^2 \beta_W}{2 m_H \sin^2 \theta_W} \quad \beta_W = \sqrt{1 - \frac{4m_W^2}{m_H^2}}$$

$$\Gamma(H \rightarrow W_L^+ W_L^-) = \frac{\alpha m_H^3 \beta_W}{16 m_W^2 \sin^2 \theta_W} \left(1 - \frac{2m_W^2}{m_H^2}\right)$$

$$\Gamma(H \rightarrow W^+ W^-) = \frac{\alpha m_H^3 \beta_W}{16 m_W^2 \sin^2 \theta_W} \left(1 - \frac{4m_W^2}{m_H^2} + \frac{12m_W^4}{m_H^4}\right)$$

$$= \frac{G_F m_H^3 \beta_W}{8\sqrt{2}\pi} \left(1 - \frac{4m_W^2}{m_H^2} + \frac{12m_W^4}{m_H^4}\right)$$

$$\Gamma(H \rightarrow ZZ) = \frac{1}{2} \cdot \frac{G_F m_H^3 \beta_Z}{8\sqrt{2}\pi} \left(1 - \frac{4m_Z^2}{m_H^2} + \frac{12m_Z^4}{m_H^4}\right)$$

- In the limit of $m_H \gg m_W, m_Z$

$$\Gamma(H \rightarrow ZZ) = \frac{1}{2} \Gamma(H \rightarrow WW)$$

- $H \rightarrow \gamma\gamma, Z\gamma, gg$: only via fermion and/or W loops leading to small branching ratios in general
- Equivalence theorem : $\Gamma(H \rightarrow V_L V_L) \gg \Gamma(H \rightarrow V_T V_T)$

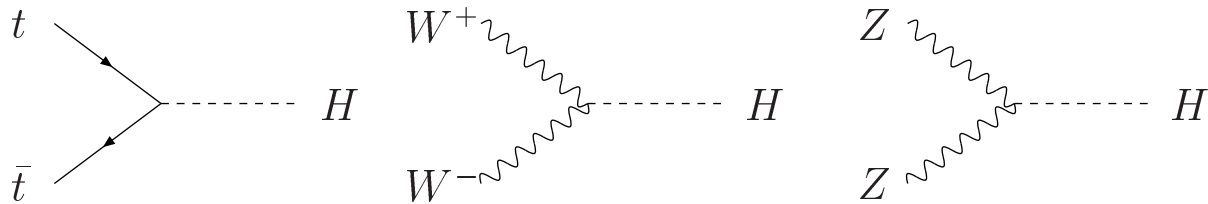
$$\Gamma(H \rightarrow f\bar{f}) \sim \alpha_W m_H \times \left(\frac{m_f}{m_W}\right)^2 \sim (\text{Yukawa})^2 m_H$$

$$\Gamma(H \rightarrow VV) \sim \alpha_W m_H \times \left(\frac{m_H}{m_V}\right)^2 \sim \lambda m_H \not\sim (\text{gauge})^2 m_H$$

in the limit of $m_H \gg m_V$.

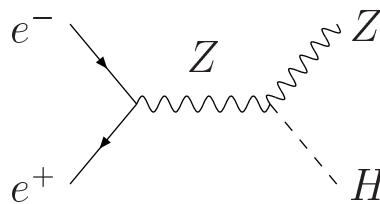
Higgs Boson Production

- 1st and 2nd generation quarks/leptons couple extremely weakly to H
- "Large" coupling required, i.e. production via heavy particles



- Main production modes

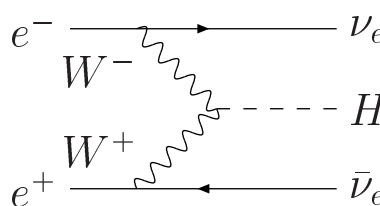
(a) Higgs-strahlung :



$$\sigma \sim \frac{G_F^2 M_Z^4}{96\pi s} \kappa_S \beta$$

\sqrt{s} lower part

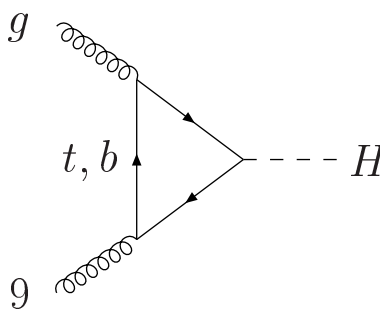
(b) W fusion :



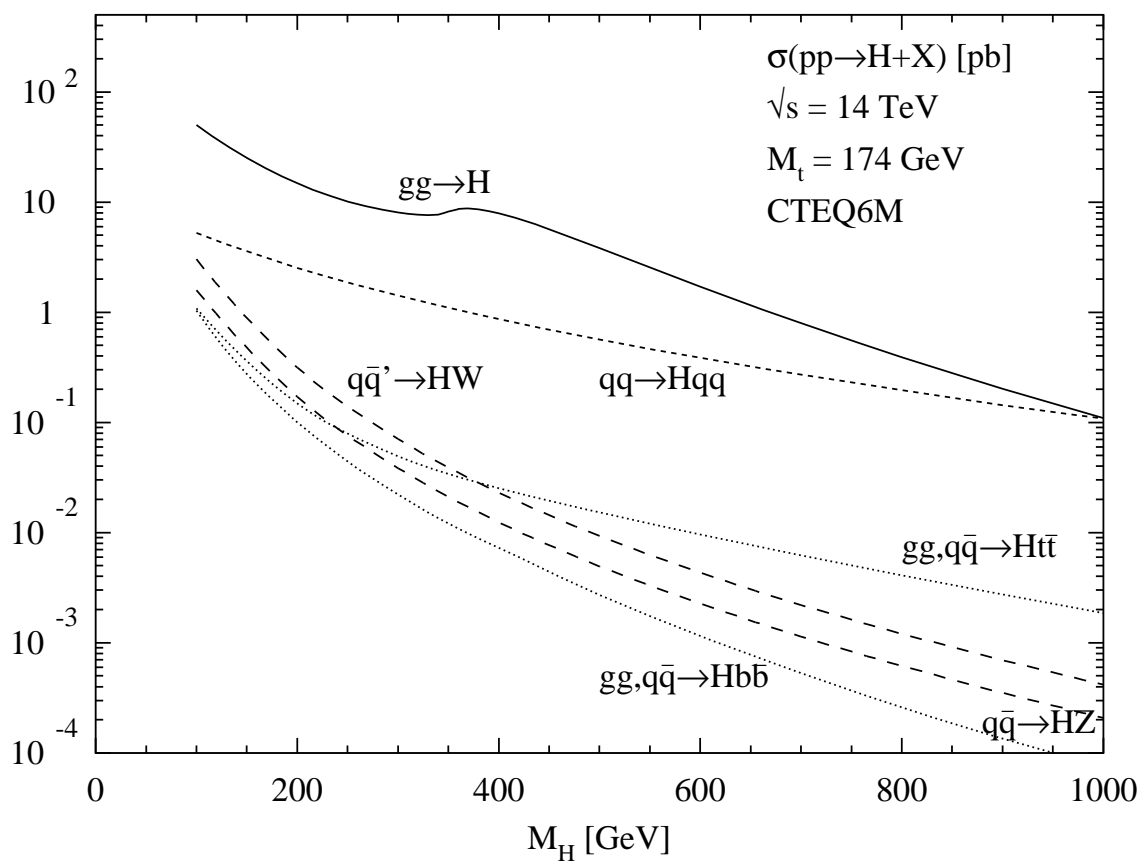
$$\sigma \sim \frac{G_F^3 M_W^4}{4\sqrt{2}\pi^3} \log \frac{s}{M_H^2}$$

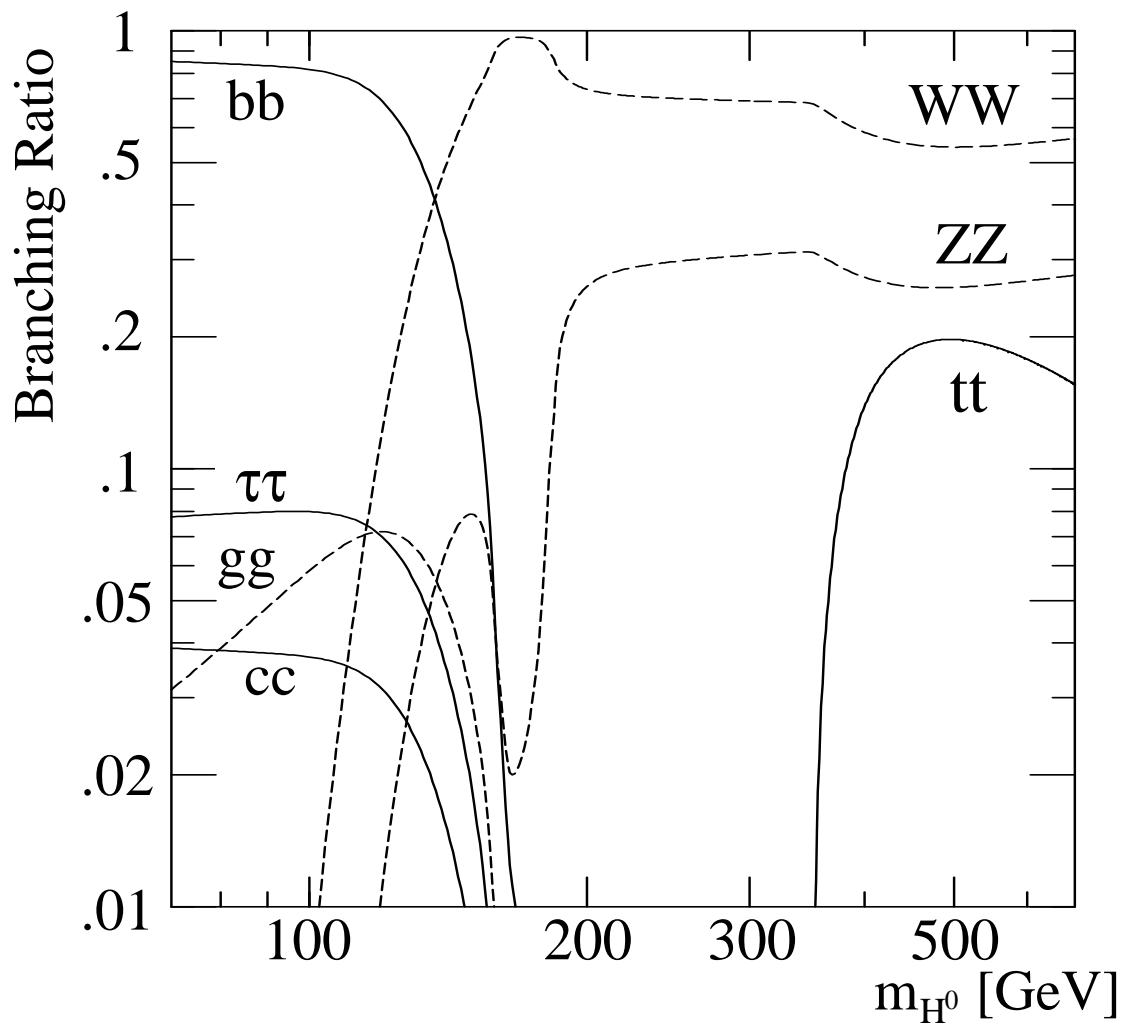
\sqrt{s} upper part

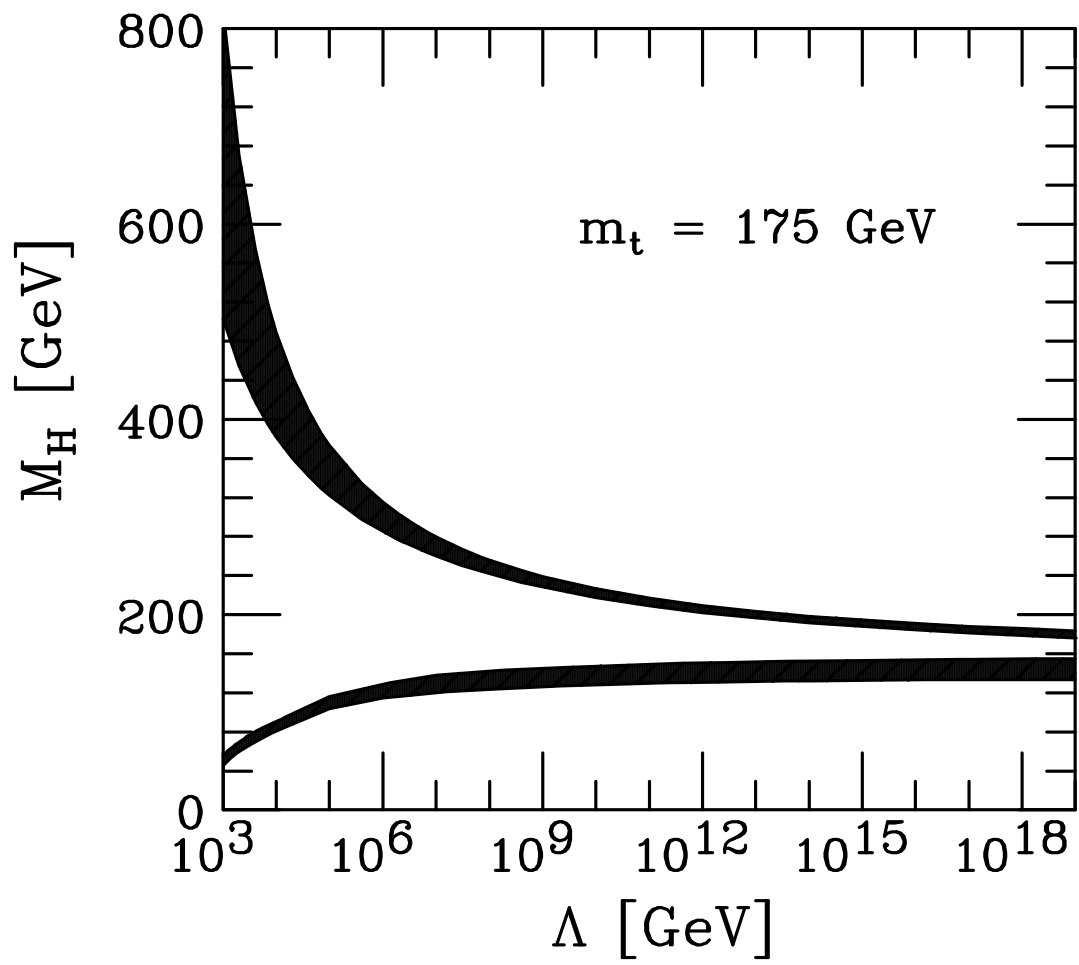
(c) Gluon fusion :

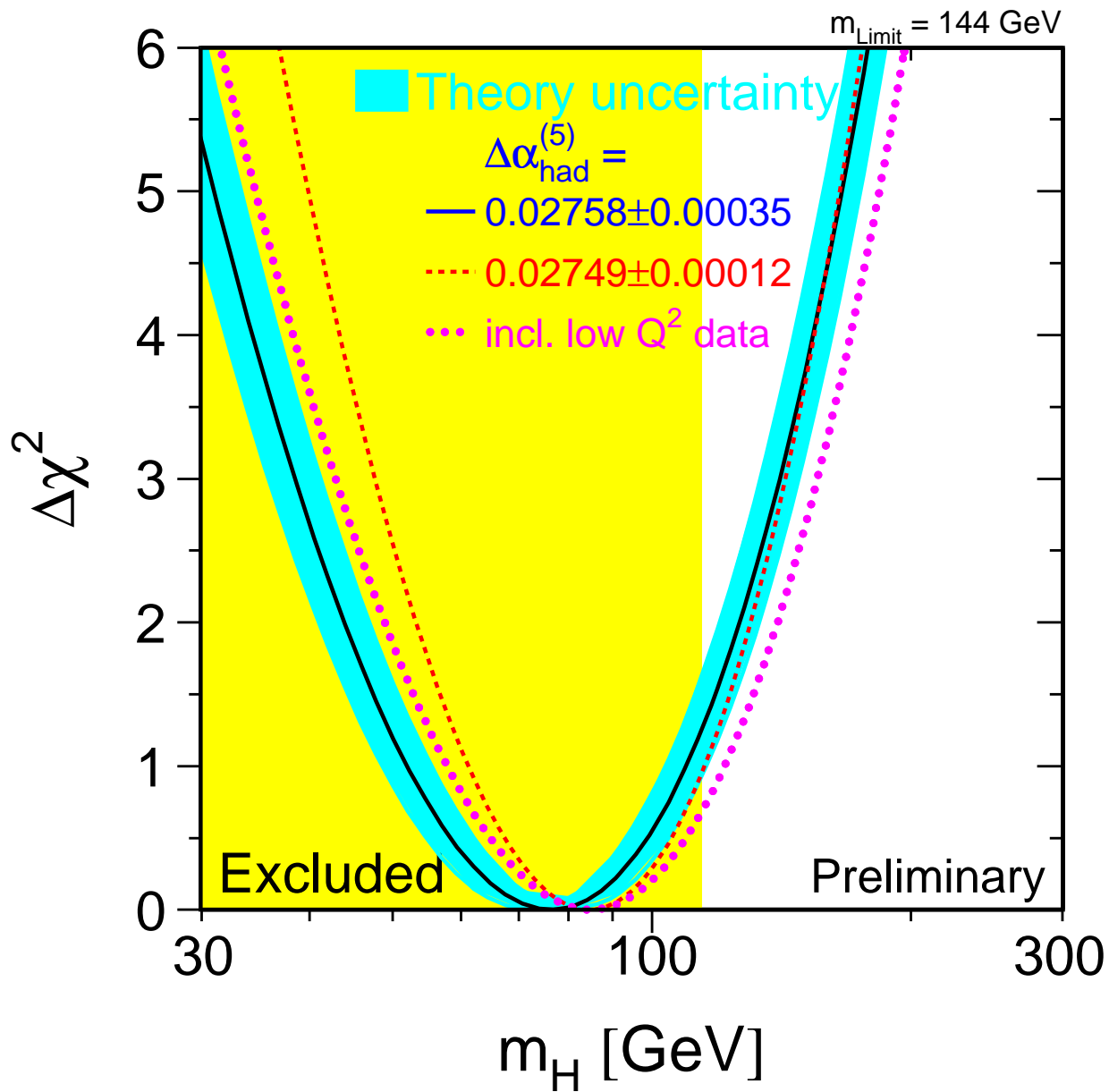


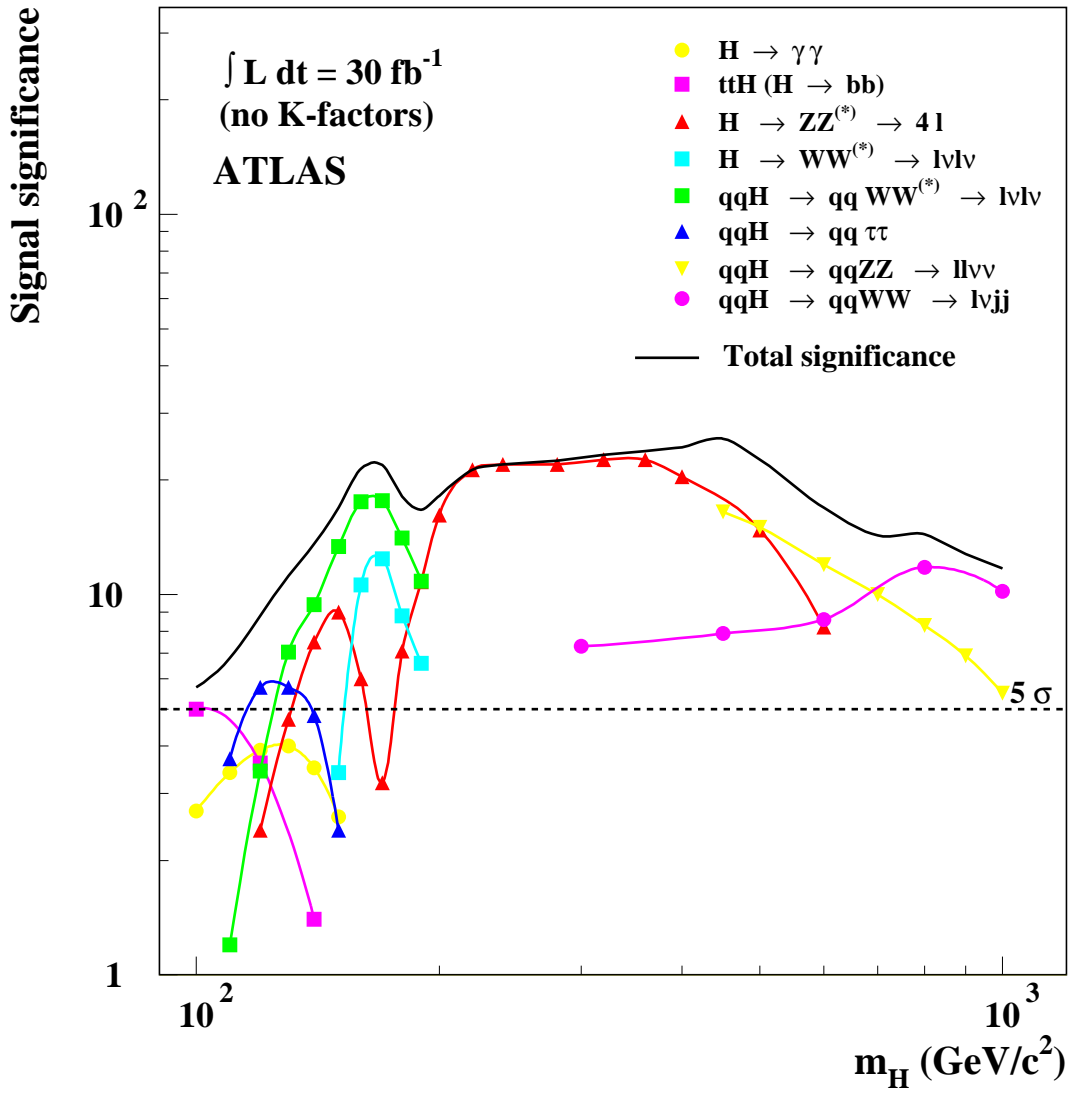
LHC

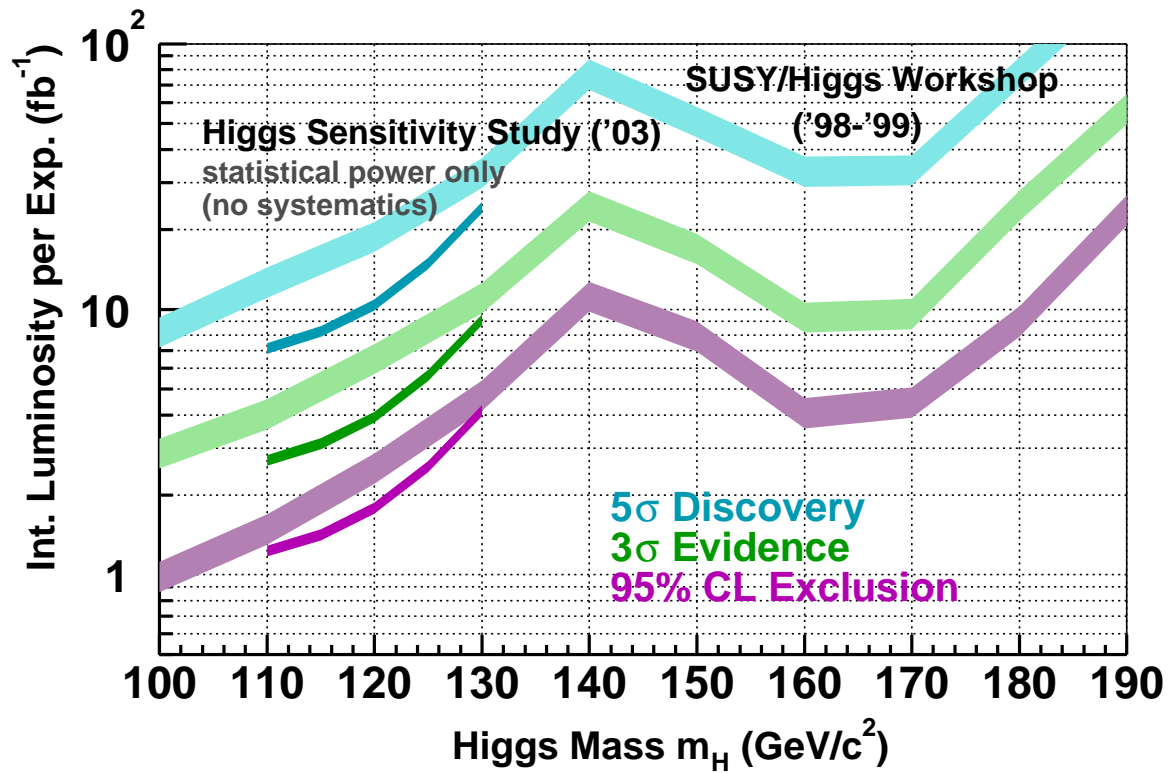












Higgs Physics Menu

$$m_H$$

elementary or composite ?
electroweak physics
 $t\bar{t}$ condensation ?

$$\Gamma_H$$

Higgs sector
Resonance shape (if wide)
How to measure ? (if narrow)

$$J^{PC} = 0^{++}$$

Branching Ratios

$H \rightarrow W^+W^-/ZZ \rightarrow$ custodial SU(2) symmetry

$H \rightarrow t\bar{t}, \tau^+\tau^-, \dots \rightarrow$ Yukawa; minimal or not ?

$H \rightarrow \gamma\gamma, Z\gamma, gg \rightarrow$ one-loop structure