

# **High-z cosmological structures and reionization**

**Ilian T. Iliev**

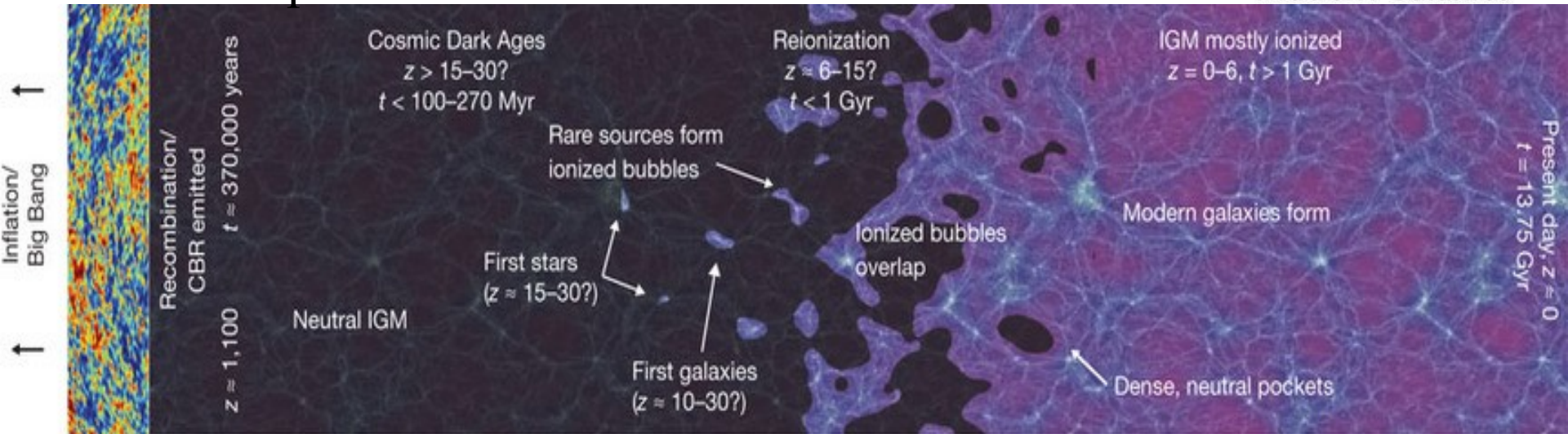
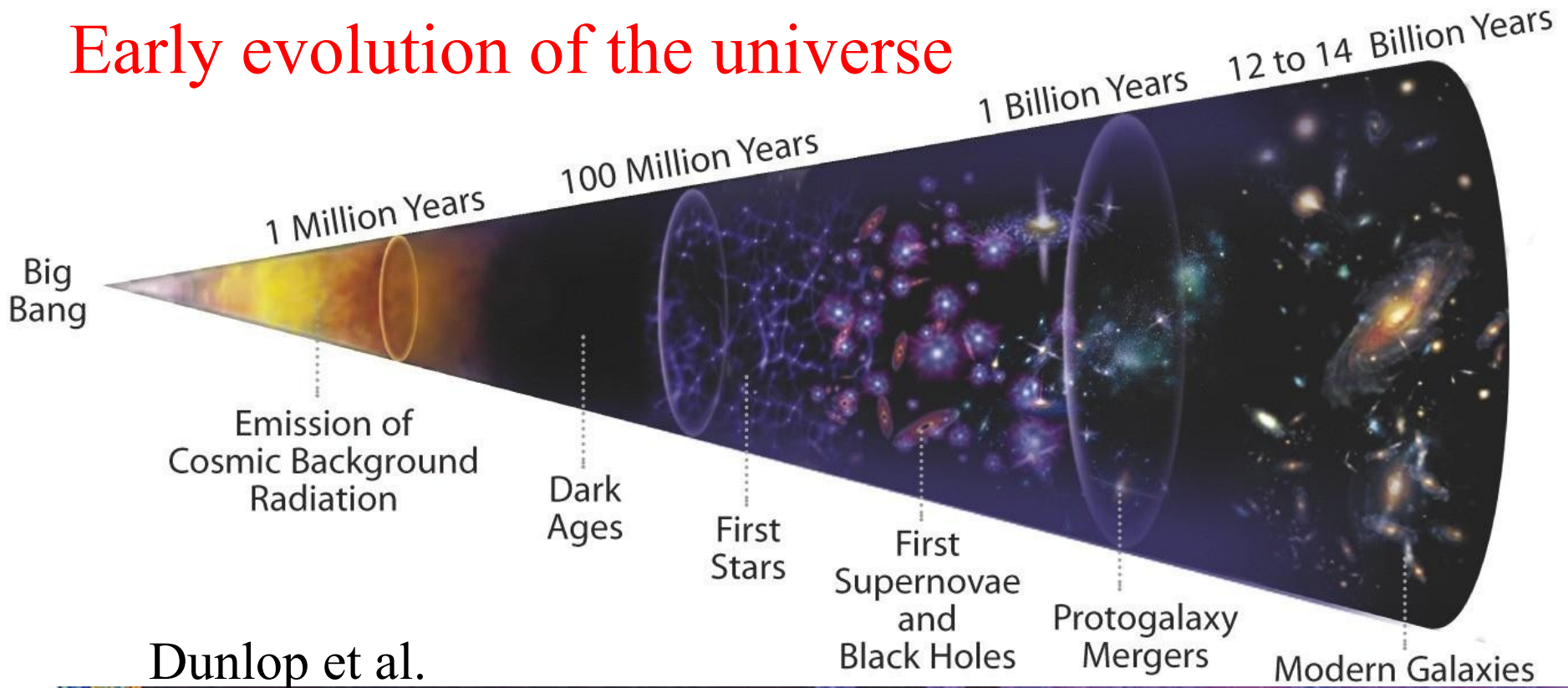
**University of Sussex**

**with**

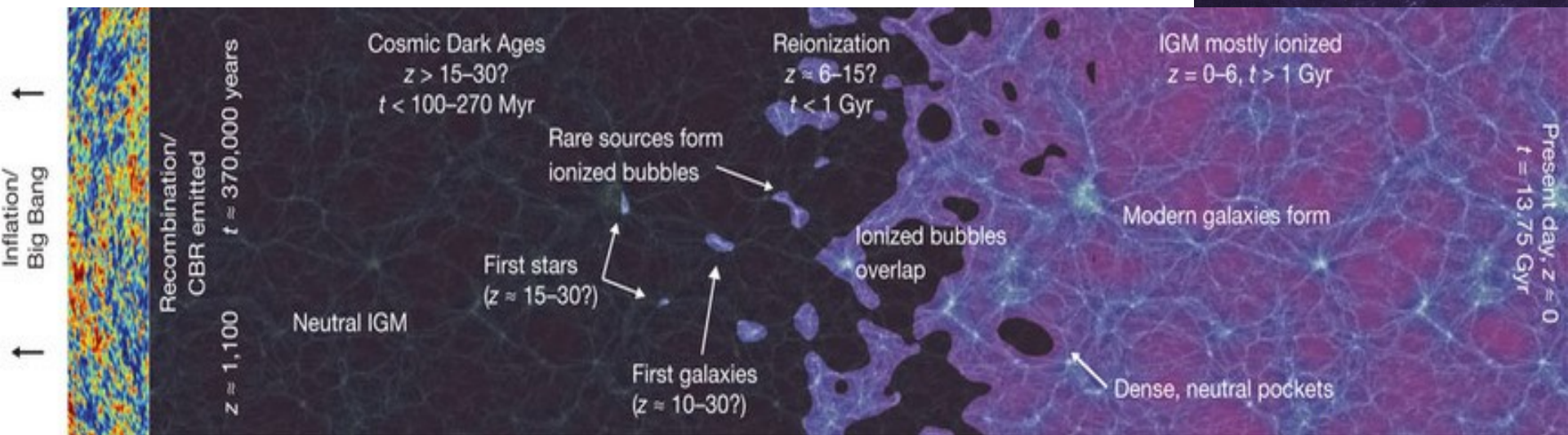
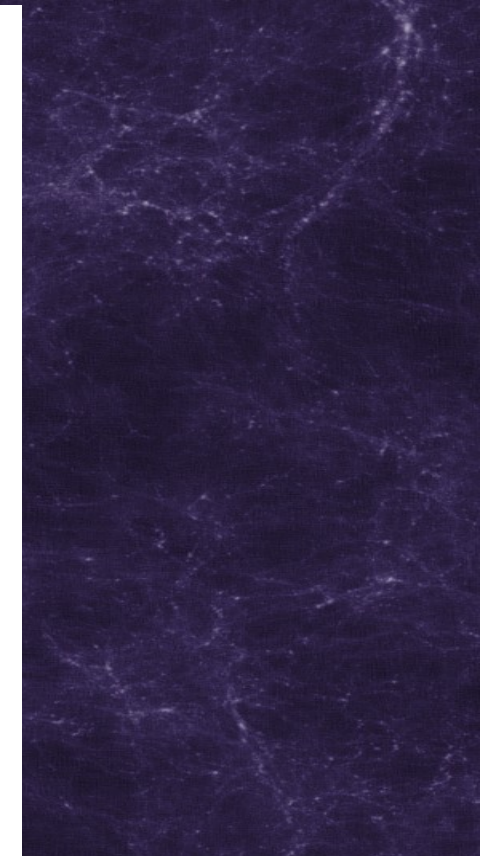
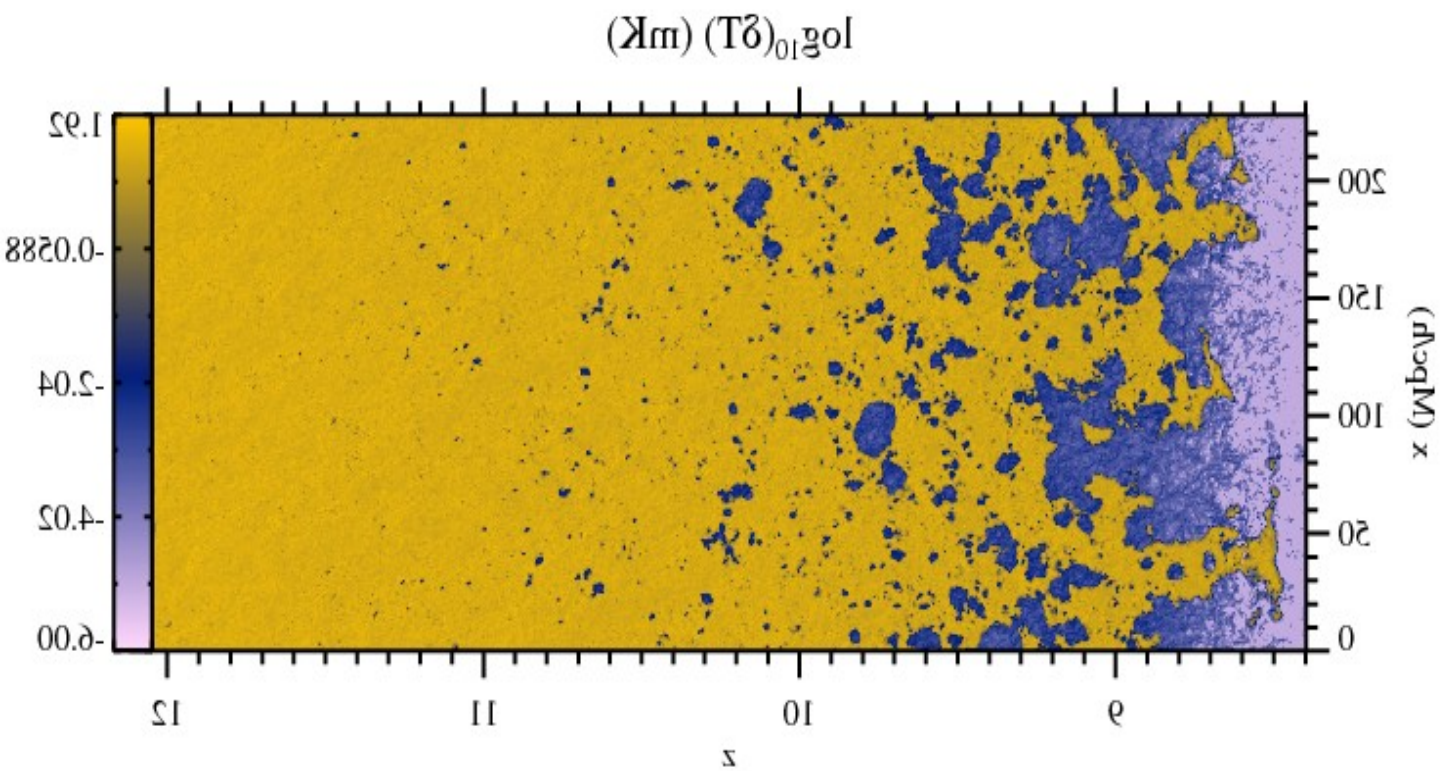
**Garrelt Mellema (Stockholm), Paul Shapiro  
(Austin), Yi Mao (Paris), Kyungjin Ahn (Chosun),  
William Watson (Sussex), Stefan Gottloeber  
(Potsdam), Gustavo Yepes (Madrid) and others**



# Early evolution of the universe







# Progress of reionization: 3D view





# Large-Scale Simulations of Reionization

**N-body: CubeP<sup>3</sup>M**  
(Harnois-Deraps, et al. 2012)

**3072<sup>3</sup>-5488<sup>3</sup> particles**  
(29 to 165 billion)

**density slices**

**velocity slices**

**halo catalogues-sources**

**Scales well at least up to**  
**21,952 cores**

114-425/h Mpc (CubeP<sup>3</sup>M)  
resolving  $10^8 - 10^9 M_{\text{solar}}$  halos

up to  $120 \times 10^6$  sources

50-100 dens. snapshots

simple source models

sub-grid clumping

no hydro – large scales.

**C<sup>2</sup>-Ray code**

(Mellema, et al. 2006)

- radiative transfer

- noneq. chemistry

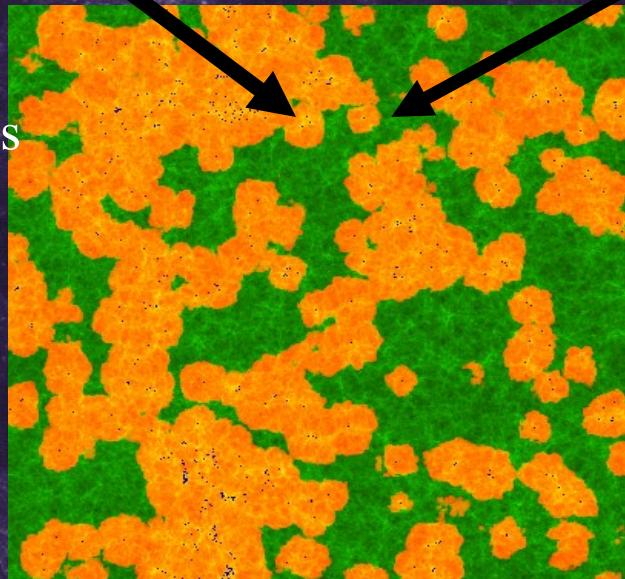
- precise

- highly efficient

- coupled to gasdynamics

- massively parallel  
(excellent scaling to  
40,000+ cores).

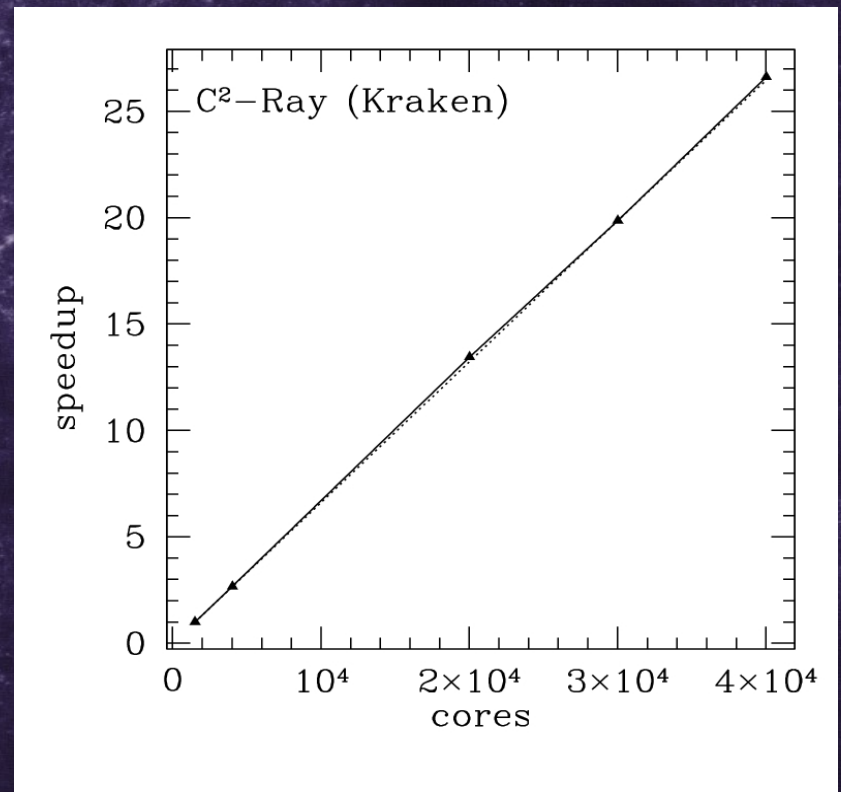
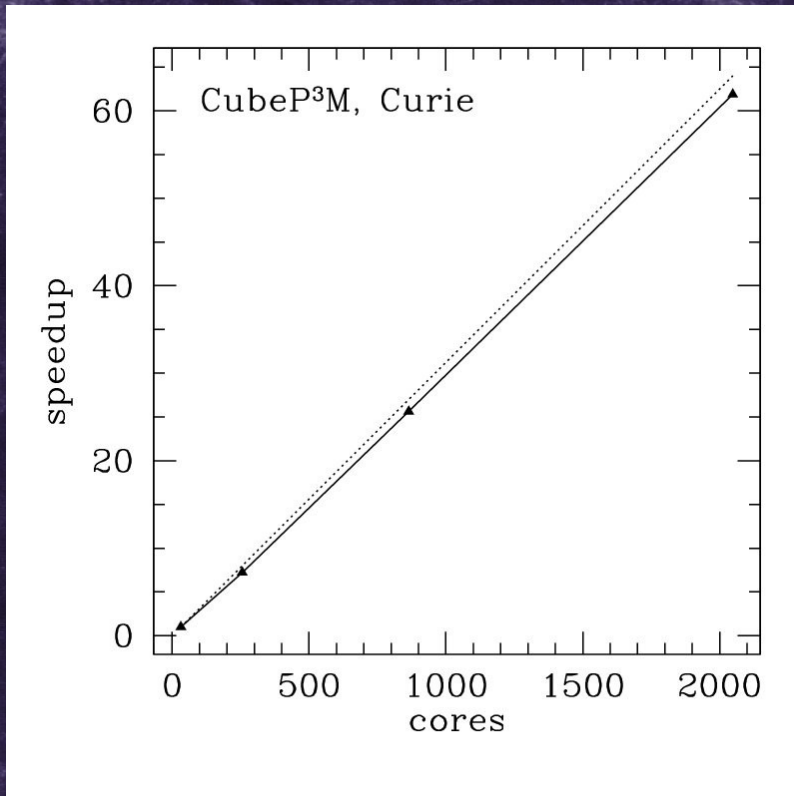
**Coupled to hydro**





# Code scaling

(Iliev et al. 2012, Harnois-Deraps et al. 2012)





# The Formation of Early Cosmic Structures

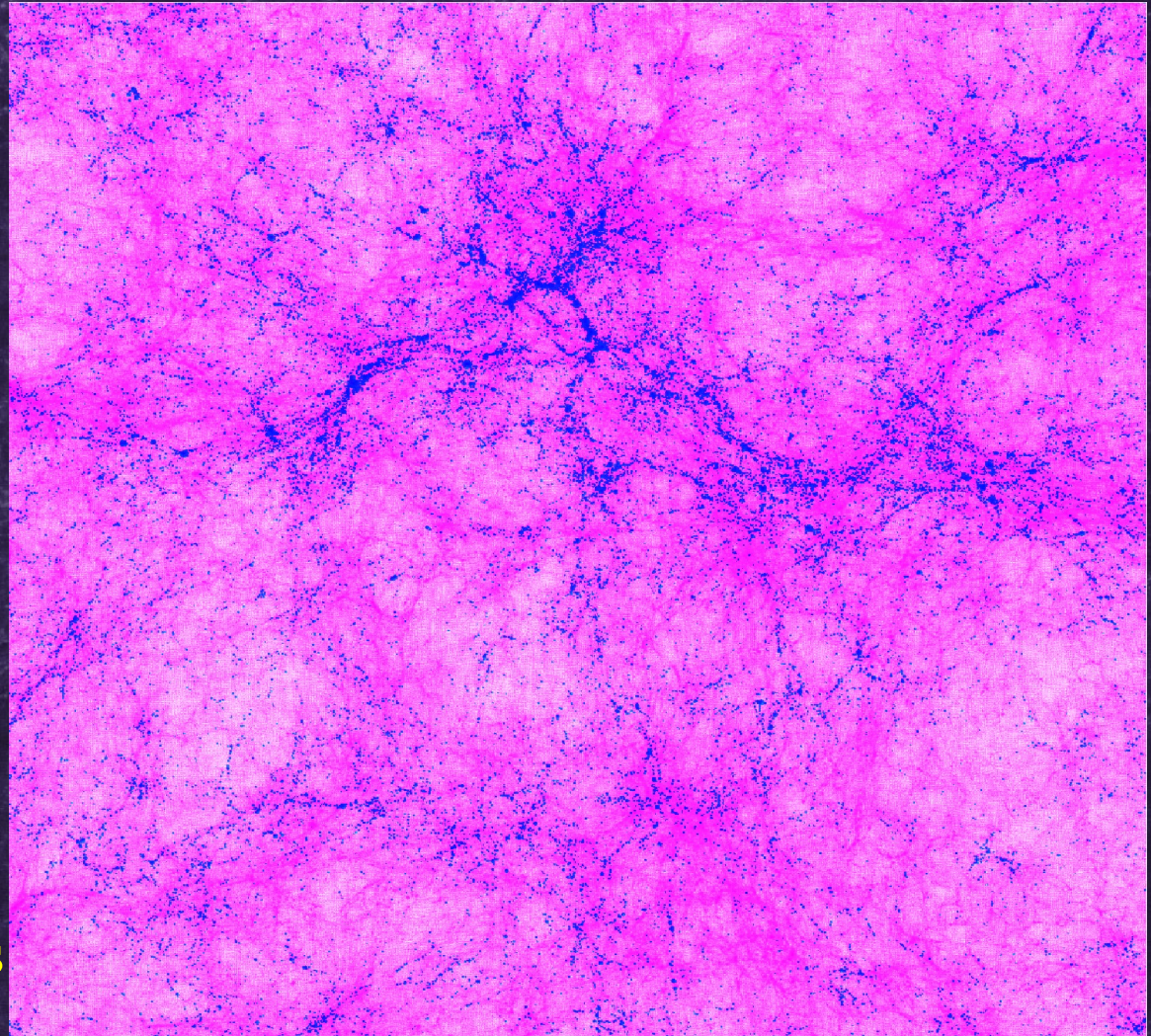
(Iliev, et al. 2006a, MNRAS, 369, 1885; Iliev et al. ArXiv1107.4772; and in prep.)

425/h Mpc box @  $z=6$   
5488<sup>3</sup> particles (165 billion),  
10,976<sup>3</sup> cells, P<sup>3</sup>M simulation  
density=violet, halos=blue  
41.5x41.5 Mpc zoomed slice

Halos  $10^9 M_{\text{solar}}$  and above  
resolved. First halos form  
at  $z \sim 26$ ; 176 million halos  
by  $z=2.6$ )

Volume comparable to  
the FOV of EoR radio  
surveys like LOFAR

All atomically-cooling halos  
( $>10^8 M_{\text{solar}}$ ) are in the RT  
( $10^8$ - $10^9 M_{\text{solar}}$  modelled  
sub-grid)



Simulation ran at Texas Advanced  
Computing Facility on 10,988-21,976 cores.



# The Formation of Early Cosmic Structures: The Very Small Scales

(Watson et al. In prep.)

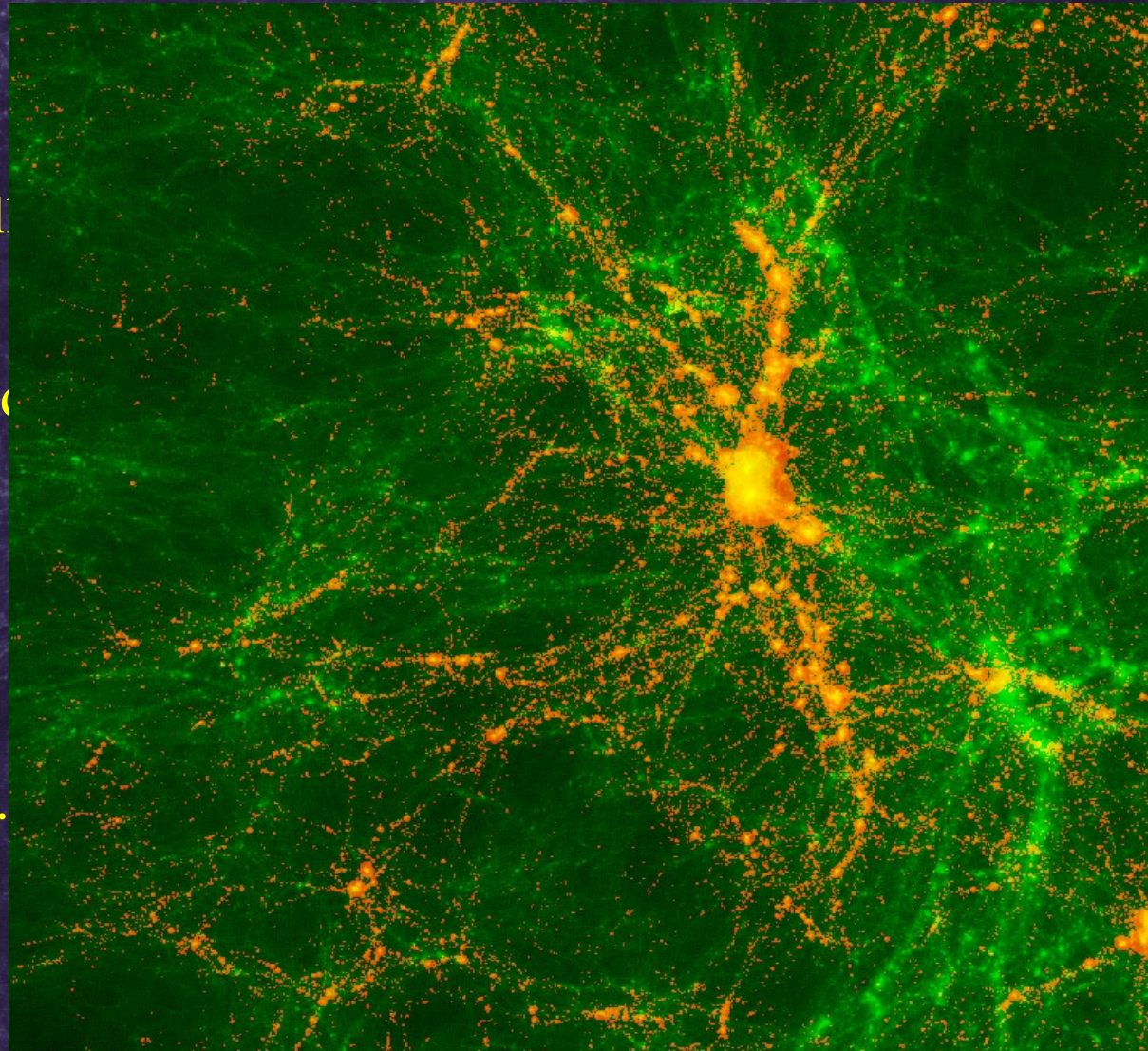
20/h Mpc box @  $z=8$ , zoom  
5488<sup>3</sup> particles (165 billion),  
10,976<sup>3</sup> cells, P<sup>3</sup>M simulation

Resolves all halos down to small  
minihalos ( $10^5 M_{\text{solar}}$ ).

Structures are highly biased  
Extend to extremely small  
scales (resolution of this  
simulation is 182 pc!)

First halos form at  $z=43$ .  
112+ million halos at  $z=8$ .

Very useful for modelling  
the effects of small-scale  
structure and 21-cm  
absorption, etc..



Simulation ran at Texas Advanced  
Computing Center on 10,976-21,952 cores.



# The Formation of Early Cosmic Structures: The Very Large Scales

(Iliev et al., in prep.)

JUBILEE project

(S. Gottloeber, G. Yepes, J. Diego, W. Watson and others)

6/h Gpc box @  $z=0$

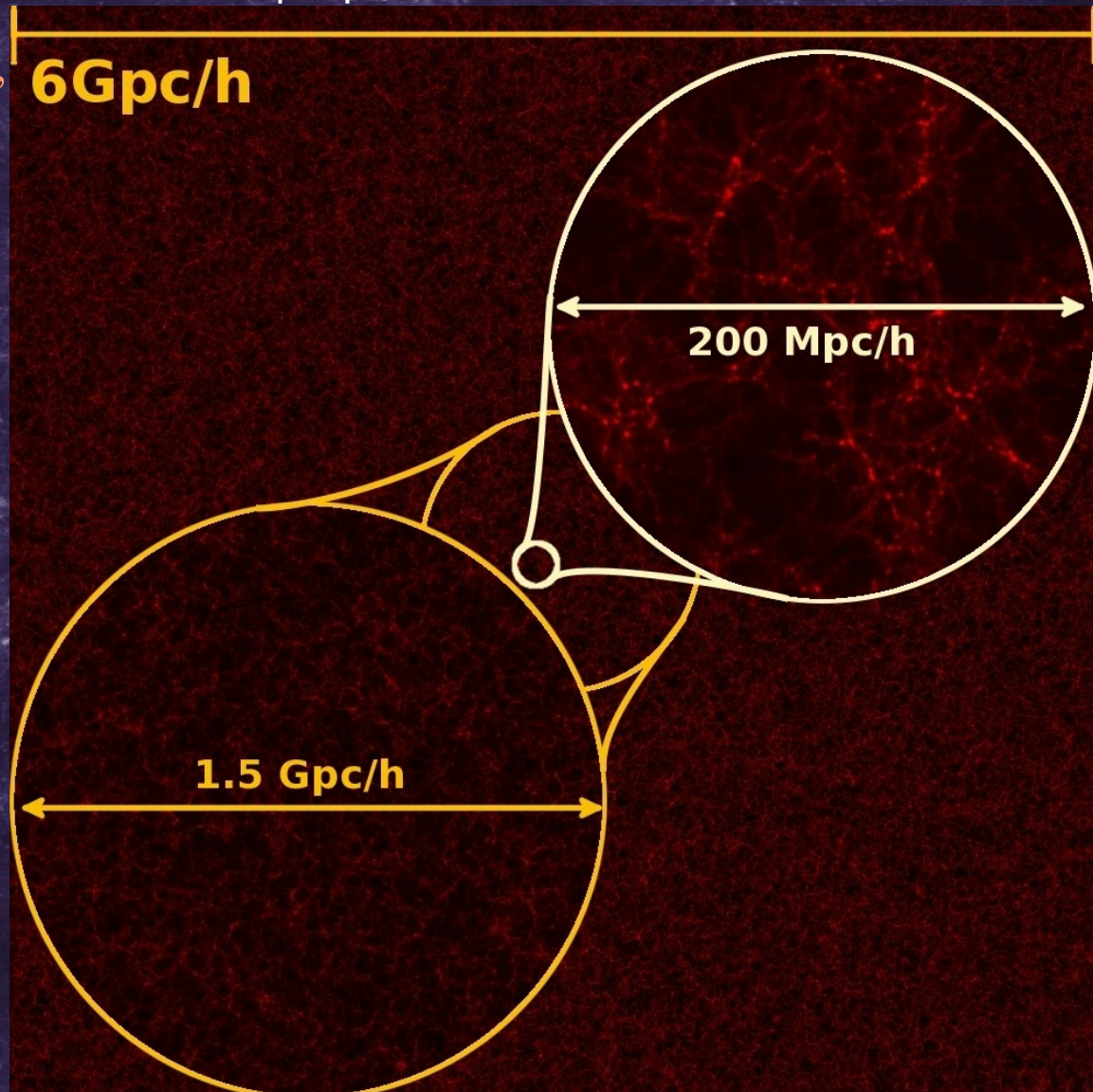
$6000^3$  particles (216 billion),

$12,000^3$  cells, P<sup>3</sup>M simulation

Volume comparable to the observable universe. Resolves all halos above  $\sim 2 \times 10^{12} M_{\text{solar}}$ .

Rich statistics: First halos form at  $z > 10$ , over 350 million halos at  $z=0$ , 8.5 million galaxy clusters at  $z=0$ .

Useful for studies of statistics and clustering of very massive, rare sources, as well as modelling of galaxy surveys and ISW.



Simulation ran on JUROPA at Juelich Supercomputing Center on 8000 cores.



# Halo mass function

(Watson et al., in prep.)

- Halo multiplicity function:

$$f(\sigma, z) \equiv \frac{M}{\rho_0(z)} \frac{dN(M, z)}{d \ln \sigma^{-1}}$$

- Fitting formula (e.g. Tinker et al. 2008):

$$f(\sigma) = A \left[ \left( \frac{\beta}{\sigma} \right)^\alpha + 1 \right] e^{-\gamma/\sigma^2}$$

- Three approaches to halo finding tested: FOF (Gadget), AHF, and CPMSO (CubeP<sup>3</sup>M).



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# Simulation suite

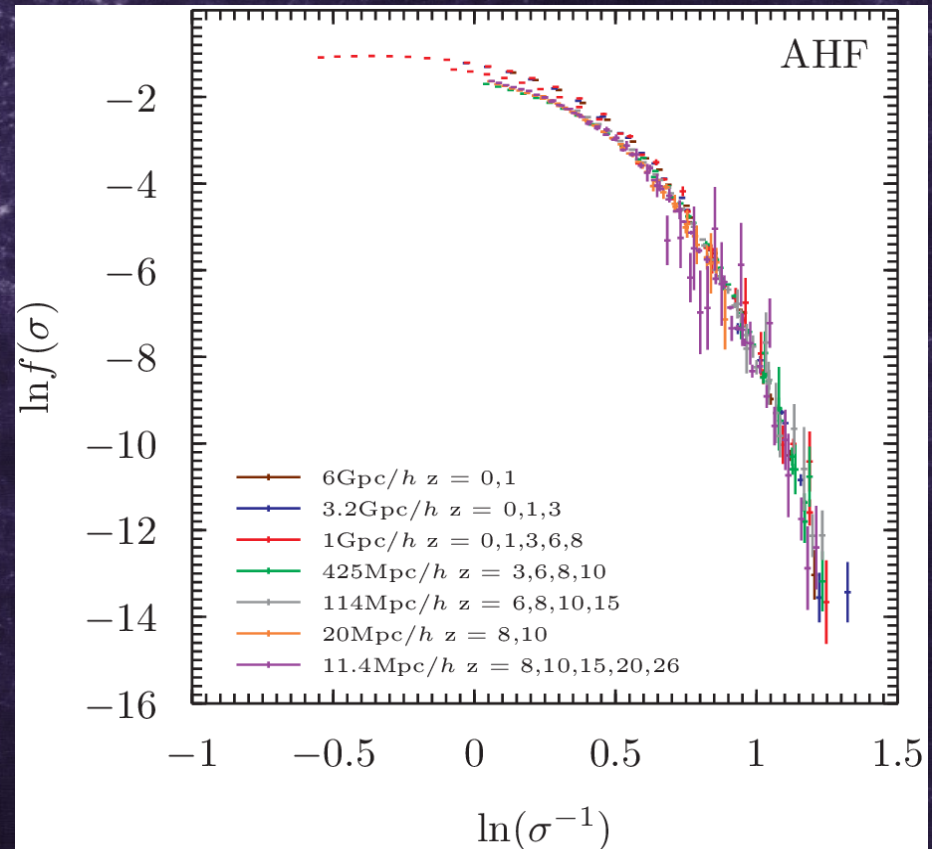
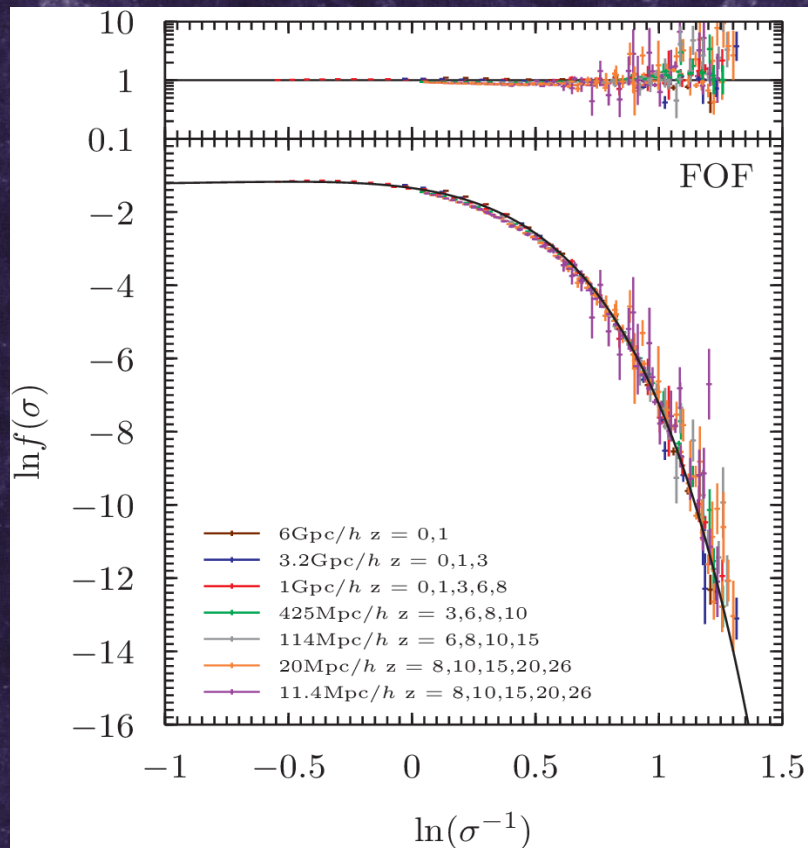
(Watson et al., in prep.)

Box Size	$N_{part}$	Mesh	Resolution	$m_{particle}$	$M_{halo,min}$	$z_{in}$	$\mathcal{P}(k)_{max}$	$\delta_{in}^{rms}$	$z_{firsthalo}$
11.4 $h^{-1}$ Mpc	3072 <sup>3</sup>	6144 <sup>3</sup>	0.18 $h^{-1}$ kpc	$5.19 \times 10^3 M_{\odot}$	$1.04 \times 10^5 M_{\odot}$	300	$2.0 \times 10^{-5}$	0.074	41
20 $h^{-1}$ Mpc	5488 <sup>3</sup>	10976 <sup>3</sup>	0.18 $h^{-1}$ kpc	$5.19 \times 10^3 M_{\odot}$	$1.04 \times 10^5 M_{\odot}$	300	$2.0 \times 10^{-5}$	0.090	44
114 $h^{-1}$ Mpc	3072 <sup>3</sup>	6144 <sup>3</sup>	1.86 $h^{-1}$ kpc	$5.47 \times 10^6 M_{\odot}$	$1.09 \times 10^8 M_{\odot}$	300	$1.2 \times 10^{-5}$	0.074	30
425 $h^{-1}$ Mpc	5488 <sup>3</sup>	10976 <sup>3</sup>	3.87 $h^{-1}$ kpc	$5.27 \times 10^7 M_{\odot}$	$1.05 \times 10^9 M_{\odot}$	300	$9.5 \times 10^{-6}$	0.137	25
1000 $h^{-1}$ Mpc	3456 <sup>3</sup>	6912 <sup>3</sup>	14.47 $h^{-1}$ kpc	$2.8 \times 10^9 M_{\odot}$	$5.50 \times 10^{10} M_{\odot}$	150	$4.6 \times 10^{-4}$	0.011	17
3200 $h^{-1}$ Mpc	4000 <sup>3</sup>	8000 <sup>3</sup>	40.00 $h^{-1}$ kpc	$5.8 \times 10^{10} M_{\odot}$	$1.16 \times 10^{12} M_{\odot}$	120	$4.5 \times 10^{-4}$	$3.39 \times 10^{-6}$	11
6000 $h^{-1}$ Mpc	6000 <sup>3</sup>	12000 <sup>3</sup>	50.00 $h^{-1}$ kpc	$1.07 \times 10^{11} M_{\odot}$	$2.14 \times 10^{12} M_{\odot}$	100	$2.8 \times 10^{-5}$	$1.22 \times 10^{-7}$	11



# Halo mass function through the cosmic ages

(Watson et al, in prep.)



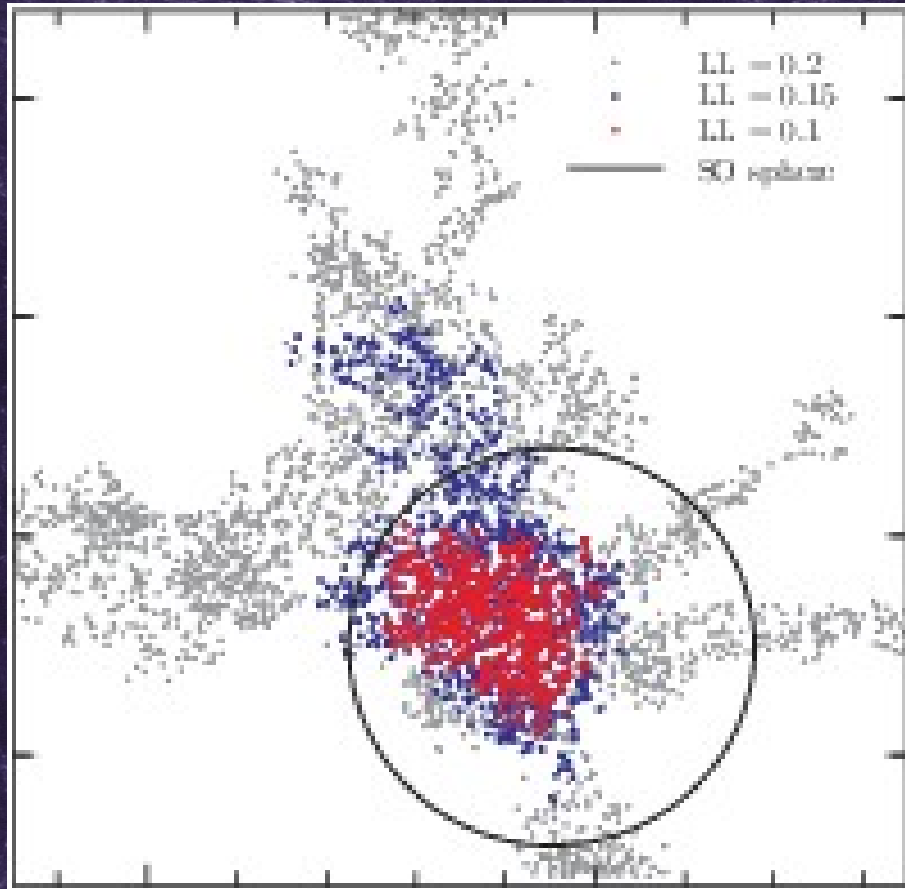
FOF: universal shape

SO: redshift- and  $\Omega$ -dependent



# Effect of FOF linking length

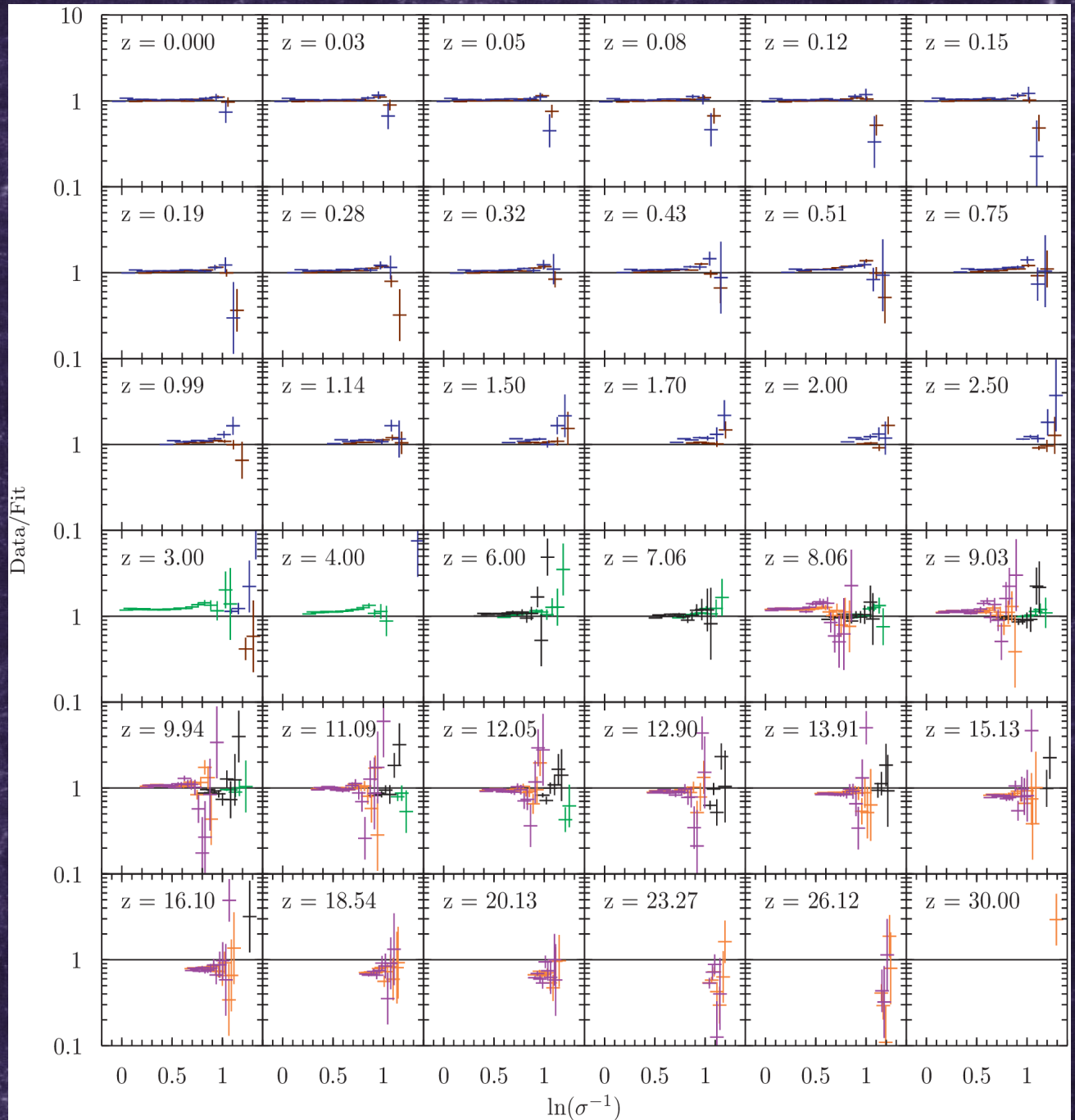
(Watson et al., in prep.)



- Linking length (ll) is a parameter used for defining FOF halos.
- Typically a fixed value of  $ll=0.2$  is used.
- At higher- $z$  this is not appropriate value and among other issues results in over-linking.
- Shorter ll produces more sensible results.

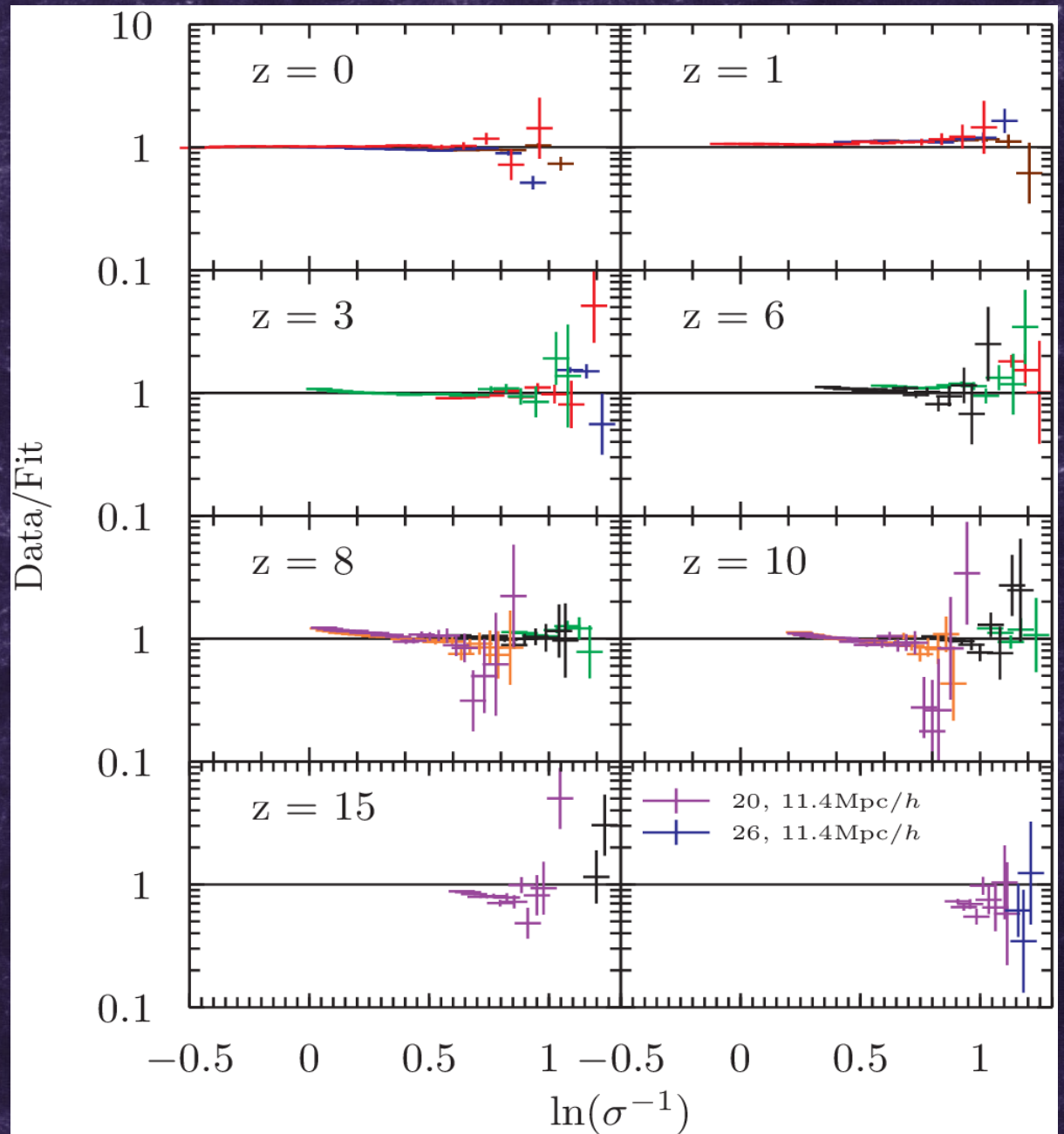


# Halo mass function fit: CPMSO (Watson et al., in prep.)



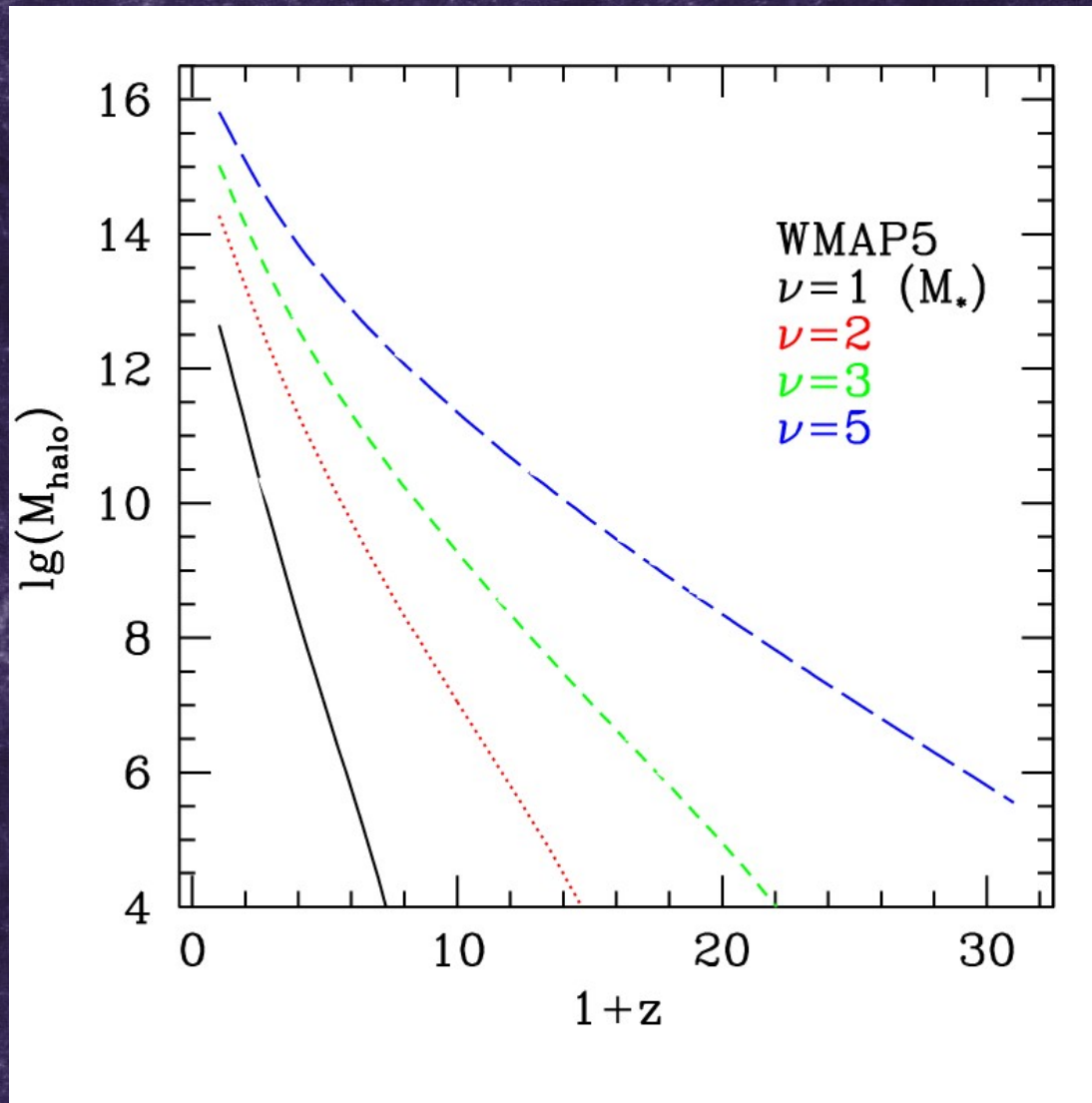


# Halo mass function fit: AHF (Watson et al., in prep.)





# How rare are halos?





# Scales of reionization

607 Mpc

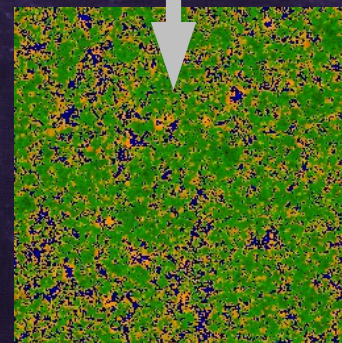
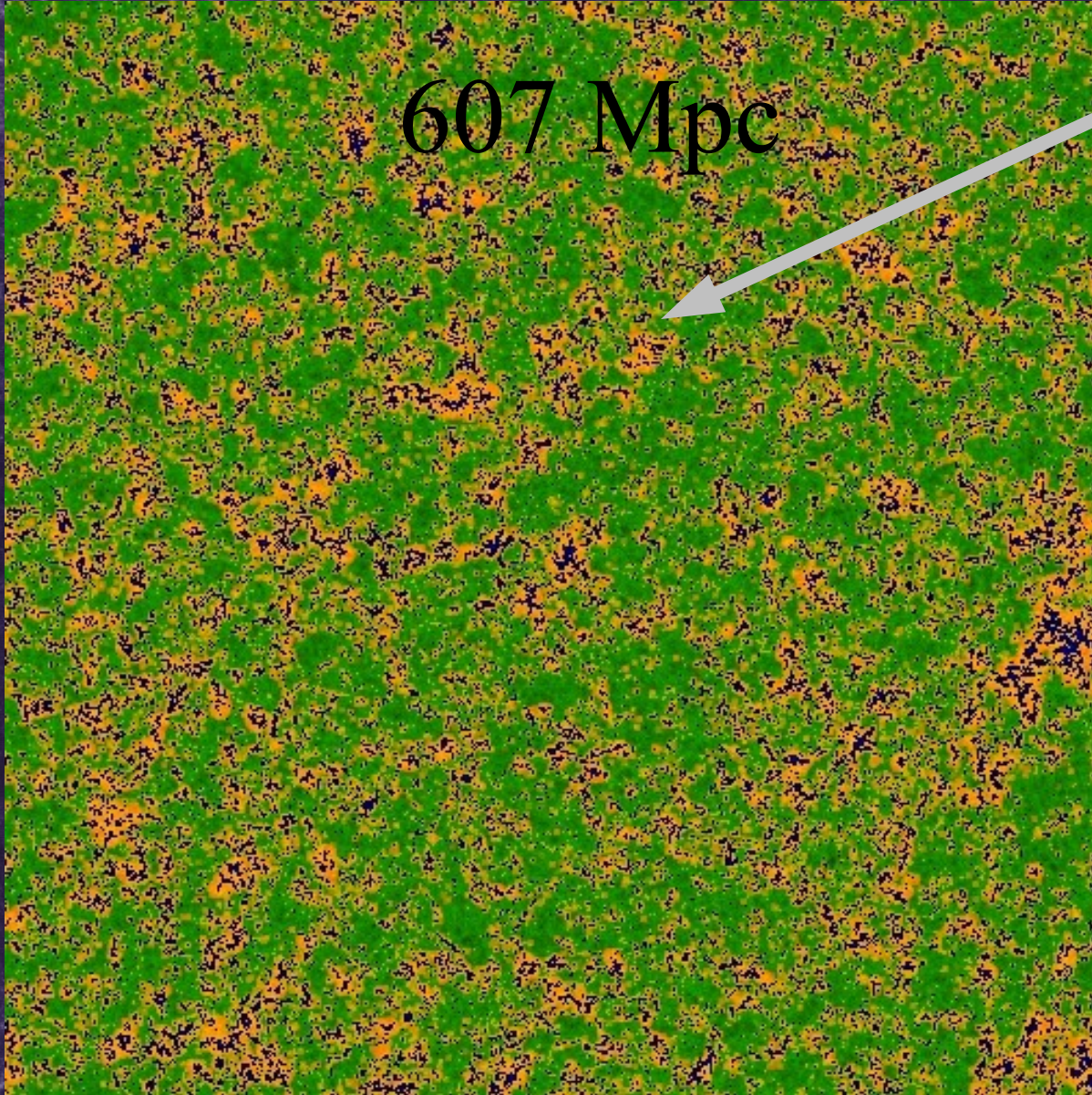
New large-scale  
EoR simulation

Previous  
large-scale

163 Mpc

9 Mpc

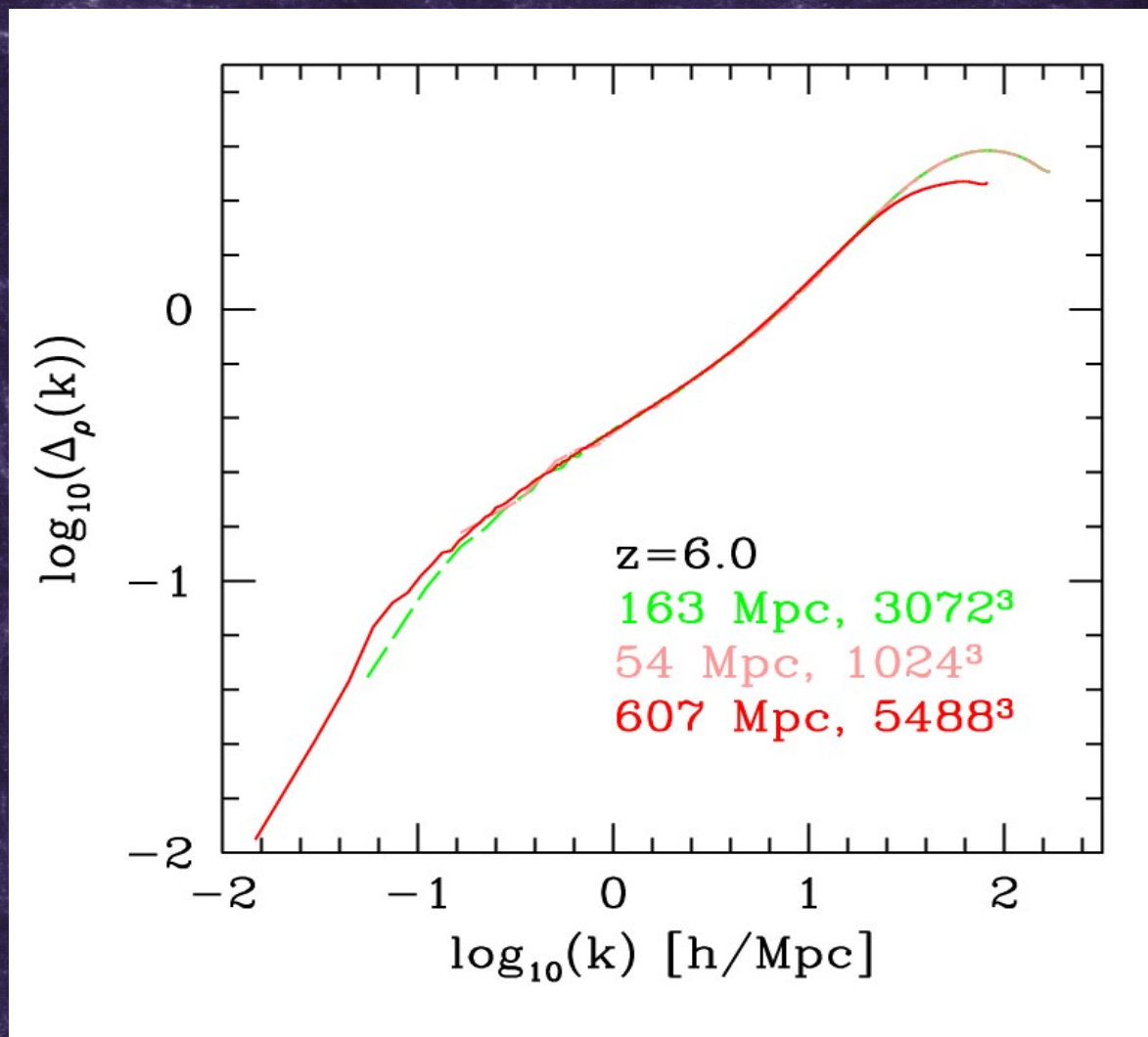
Typical hydro  
sim.  $\sim$  radio beam





# Density fluctuations: power

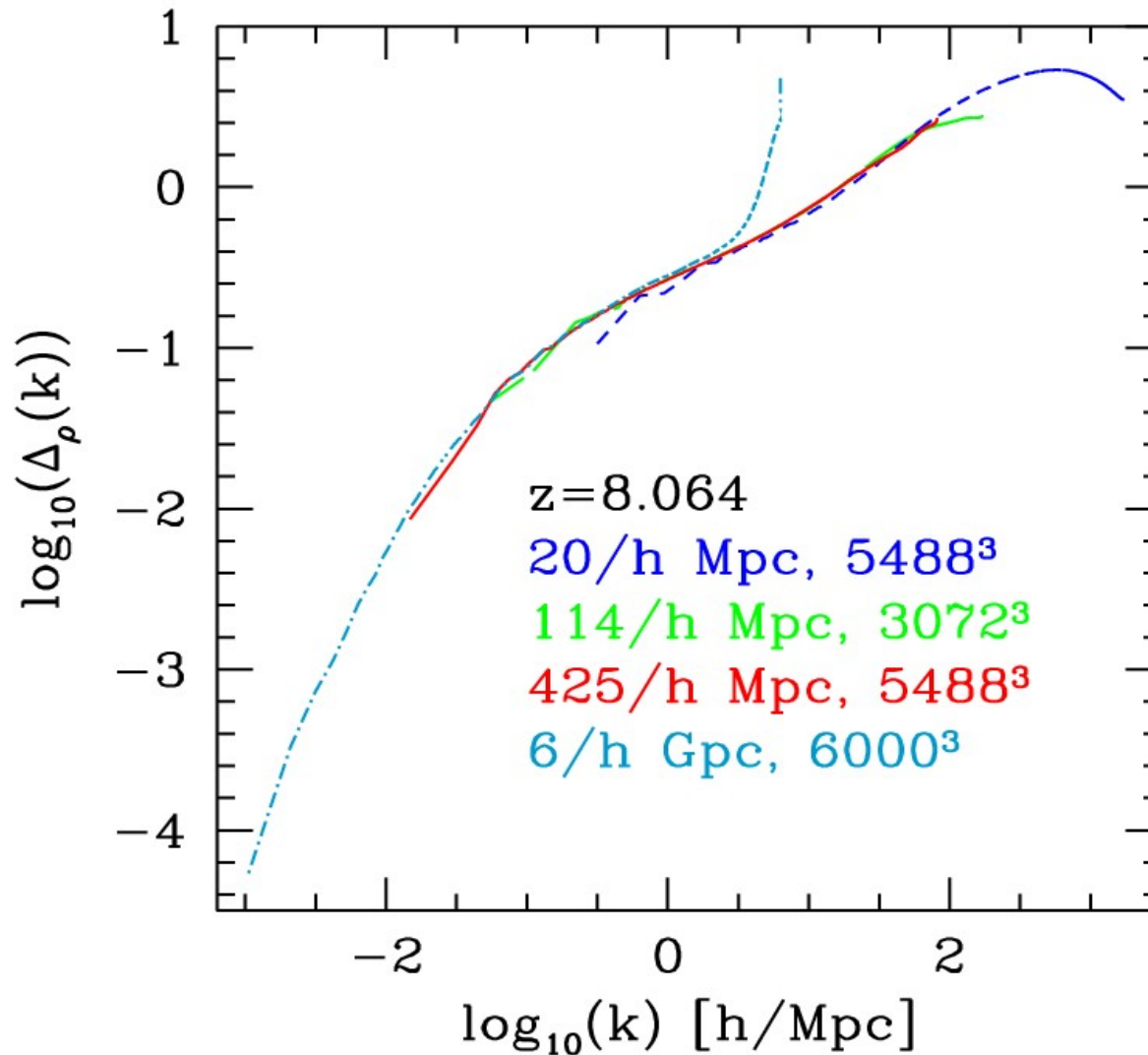
(Iliev et al., in prep.)





# Density fluctuations: power

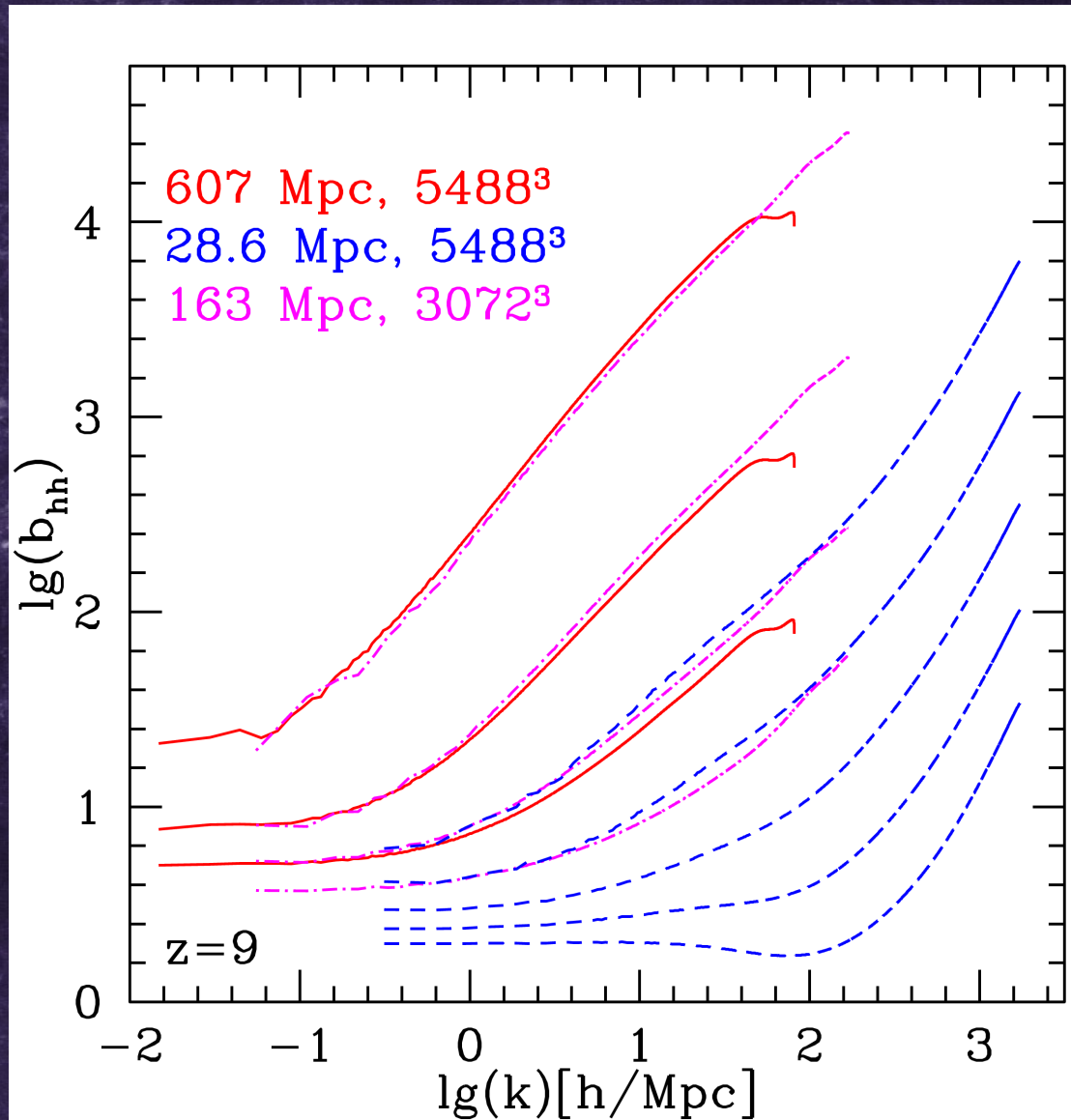
(Iliev et al., in prep.)





# The high- $z$ halo bias (Iliev et al., in prep.)

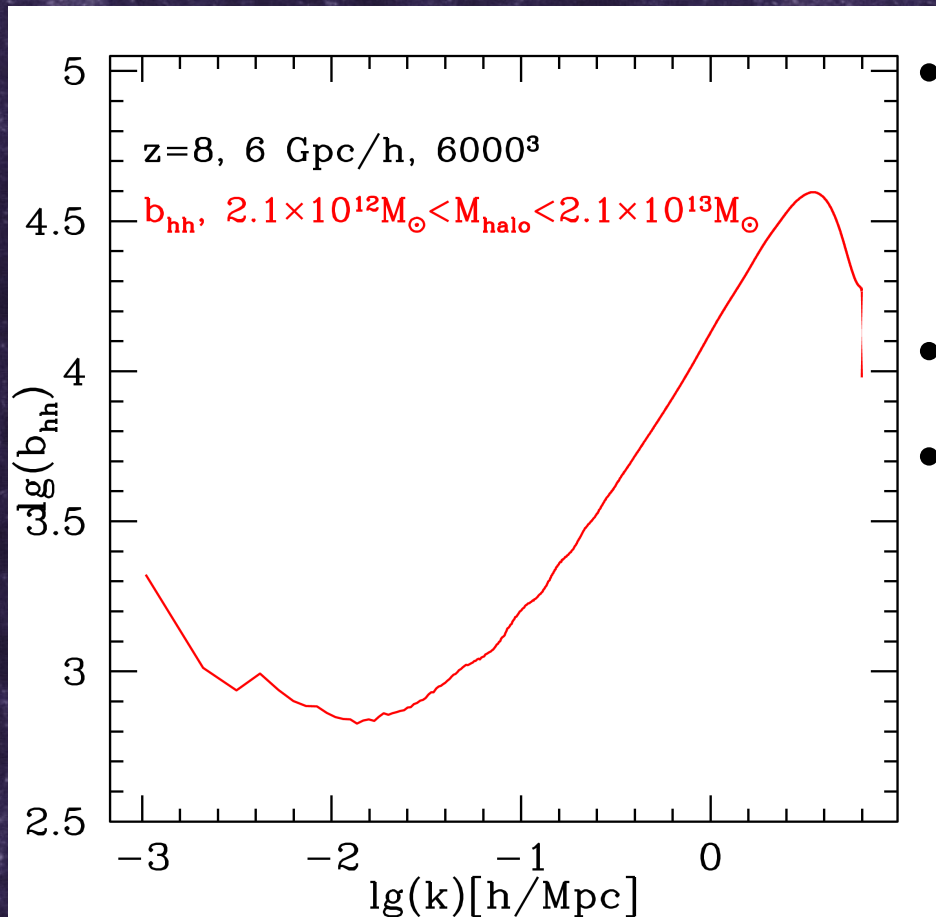
- Halos at high- $z$  are strongly clustered.
- Bias increases fast with halo mass and can reach a thousands in the nonlinear regime.
- Scale at which bias becomes linear varies significantly with halo mass.
- Simulations with different resolutions agree fairly well in the overlapping mass ranges.





# The high- $z$ halo bias: extreme objects

(Iliev et al., in prep.)



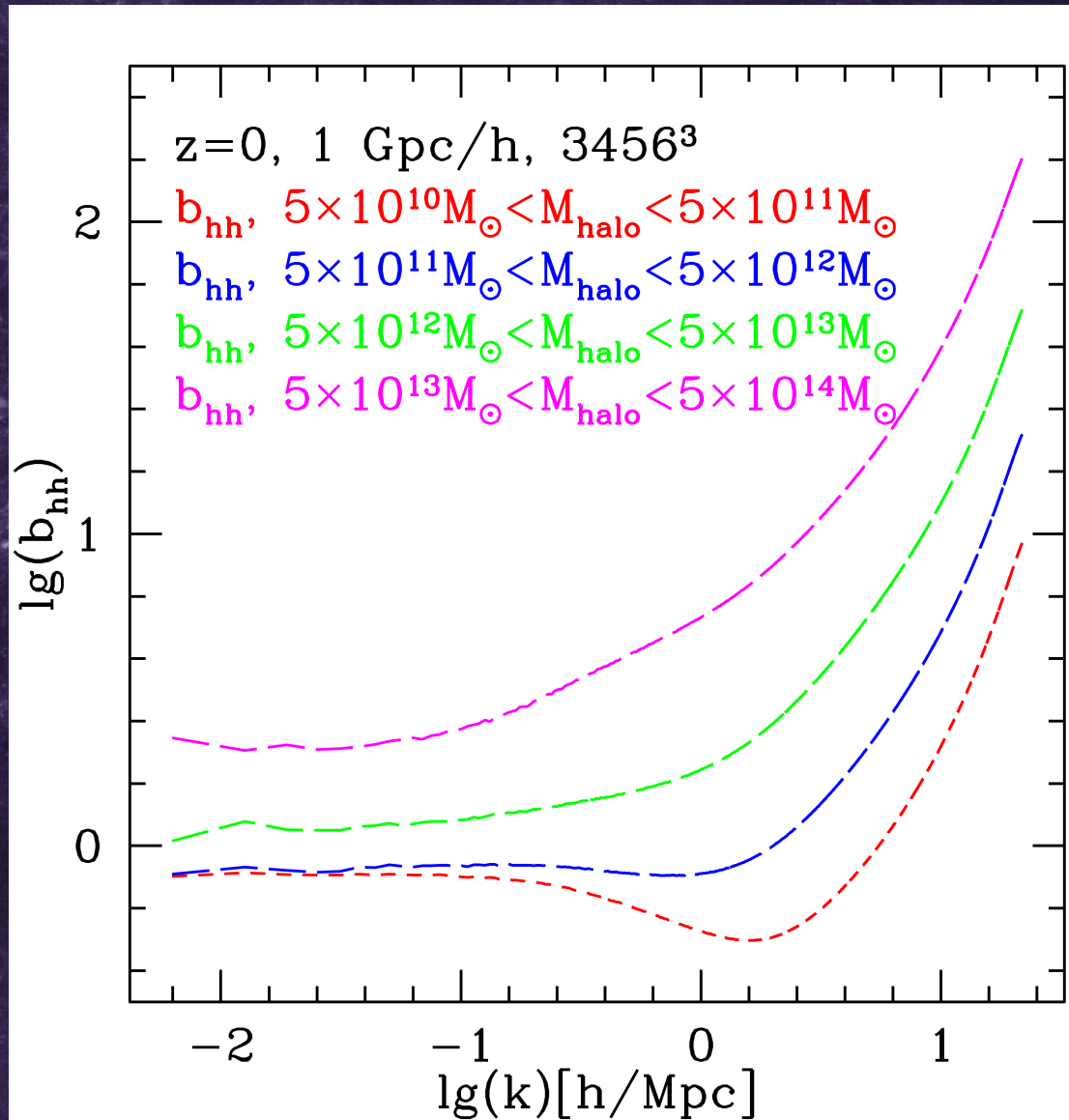
- $\sim 750$  MW+-size objects resolved at  $z=8$
- Those extreme objects, located at the highest density peaks are very highly clustered at these redshifts



# $z=0$ halo bias

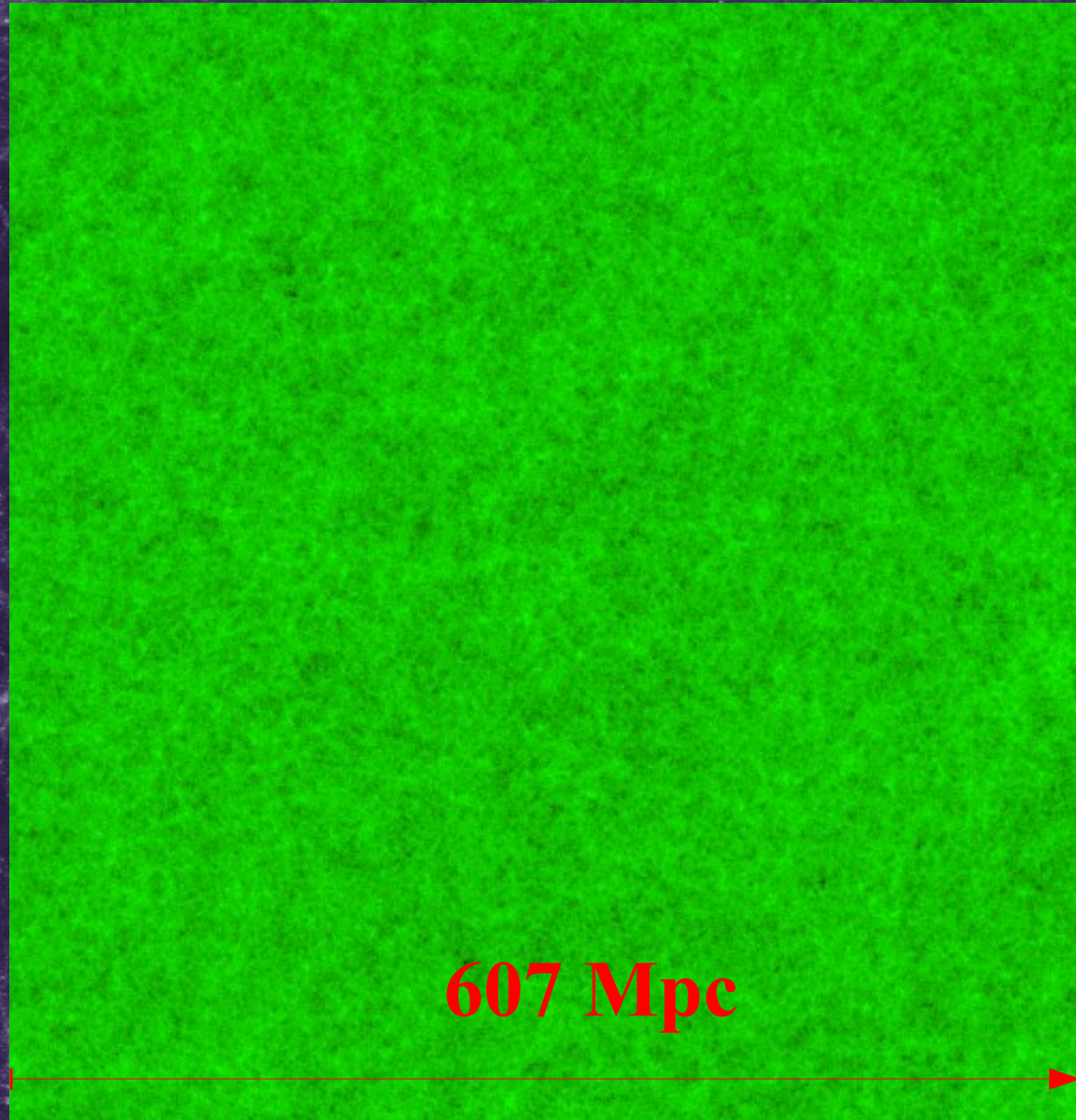
(Iliev et al, in prep.)

- Halos at  $z=0$  are much less clustered.
- Scale at which bias becomes linear varies significantly with halo mass.
- Smallest halos (below  $M_* \sim 5e12$ ) are anti-biased ( $b < 1$ ), as expected.





# Large-scale reionization: movie





# Large-scale Structure of Reionization

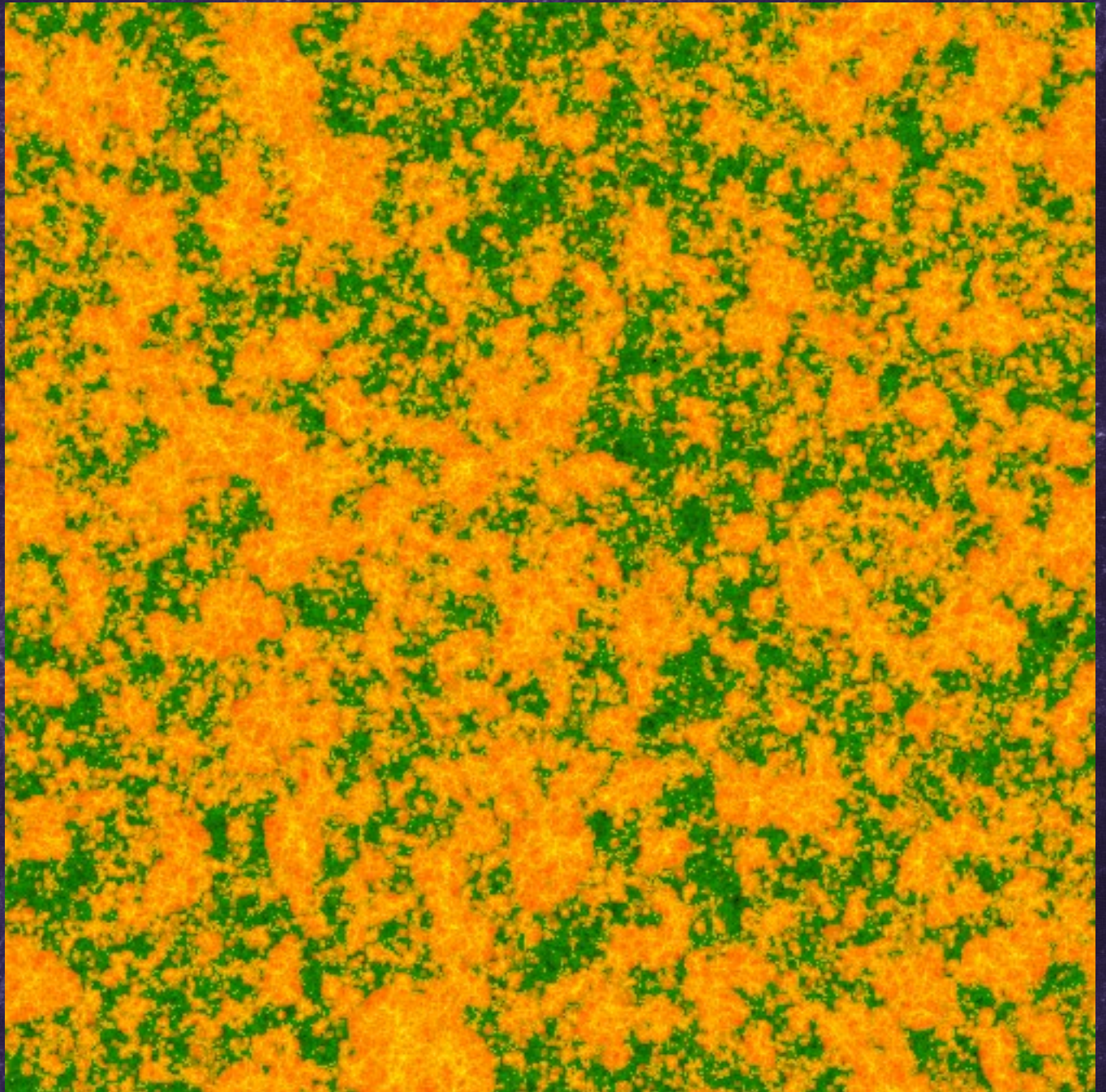
(Iliev et al, in prep.)

$z=7.35$

$x_m \sim 0.5$

425 Mpc/h

$504^3$  RT

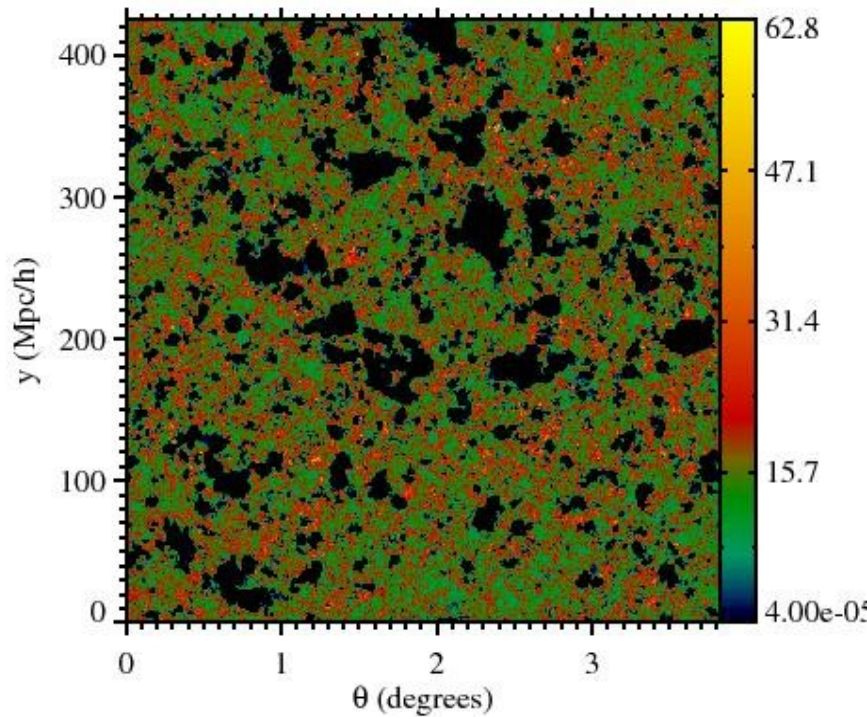




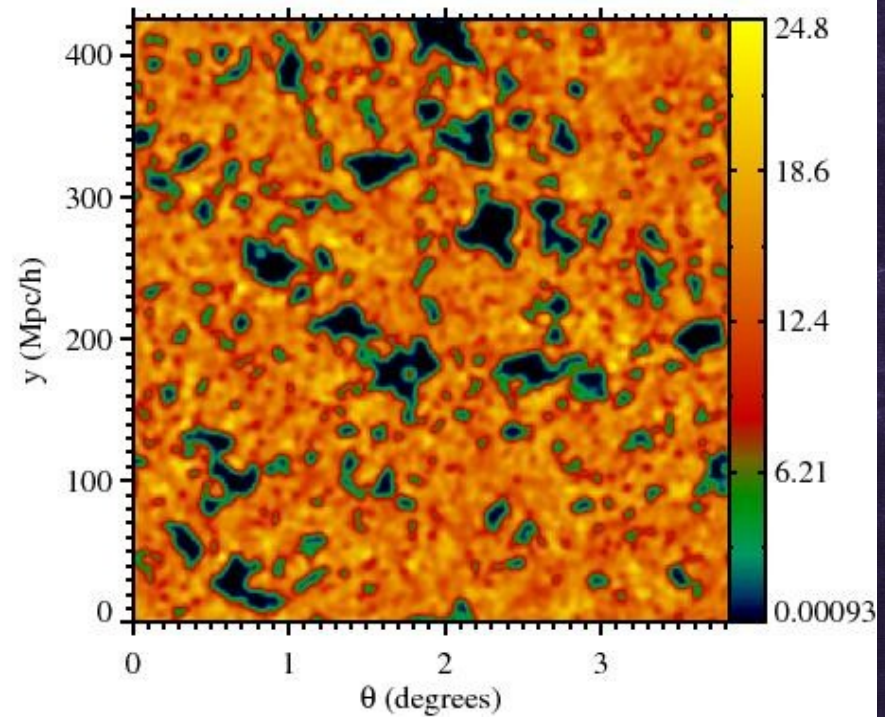
# LOFAR resolution

(Iliev et al, in prep.)

$\delta T$  (mK) at  $z=7.48$



$\delta T$  (mK) at  $z=7.48$  ( $3'$ , 0.5 MHz)



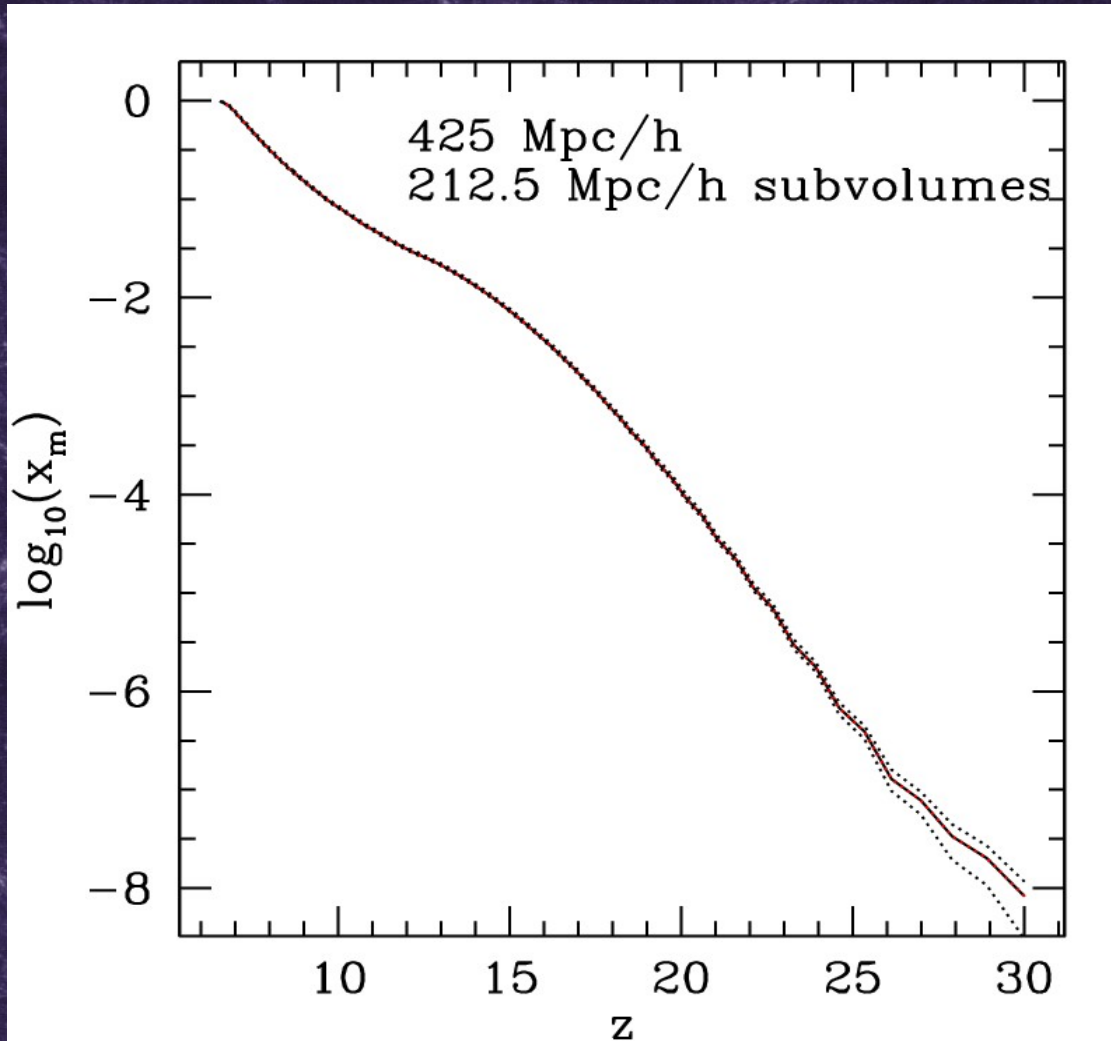






# Reionization history: how big volume is big enough?

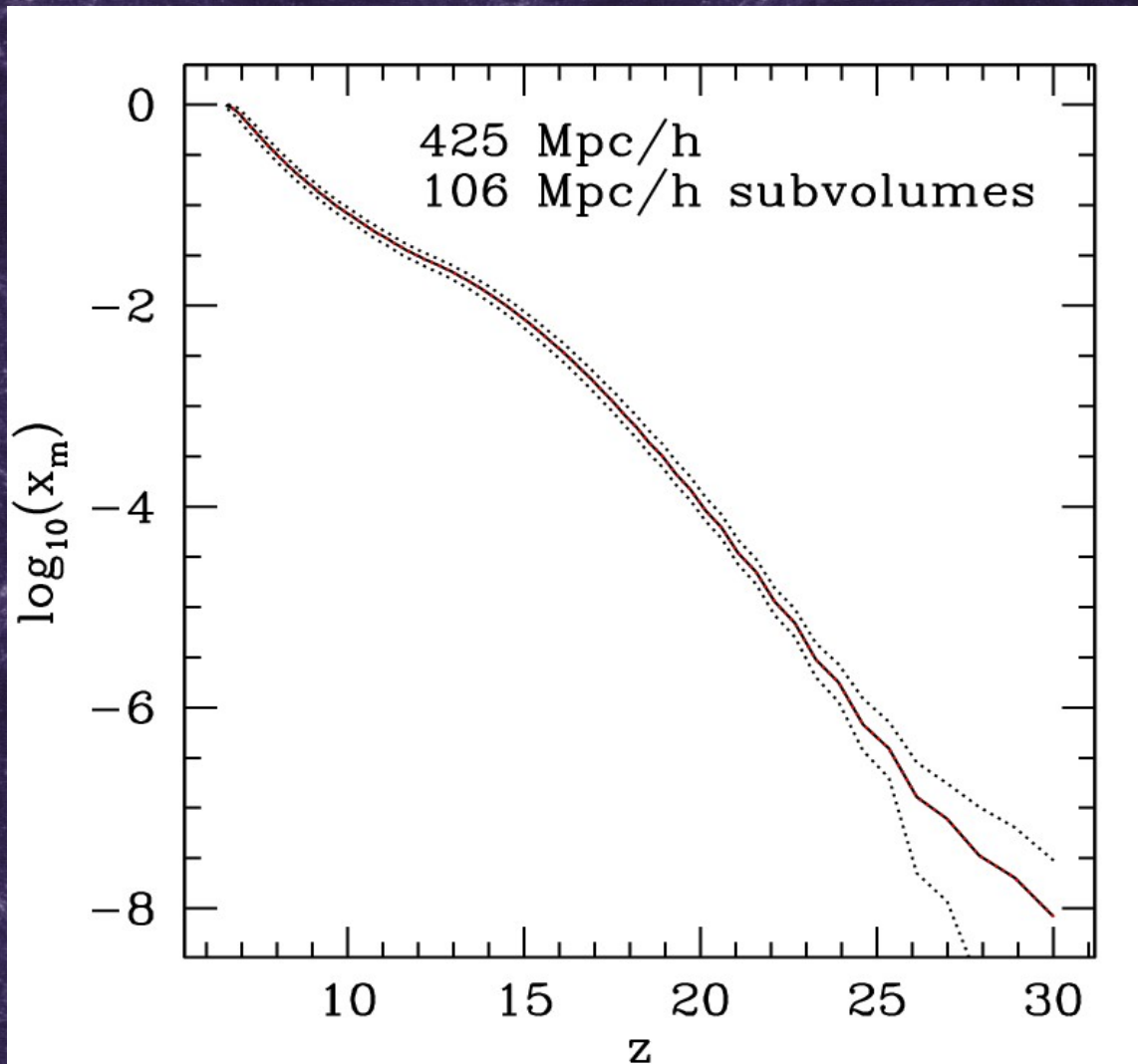
(Iliev et al, in prep.)





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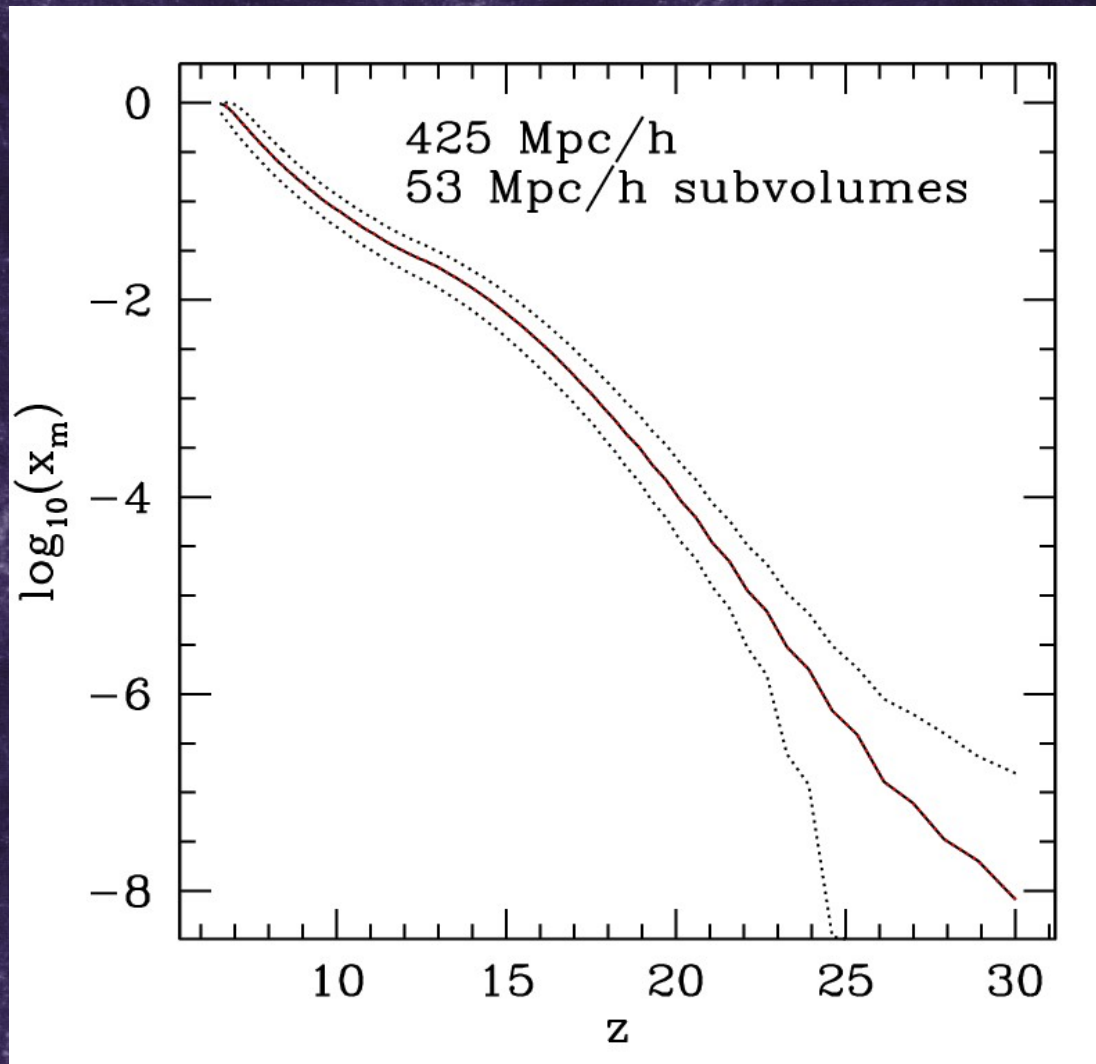
(Iliev et al, in prep.)





# Reionization history: how big volume is big enough?

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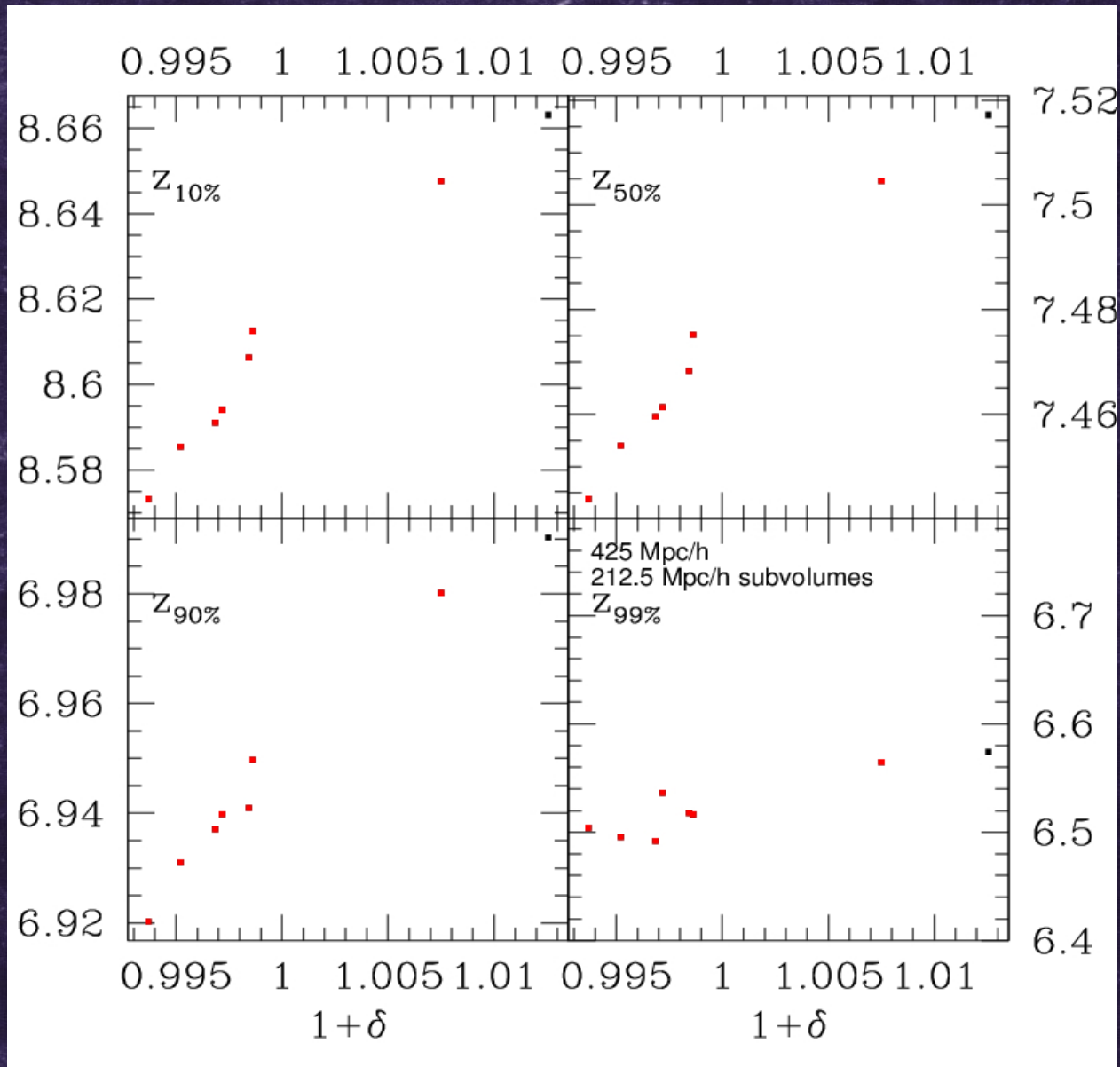




# Ionization history stages

(Iliev et al, in prep.)

black: all  
red: mean  
density

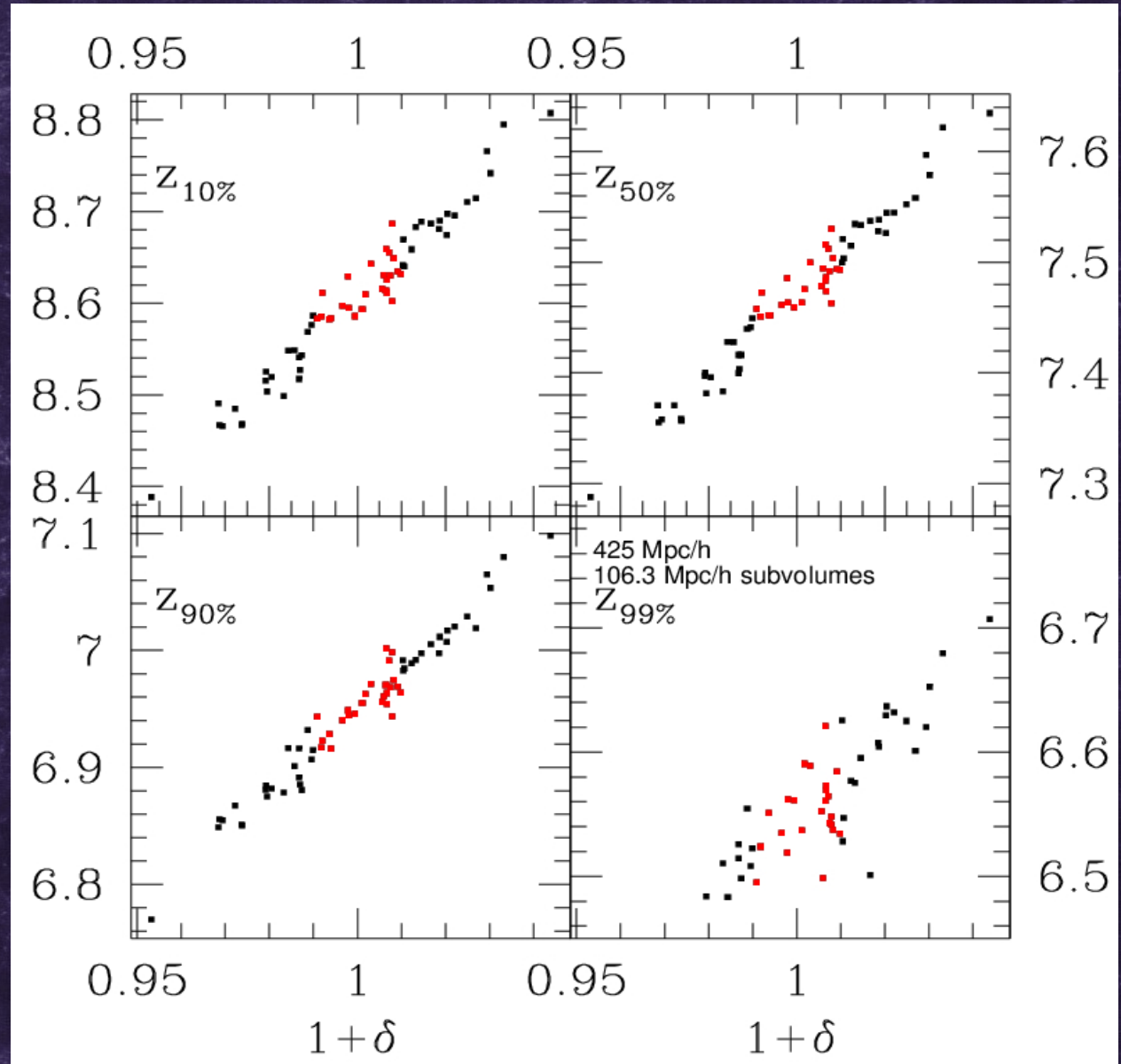




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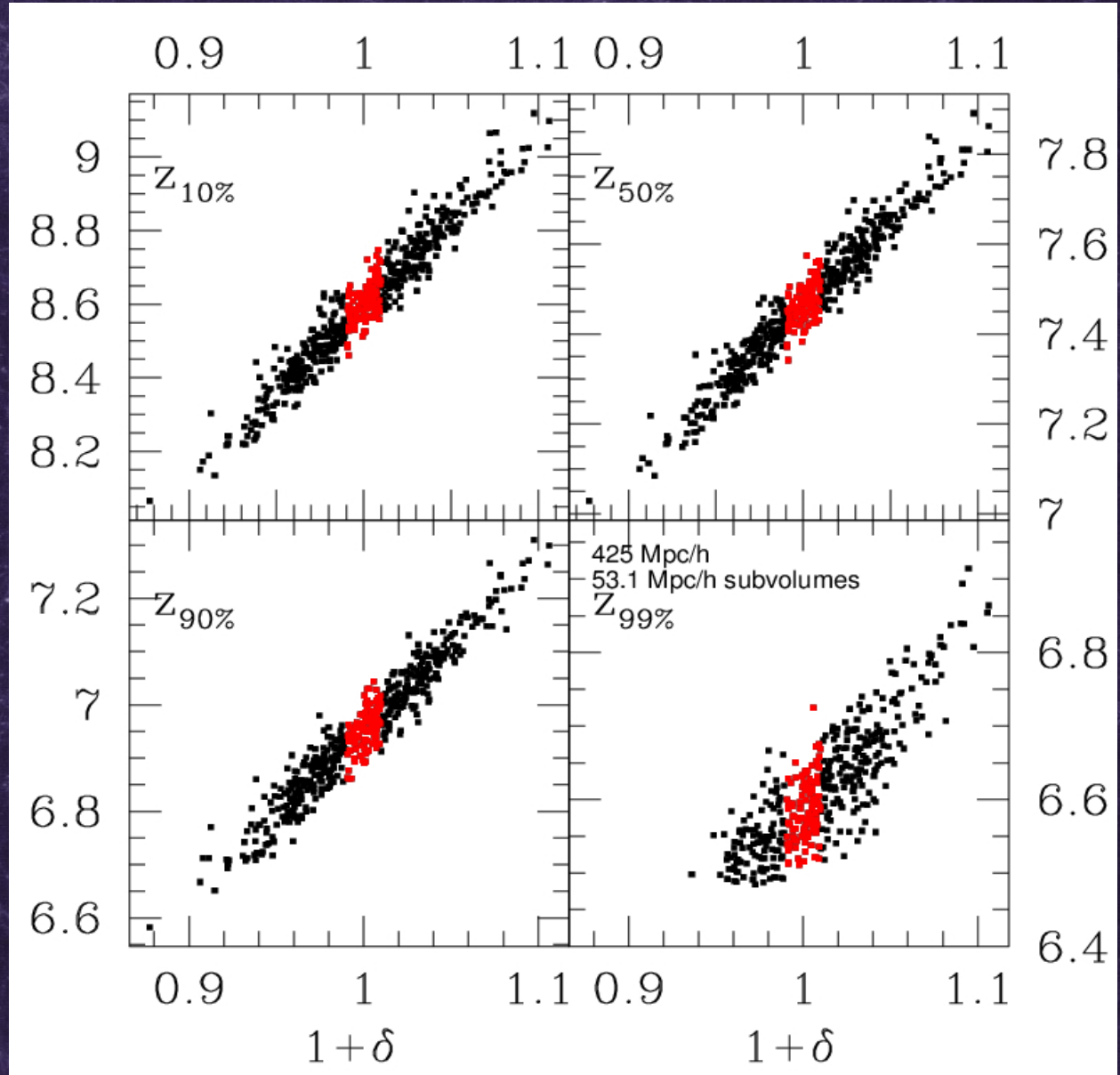




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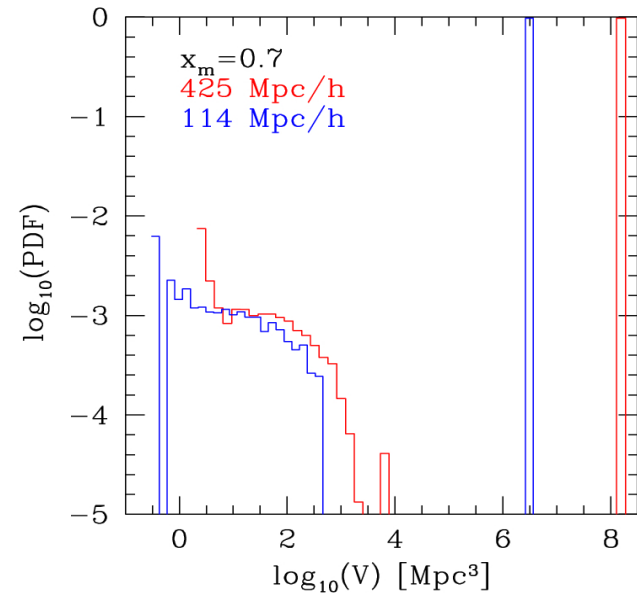
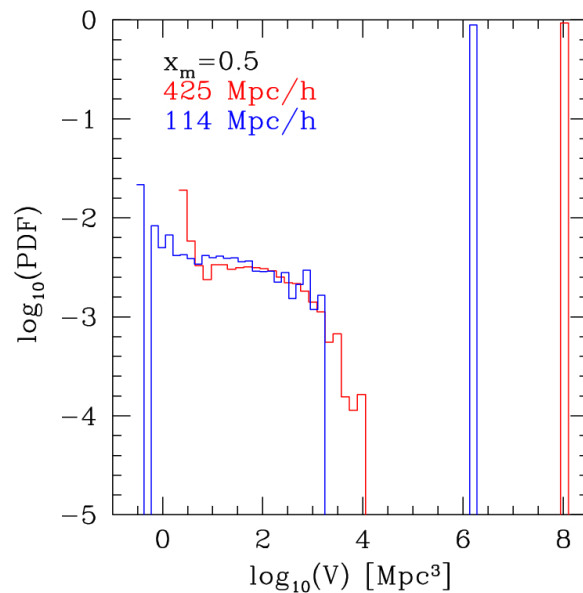
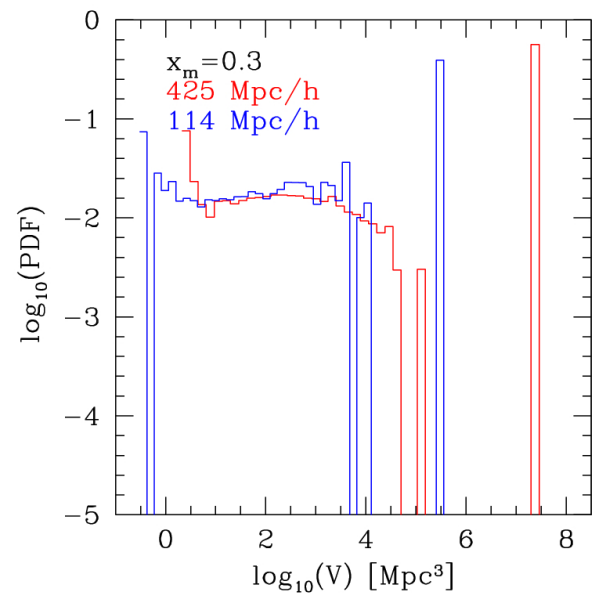




# HII region sizes: FOF

(Iliev et al, in prep.)

- Same volume in regions with  $V \ll V_{\text{box}}$
- Many more large HII regions in the larger box



Early

Middle

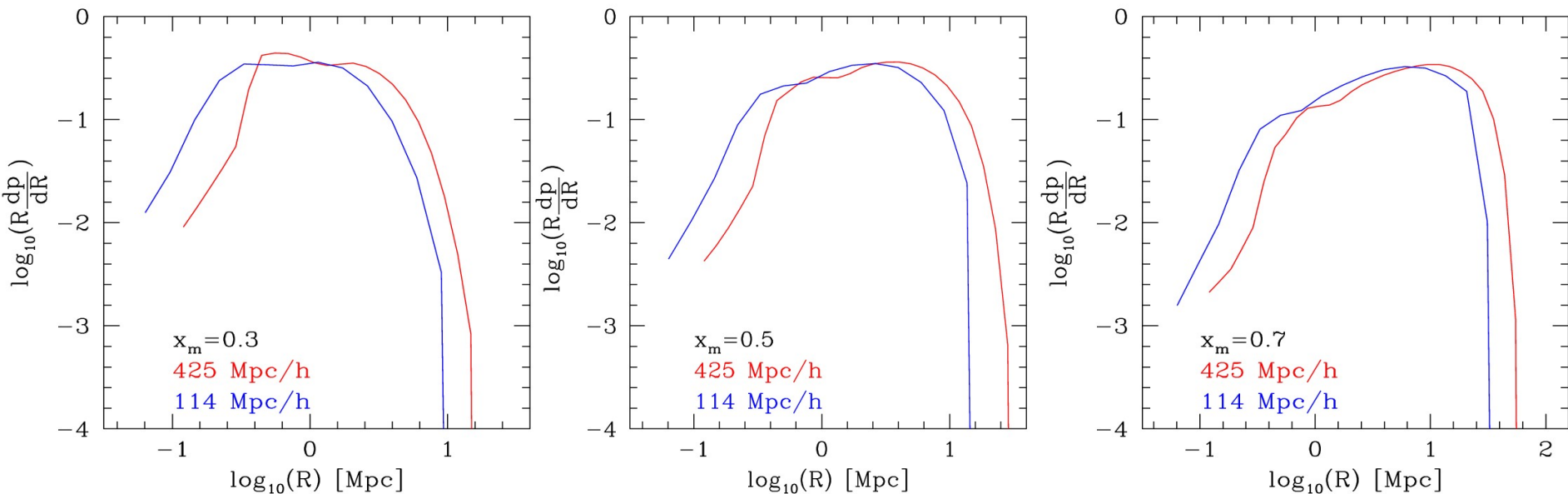
Late



# HII region sizes: Spherical Average

(Iliev et al, in prep.)

- Same volume in regions with  $V \ll V_{\text{box}}$
- Again many more large HII regions in the larger box



Early

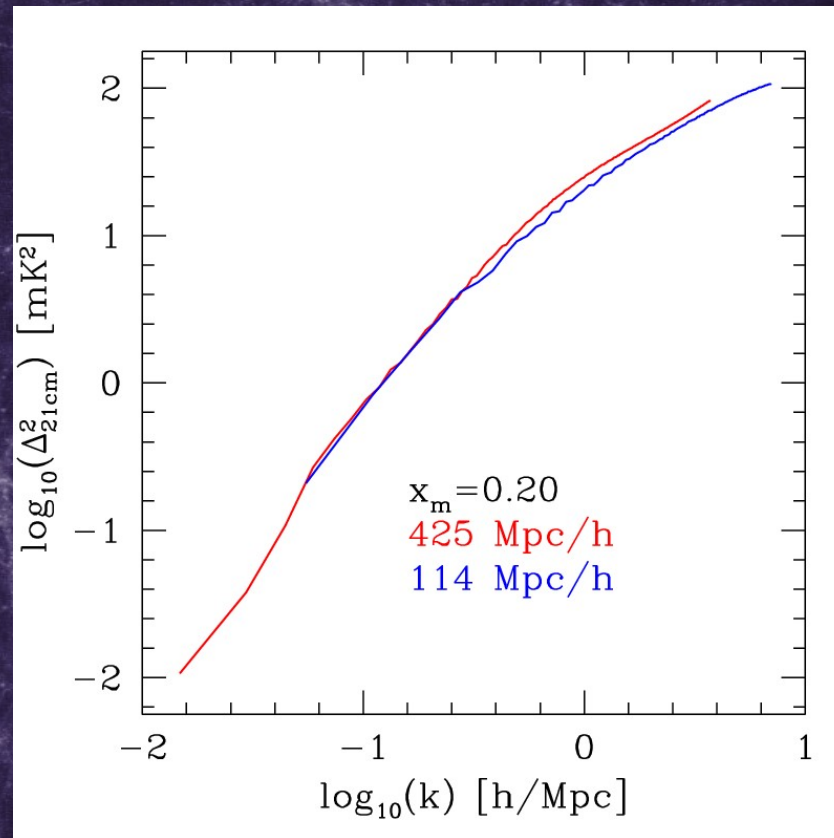
Middle

Late



# 21-cm power spectra: early

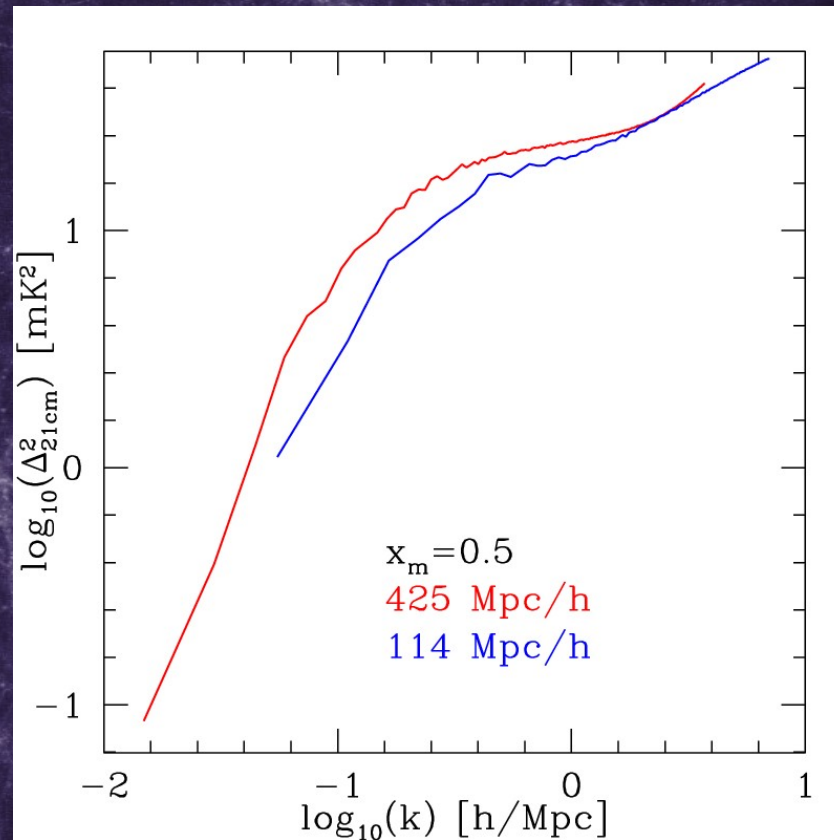
(Iliev et al, in prep.)





# 21-cm power spectra: middle

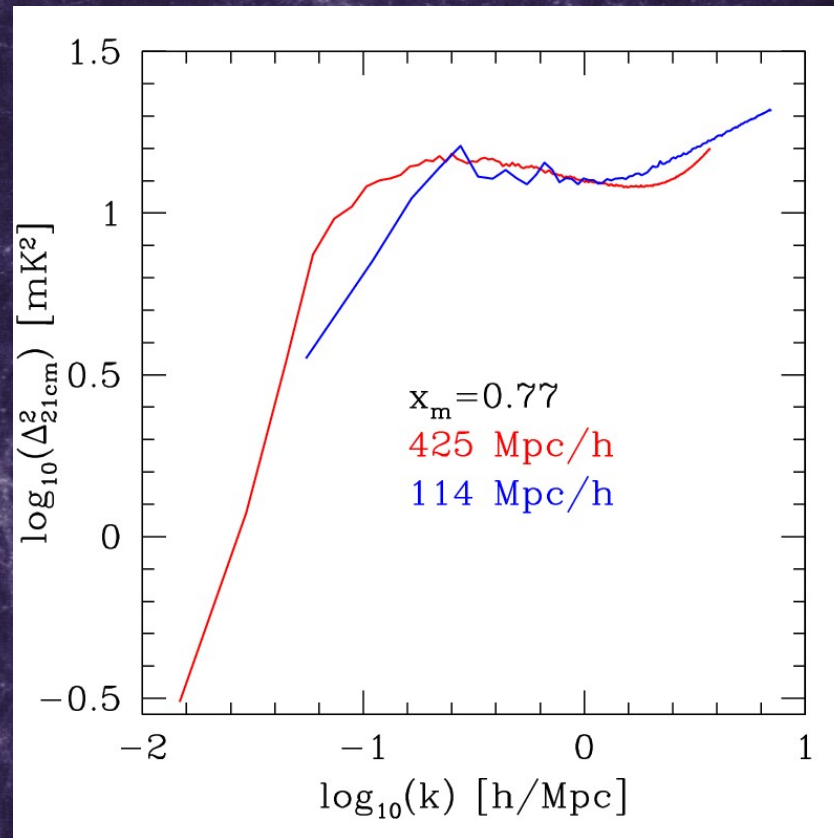
(Iliev et al, in prep.)





# 21-cm power spectra: late

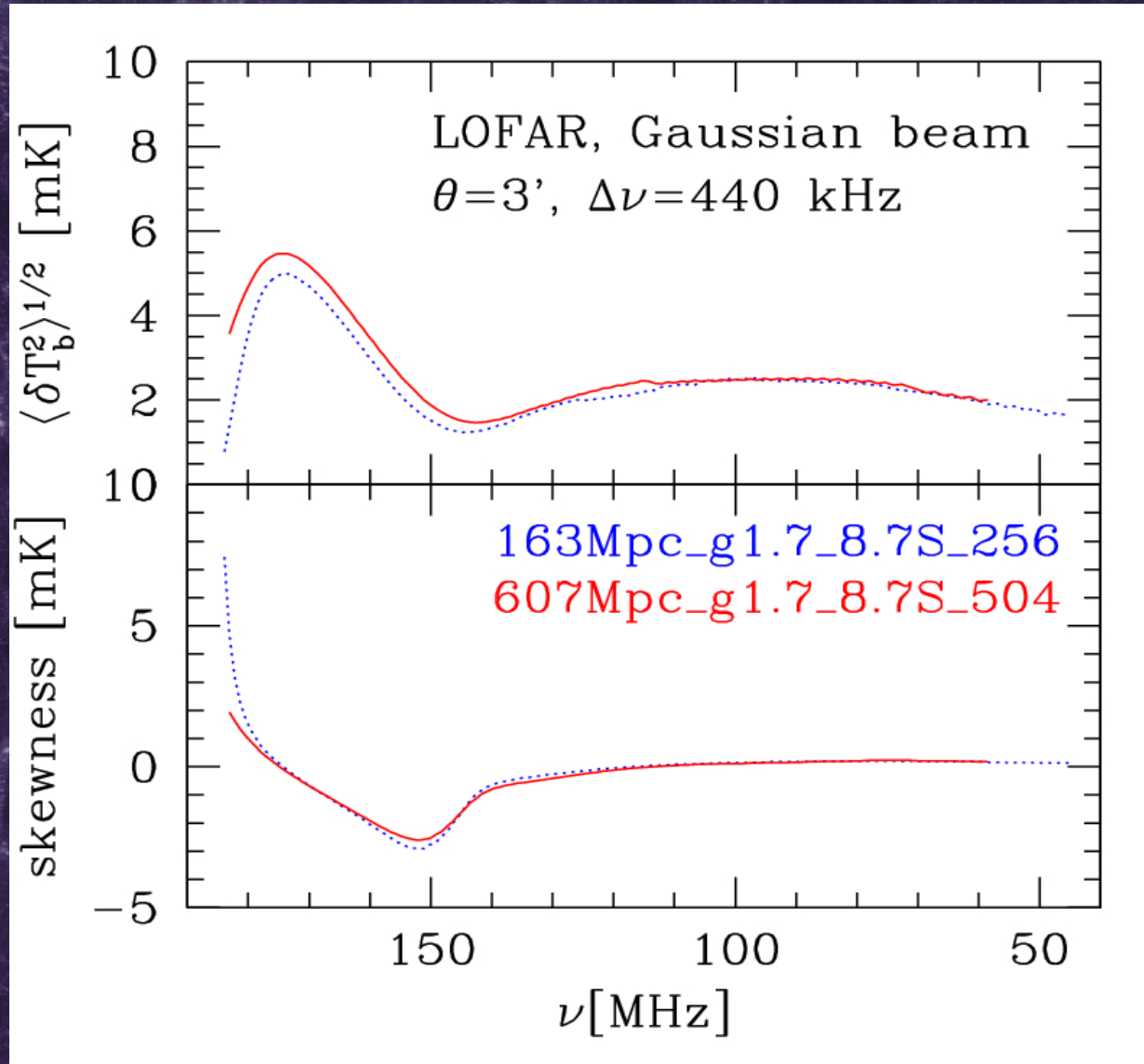
(Iliev et al, in prep.)





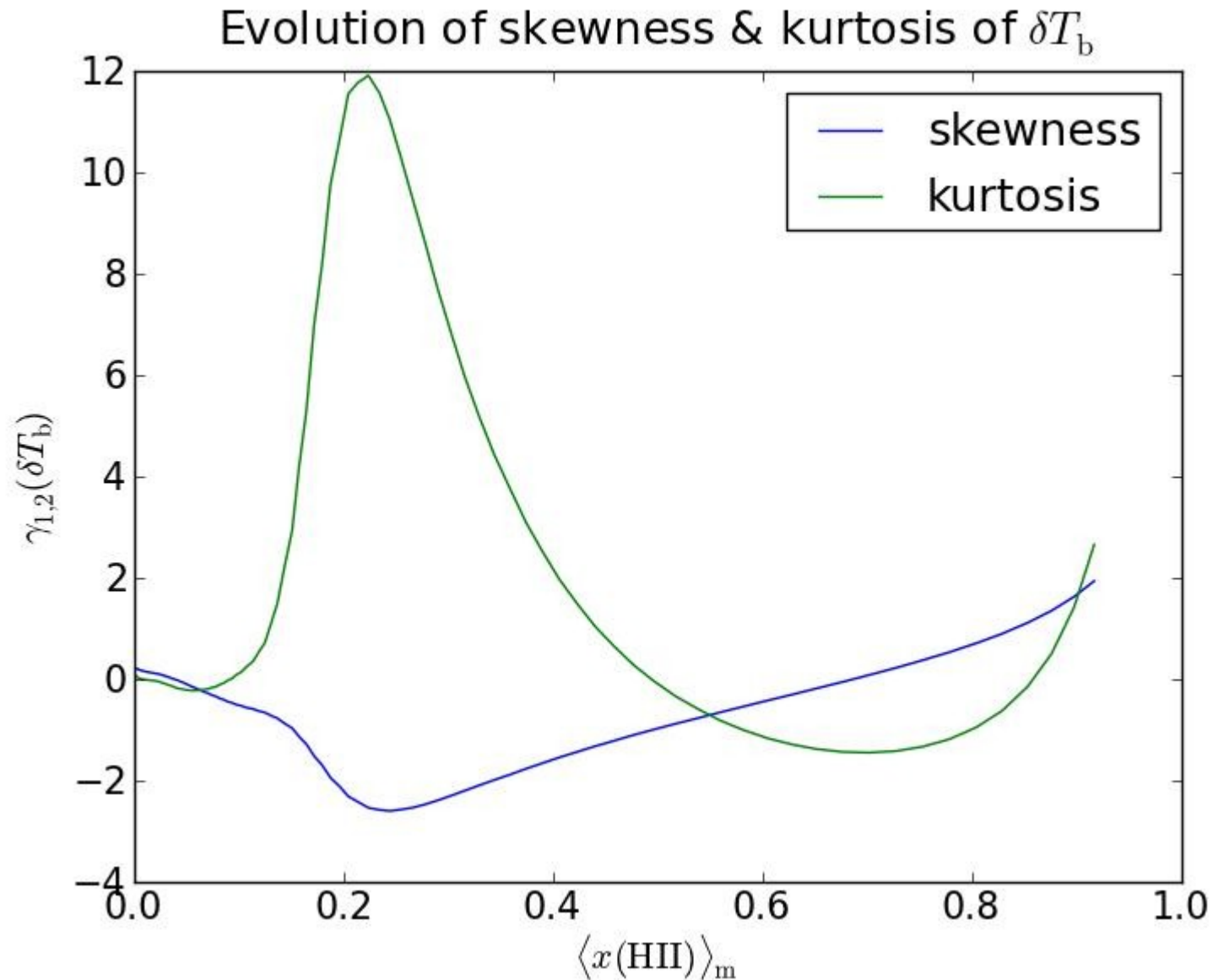
# 21-cm fluctuations: rms and skewness

(Iliev et al, in prep.)





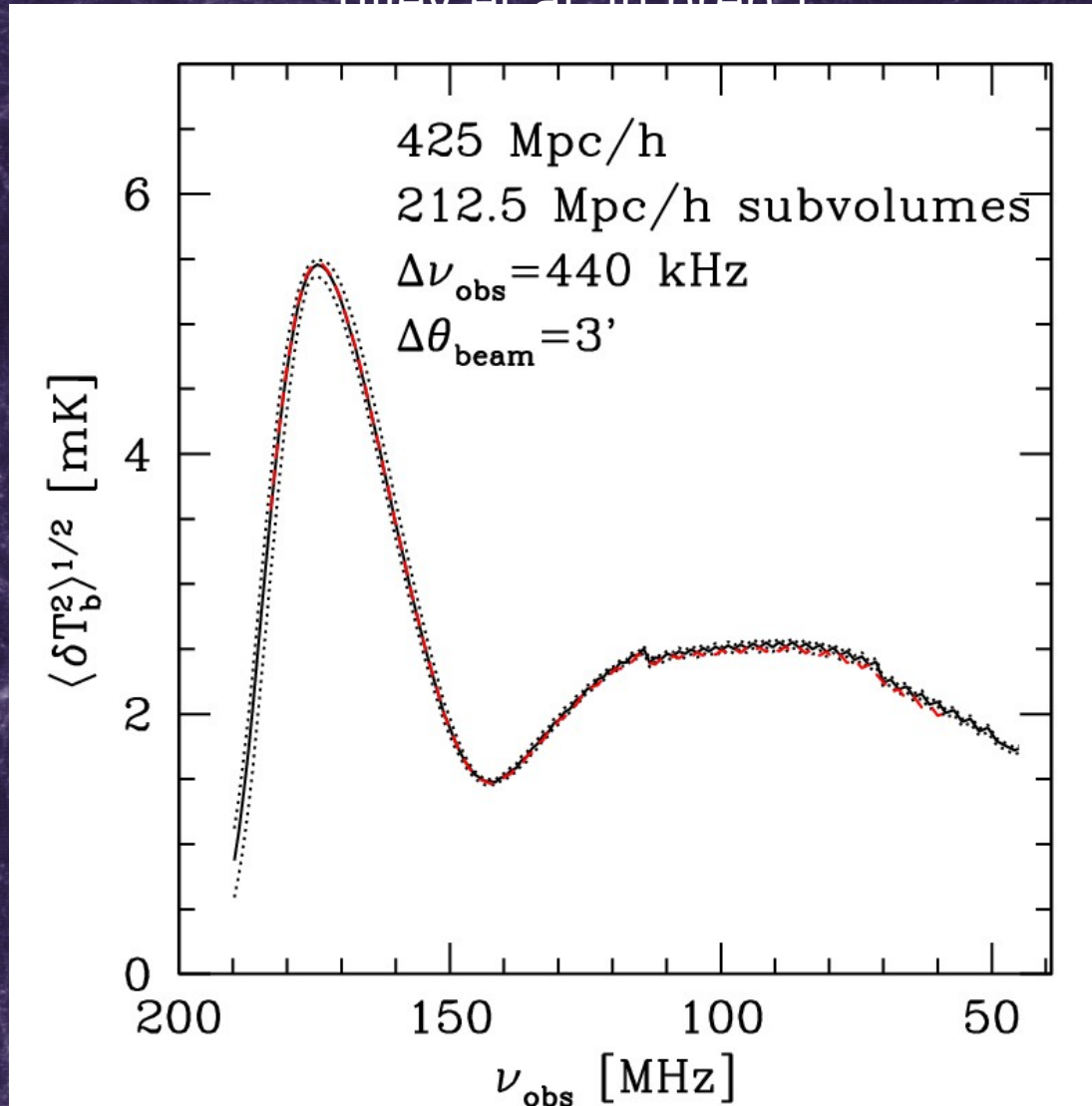
# 21-cm non-gaussianity (Iliev et al, in prep.)





# RMS convergence with box size

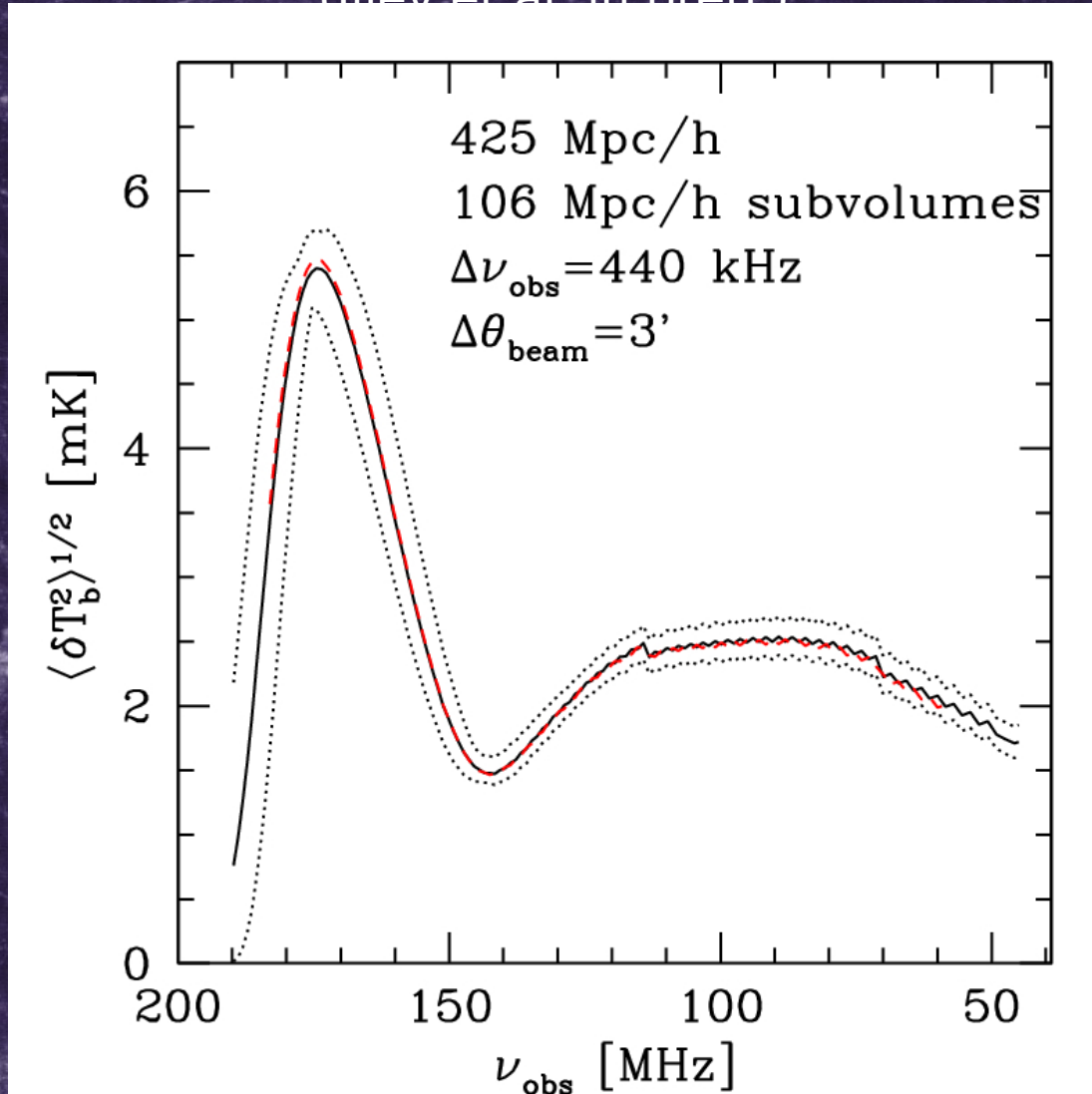
(Iliev et al. in prep.)





# RMS convergence with box size

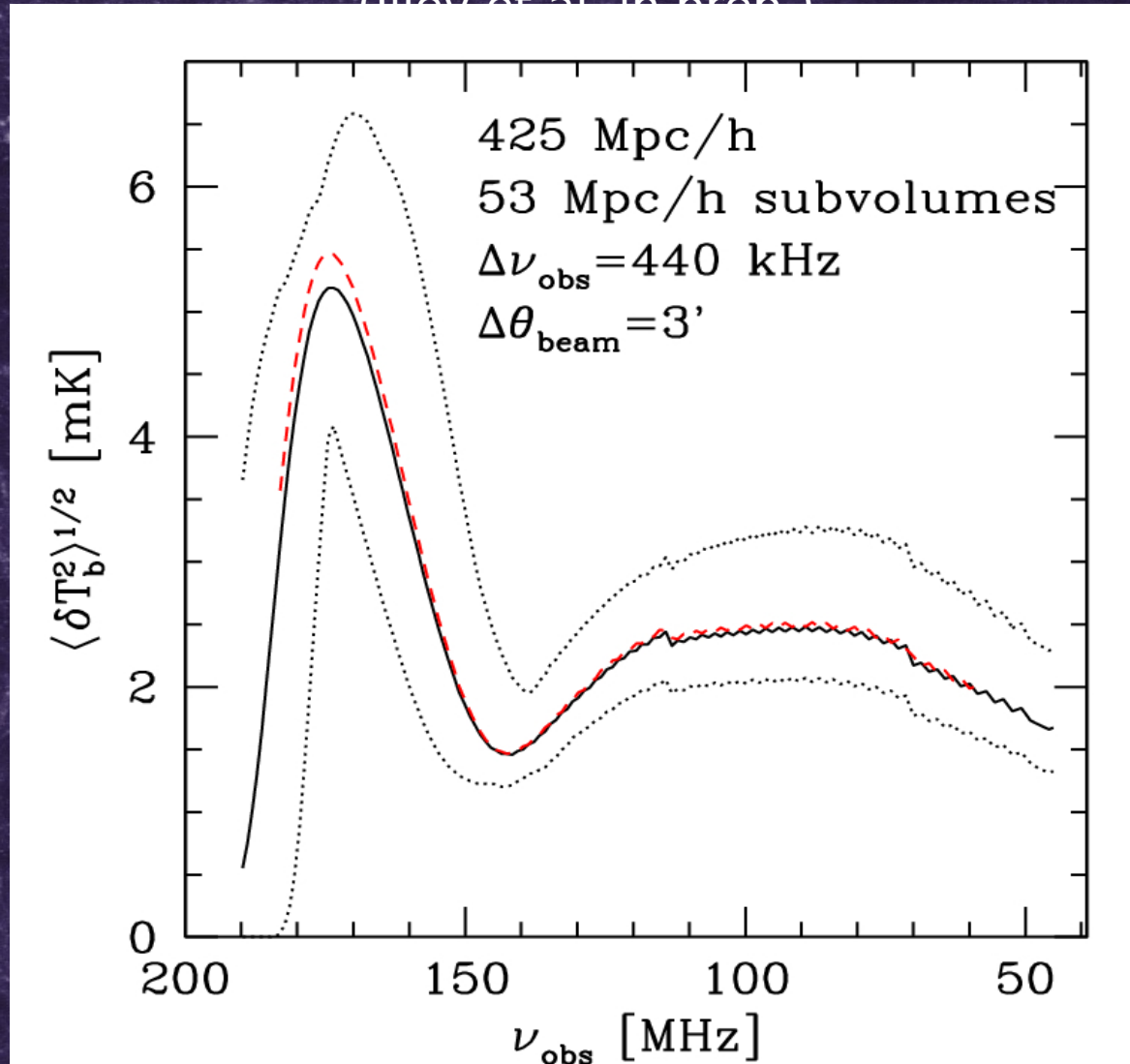
(Iliev et al. in prep.)





# RMS convergence with box size

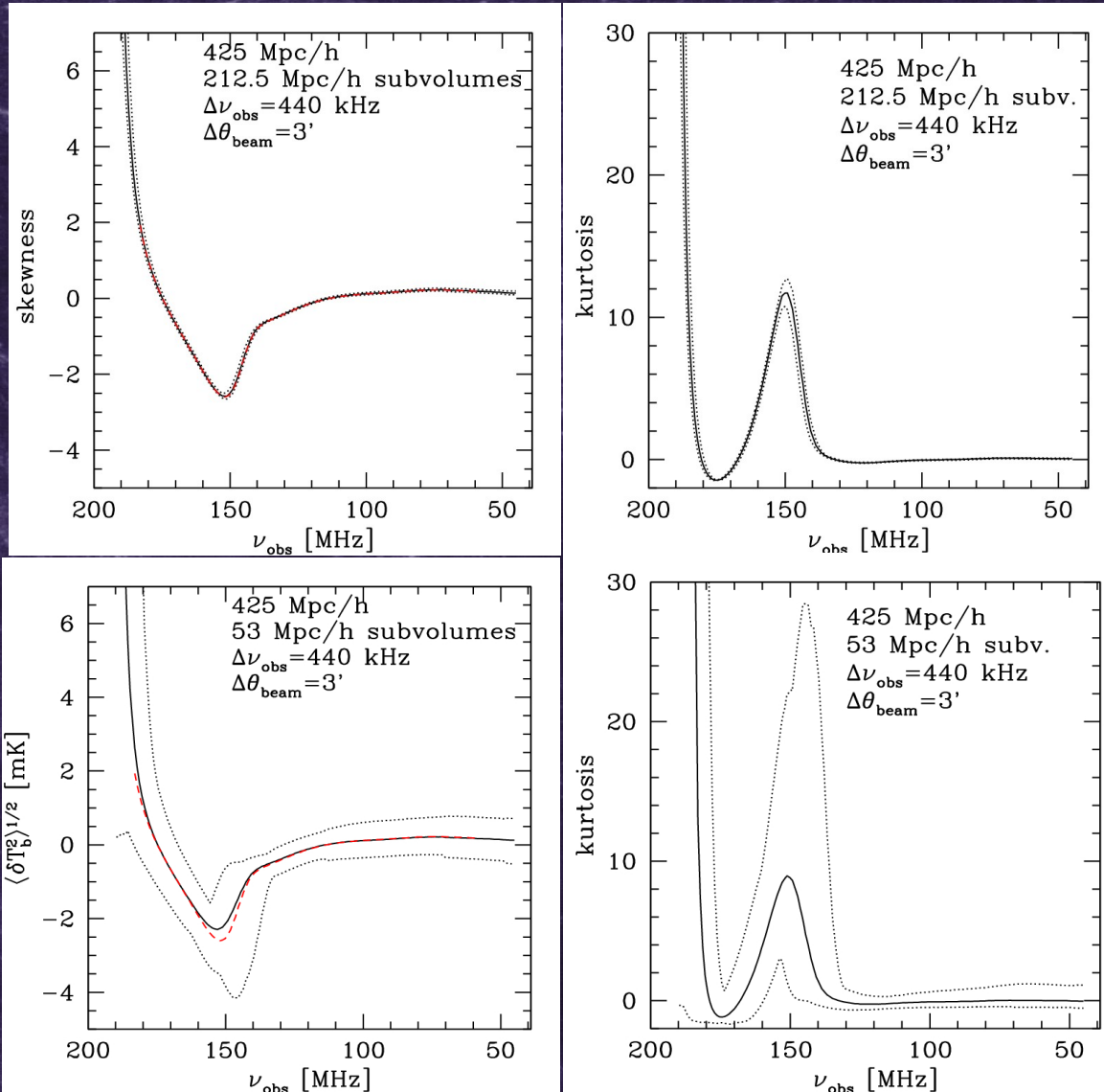
(Hlooy et al. in prep.)





# Skewness and kurtosis

(Iliev et al, in prep.)





# Redshift-space distortions in the nonlinear regime (Mao et al, in prep.)

- In the linear regime the redshifted 21-cm power spectrum can be written as:

$$P_{\Delta T}^{s,\text{lin}}(\mathbf{k}, z) = P_{\mu^0}(k, z) + P_{\mu^2}(k, z)\mu_{\mathbf{k}}^2 + P_{\mu^4}(k, z)\mu_{\mathbf{k}}^4$$

$$\mu_{\mathbf{k}} \equiv \mathbf{k} \cdot \mathbf{n} / |\mathbf{k}|$$

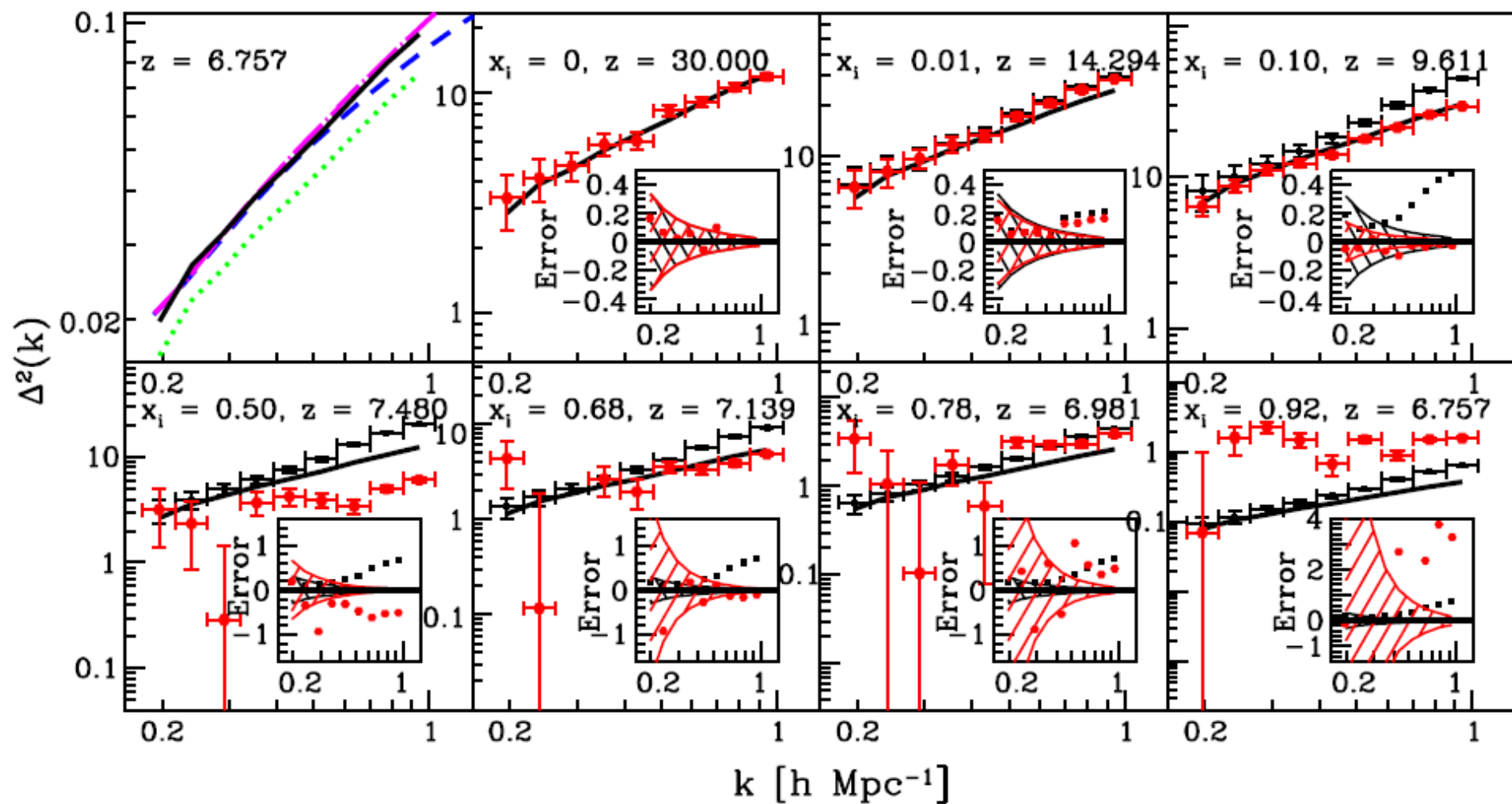
**Astrophysics**

**Cosmology**

- This assumes that density, velocity and ionization fields are linear. However, that is generally justified only for the velocity and (at large scales) for density field.
- Q: What are the limits of applicability of this approximation?



# Redshift-space distortions in the nonlinear regime (Mao et al, in prep.)

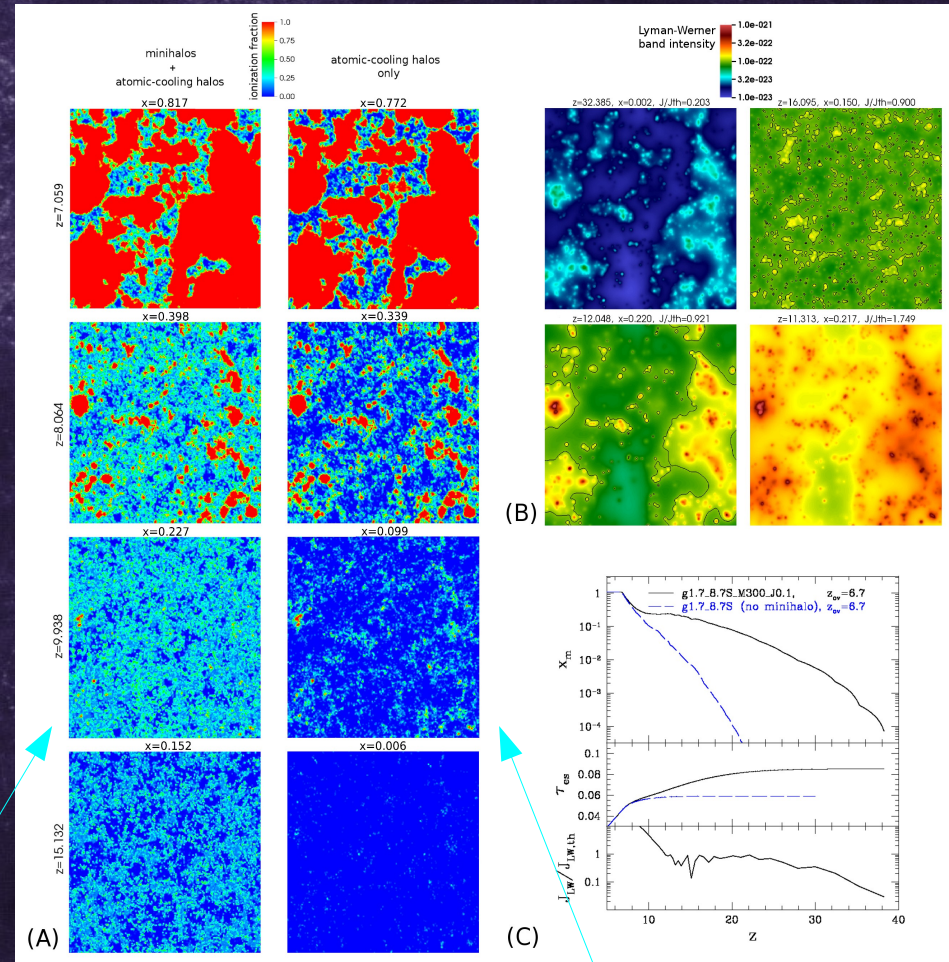




# Contribution of the First Stars to reionization

(Ahn et al, 2012)

- New method for including the formation, contribution and suppression of the First Stars in radiative transfer simulations.
- Lyman-Werner bands radiative transfer added.
- Reionization starts much earlier ( $z \sim 40$ ), is extended in time and its morphology changes significantly.



With First Stars

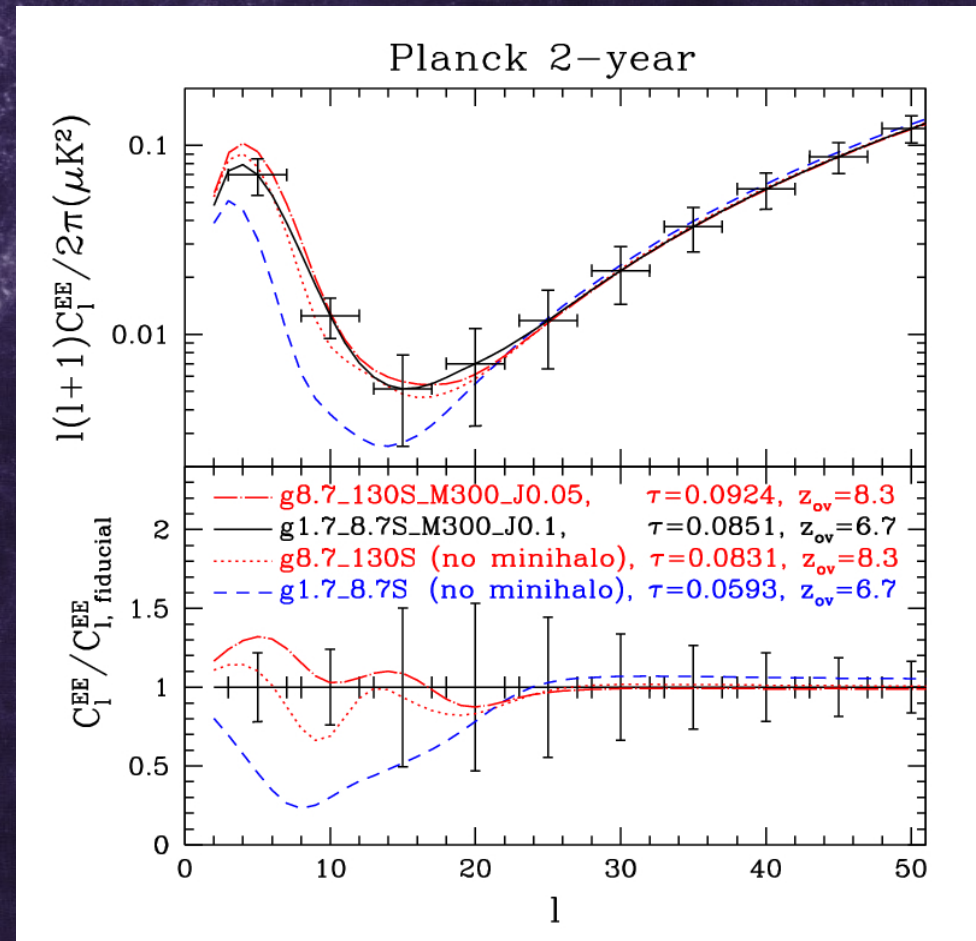
No First Stars



# Observing First Stars with Planck

(Ahn et al., 2012)

- The effect of First Stars is to both increase  $\tau_{\text{es}}$  and introduce features in the CMB polarization data at large scales (due to the different reionization history)
- Effect should be detectable with Planck

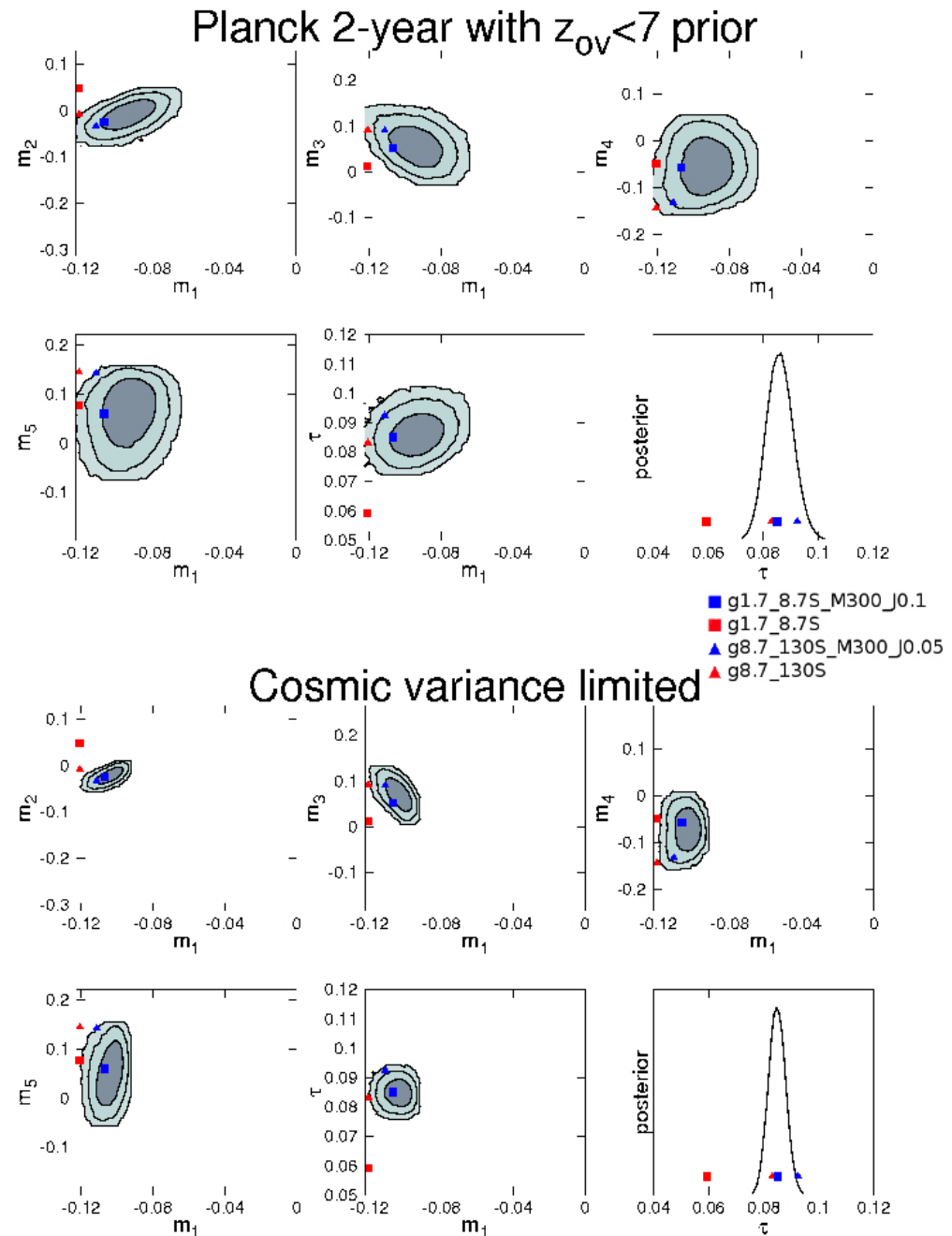




# Observing First Stars with Planck

(Ahn et al., 2012)

- Principal component analysis shows that effect is detectable with approx.  $2\text{-}\sigma$  confidence level even for fixed  $\tau_{es}$  if we assume  $z_{ov} < 7$  prior.





# Summary

- Structure formation at high- $z$  is quite different from later times — different halo mass function, higher halo clustering.
- FOF halo mass function has universal shape for fixed linking length, at all scales and redshifts.
- Spherical overdensity mass functions are redshift- and  $\Omega$ -dependent.
- Very long wavelength density fluctuations increase reionization patchiness and 21-cm signal appreciably.
- Reionization history and patchiness converge at scales above 100 Mpc/h, but vary significantly for smaller volumes, even if they are at mean density.
- $\mu$ -decomposition approximation is valid only during the early stages of reionization.
- Effects of the First Stars should be directly detectable with Planck → first direct observation of the Cosmic Dawn?