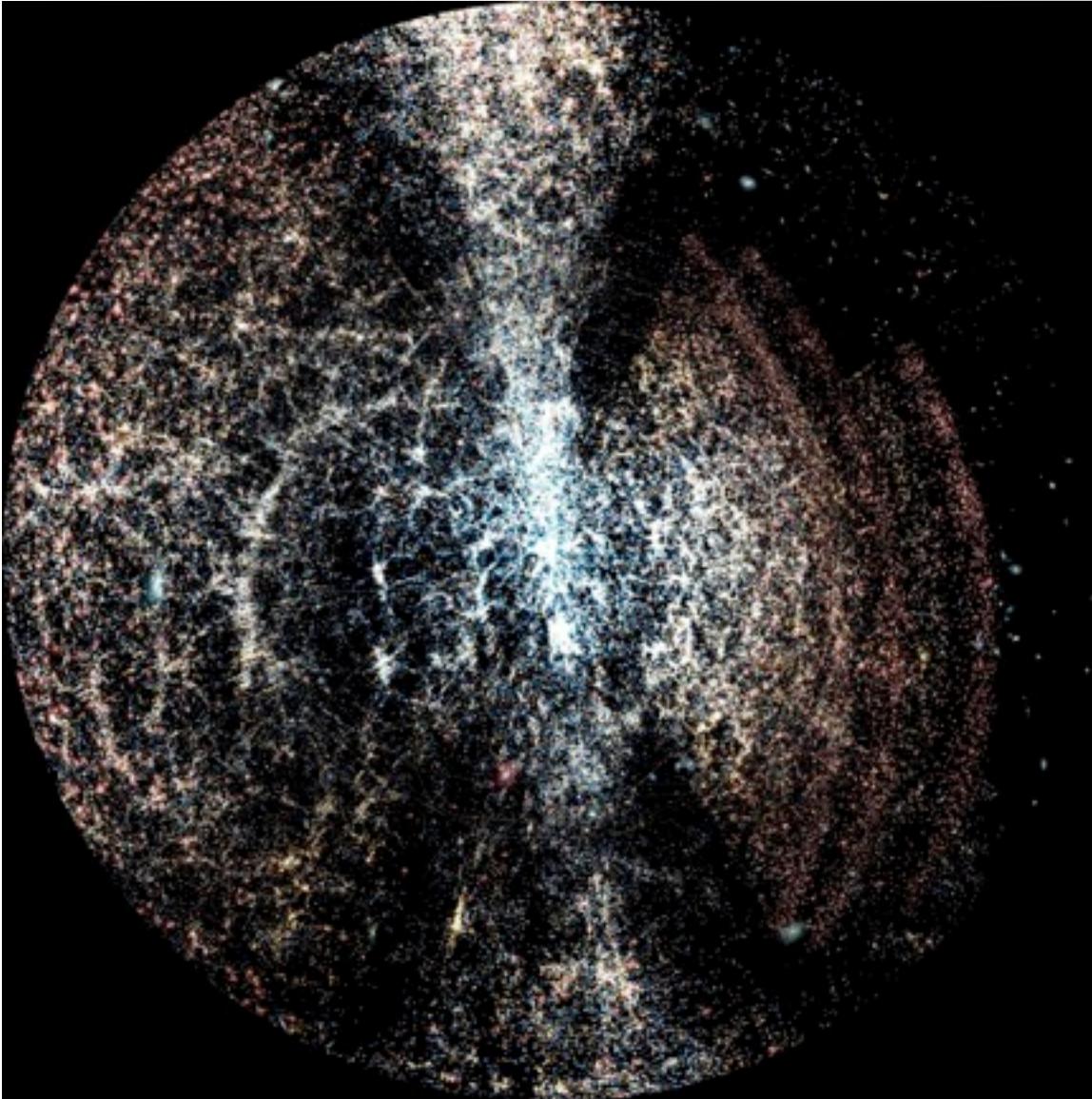


# Hierarchical amplitudes in the CFHTLS Wide Survey: Evolution since $\sim 1$

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# Introduction



The traditionnal tool: the two point correlation function

$$dP_{12} = n^2[1 + \xi(\mathbf{r}_{12})]dV_1 dV_2$$

Enough for gaussian random fields.

Non gaussian probes : **higher order statistics.**

Goal of this analysis : study the evolution with redshift of the cumulants of the galaxy distribution.

Previous studies: Szapudi et al.  
2001

# High order clustering

The factorial moments of the number of galaxies are closely related to those of the underlying field by:

$$\langle N^{[k]} \rangle = \langle N(N-1)\cdots(N-k+1) \rangle = \bar{N}^k \bar{\mu}_k$$

where  $\langle N^{[k]} \rangle$  is called the  $k^{\text{th}}$  factorial moment and  $\langle \mu_k \rangle$  are:  $\bar{\mu}_k = \frac{1}{V^k} \int_V dr_1 \dots dr_k \mu_k(r_1, \dots, r_k)$

If we separate  $\langle \mu_k \rangle$  into irreducible contributions we get:

$$\bar{\mu}_2 = 1 + \bar{\xi}_2$$

$$\bar{\mu}_3 = 1 + 3\bar{\xi}_2 + \bar{\xi}_3$$

$$\bar{\mu}_4 = 1 + 6\bar{\xi}_2 + 3\bar{\xi}_2^2 + 4\bar{\xi}_3 + \bar{\xi}_4$$

$$\bar{\mu}_5 = 1 + 10\bar{\xi}_2 + 10\bar{\xi}_3 + 15\bar{\xi}_2^2 + 10\bar{\xi}_2\bar{\xi}_3 + 5\bar{\xi}_4 + \bar{\xi}_5$$

The probability of counts in cells,  $P_N(\theta)$ , is the probability that a cell of dimension  $\theta$  contains  $N$  objects. It is straightforward to calculate the factorial moments from the CIC:

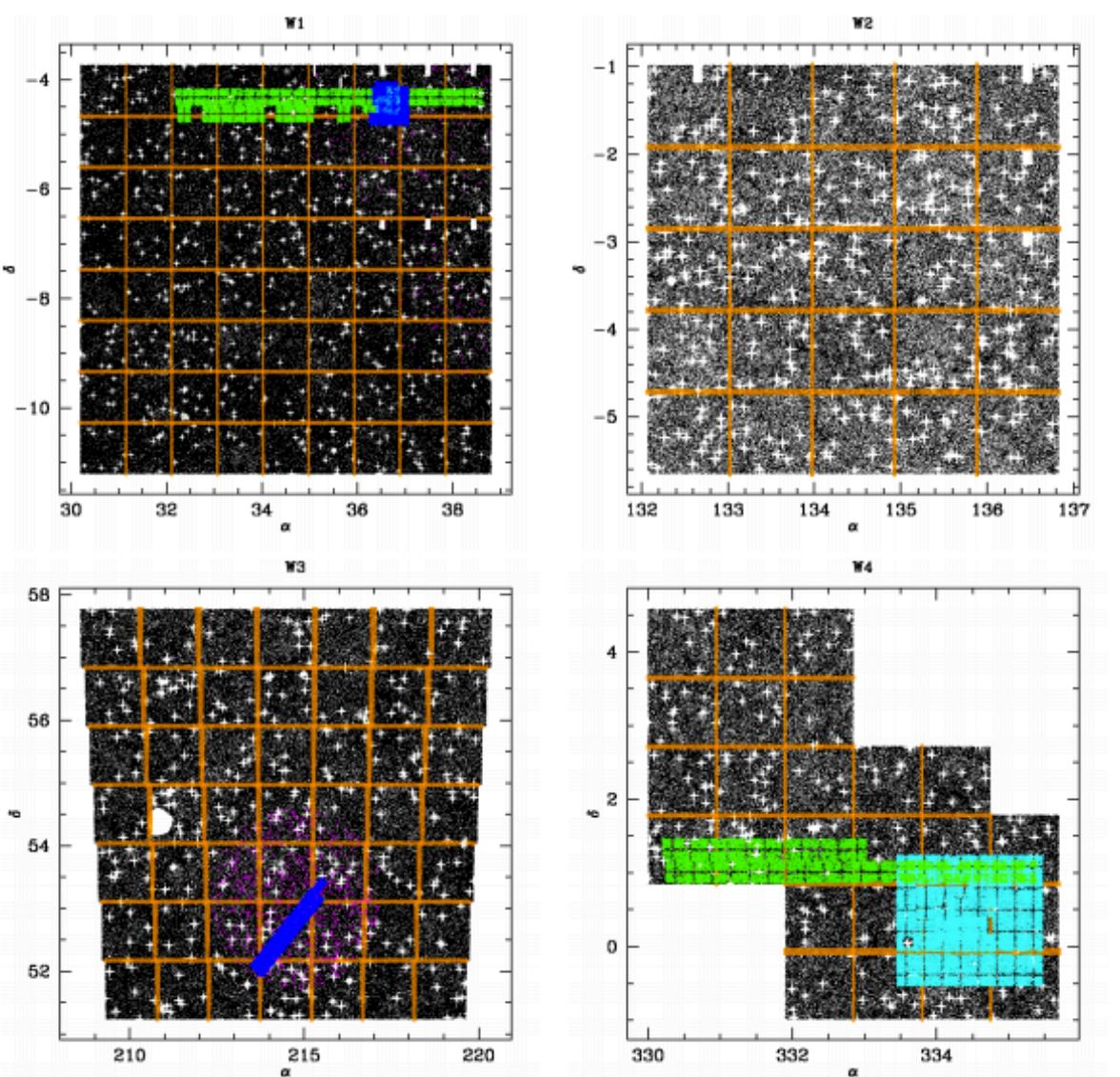
$$F_k \equiv \sum_N P_N N^{[k]}$$

And then we can deduced the hierarchical amplitudes:

$$S_k = \frac{\bar{\xi}_k}{\bar{\xi}_2^{k-1}}$$

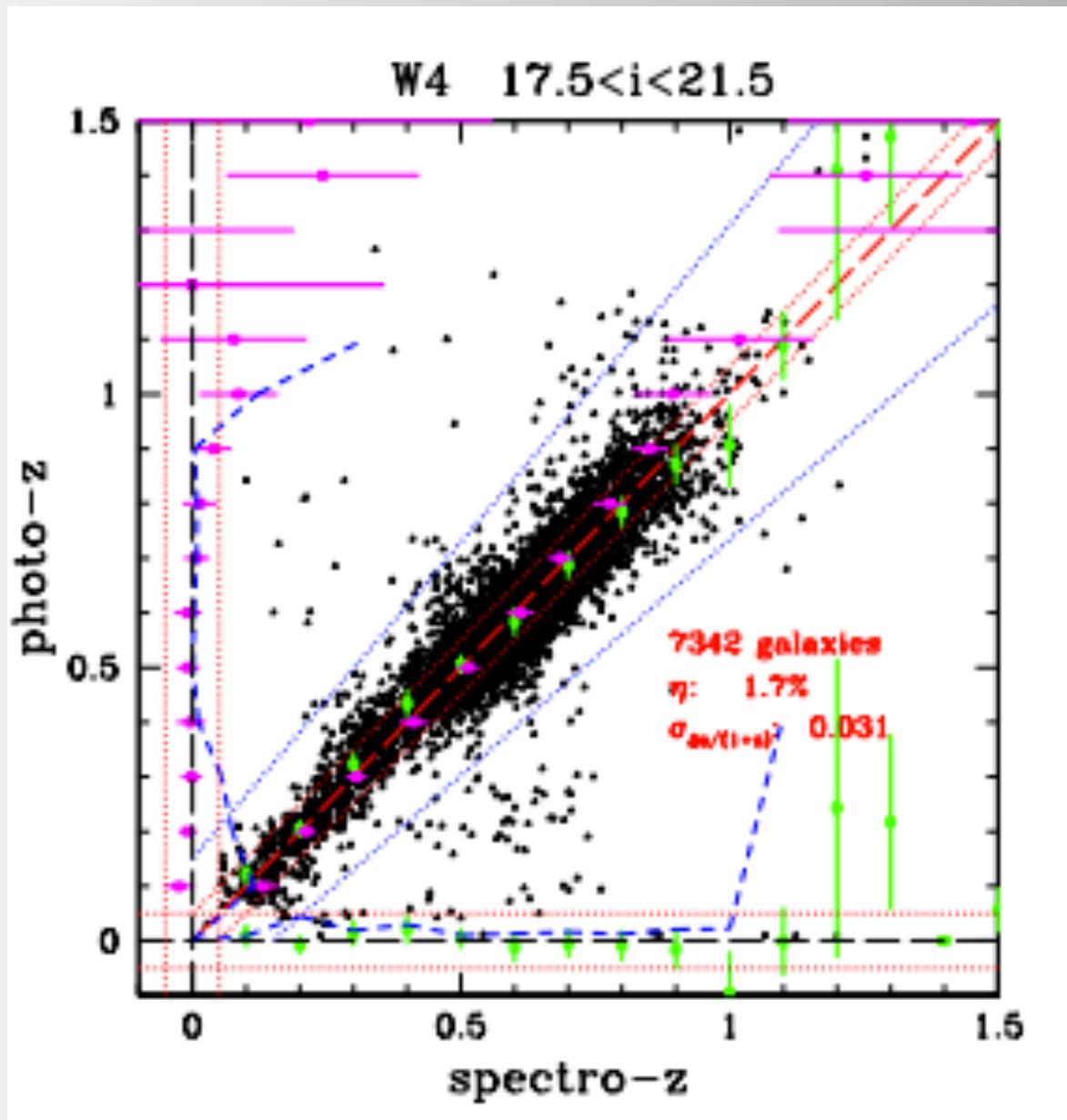
$$S_N = \frac{\bar{\xi} F_N}{N_c^N} - \frac{1}{N} \sum_{k=1}^{N-1} \binom{N}{k} \frac{(N-k) S_{N-k} F_k}{N_c^k}$$

# The CFHTLS data



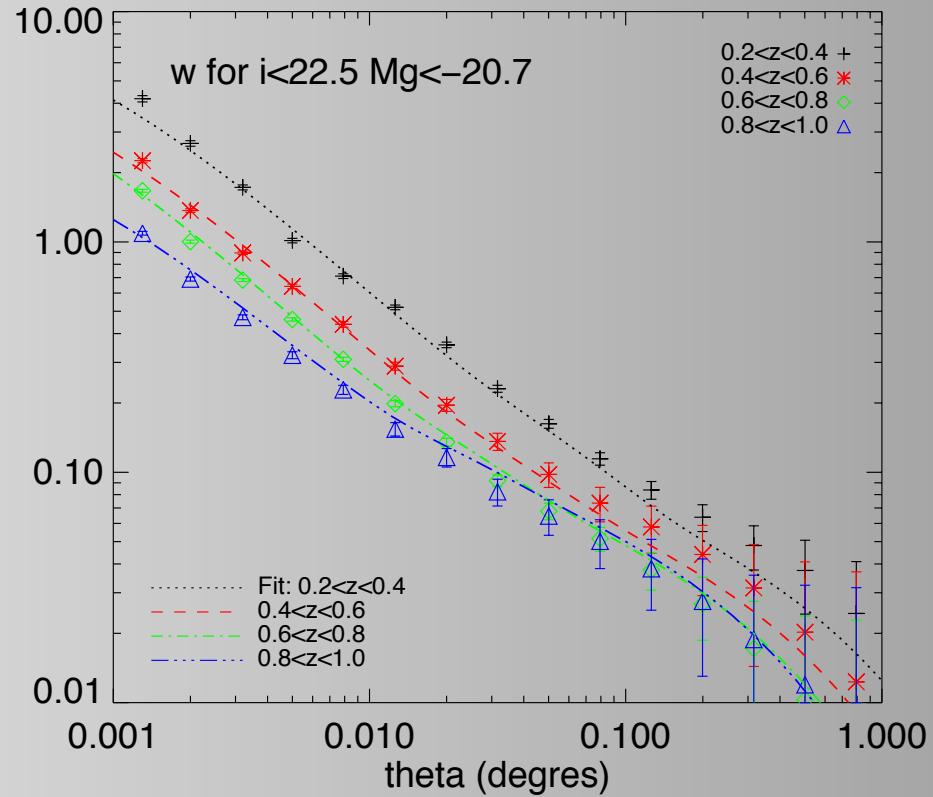
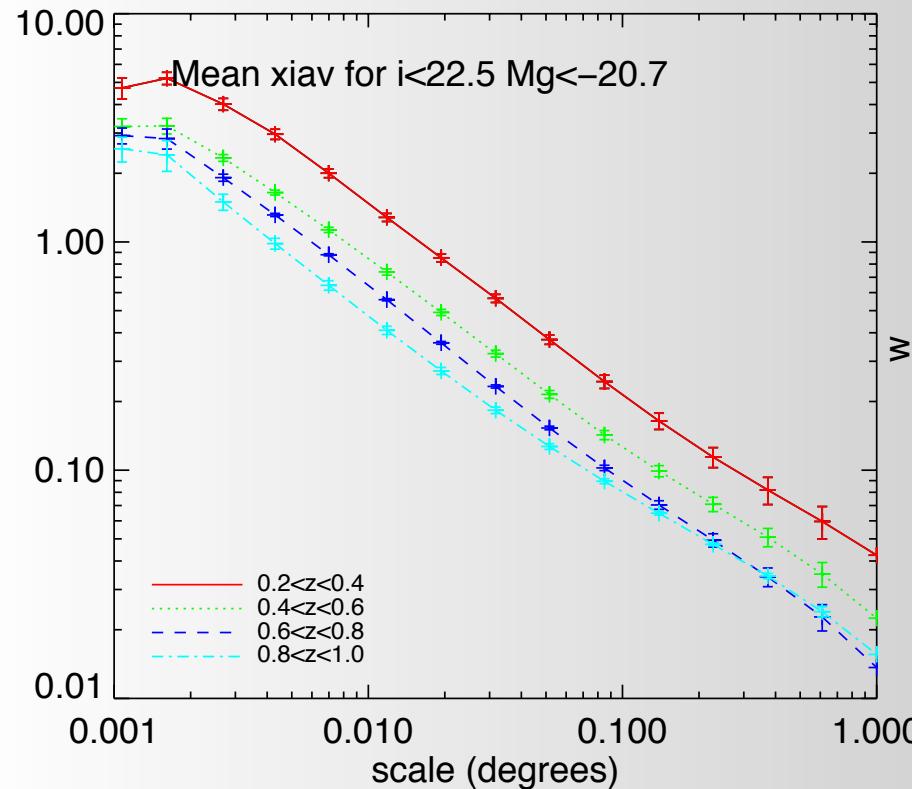
Covers **160 deg<sup>2</sup>**  
All fields are observed in  
**u\*, g, r, i, z** filters.  
Objects selected with  
**i<22.5**  
More than **1 500 000**  
**objects with photometric**  
**redshifts between 0<z<1.**

# Photometric data



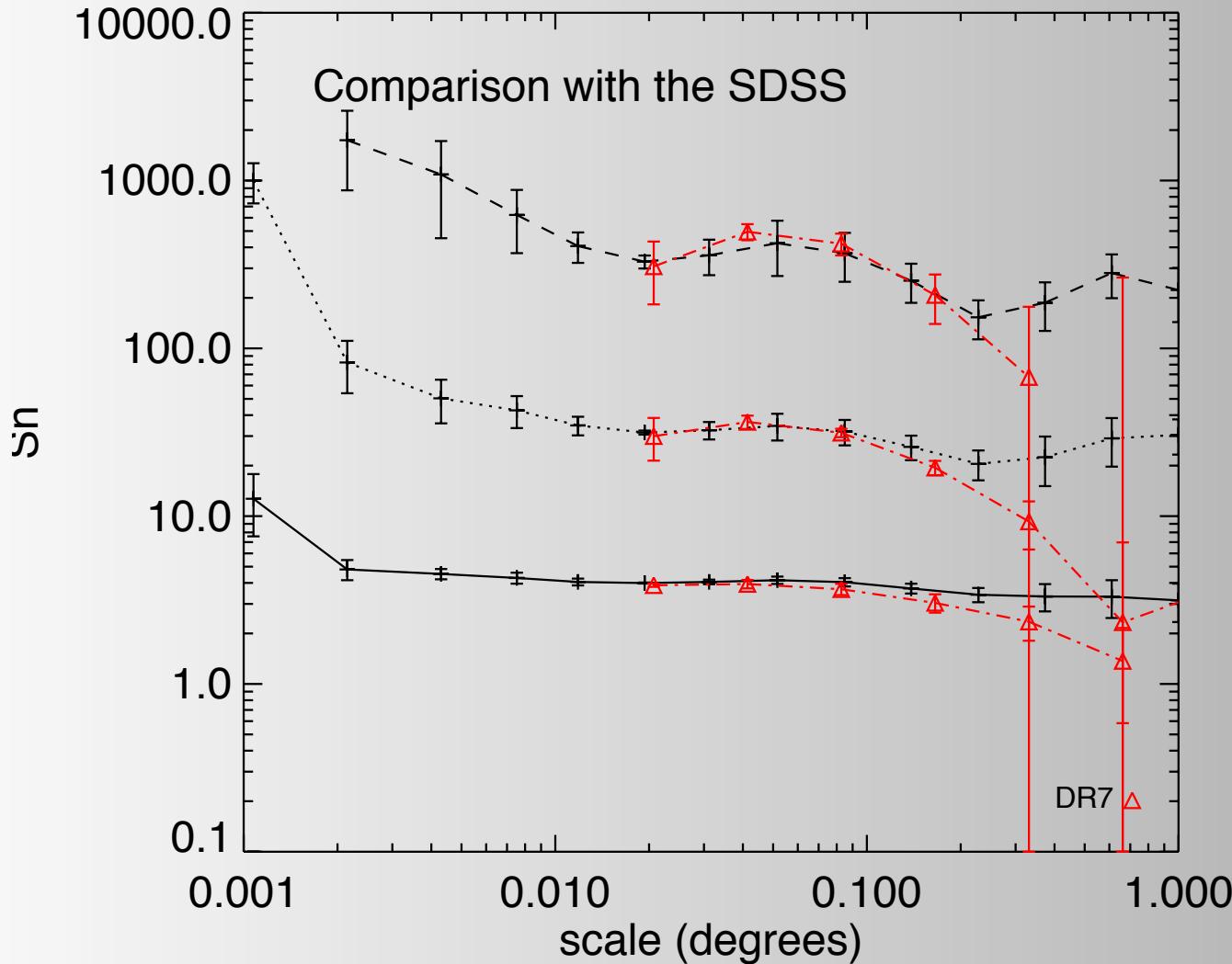
# The two point correlation function

We choose a volume limited sample with  $i < 22.5$  and  $Mg < -20.7$



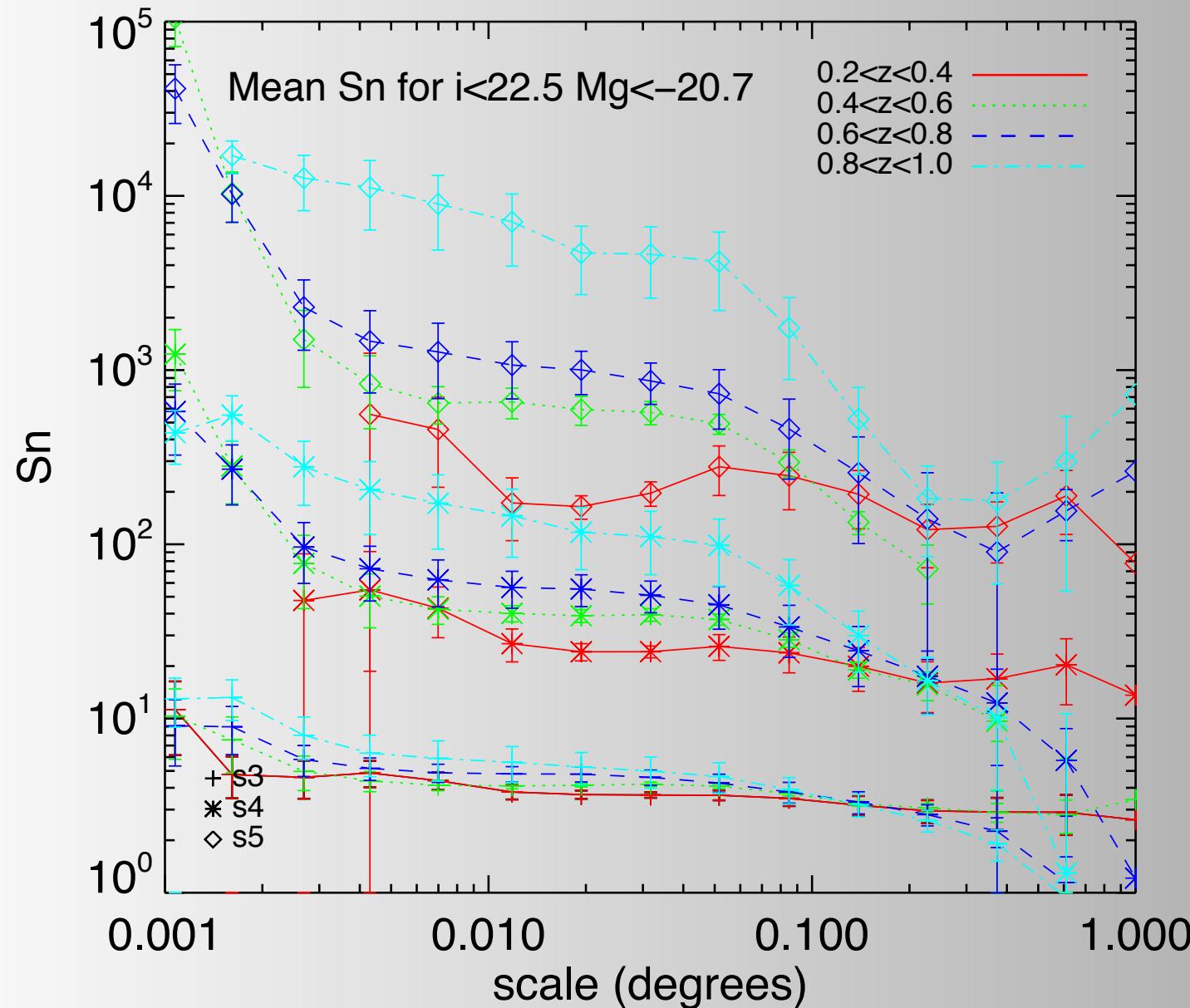
$$w(\theta) = \frac{N_r(N_r - 1)}{N_d(N_d - 1)} \frac{\langle DD \rangle}{\langle RR \rangle} - \frac{N_r - 1}{N_d} \frac{\langle DR \rangle}{\langle RR \rangle} + 1$$

# Comparison with the SDSS

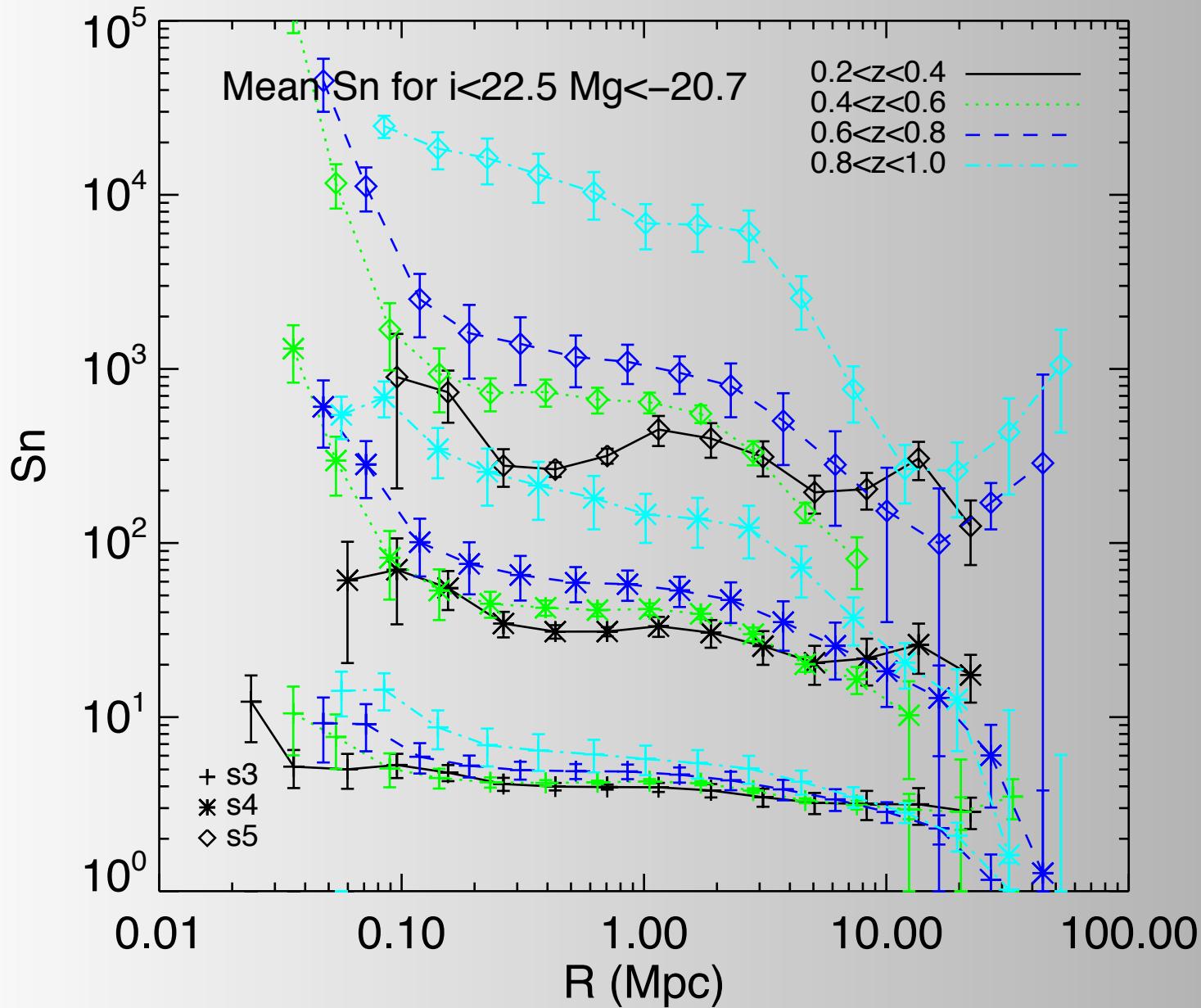


We made a sample comparable to the one in Ross et al. 2007 which corresponds to  $0 < z < 0.4$ ,  $18 < r < 21$  and  $Mr < -20.5$ . The red dots are obtained using the DR7 release of the SDSS.

# Measurements of high order clustering



# Deprojection



# Halo model

**Hypothesis:** parameters of the halo occupation function only depend on halo mass

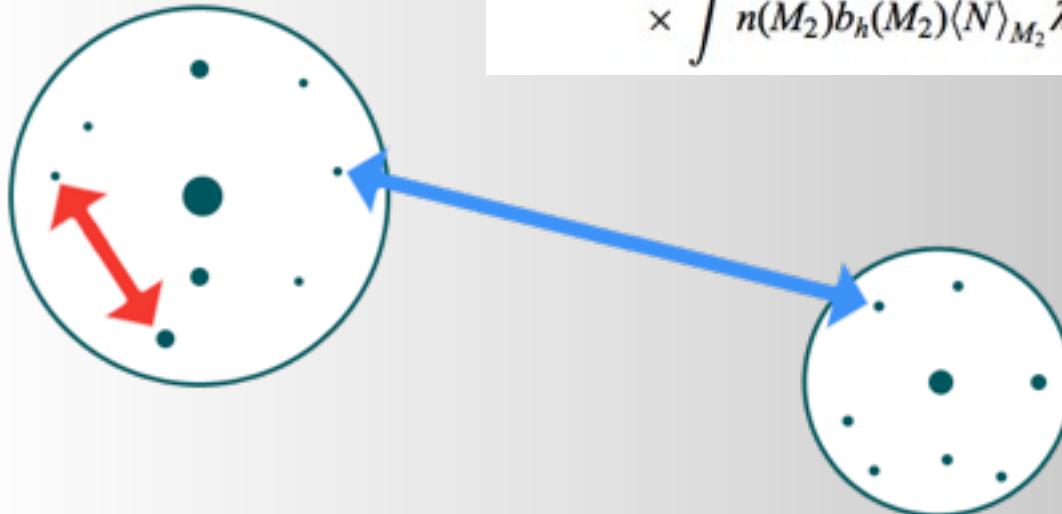
The two point correlation function is the sum of 2 terms:

- Pairs of galaxies within the same DM halo: dominant on small scales, depends on galaxy properties

$$1 + \xi_{gg}^{1h}(r) = \frac{1}{2} \bar{n}_g^{-2} \int n(M) \langle N(N-1) \rangle_M \lambda(r|M) dM$$

- Pairs of galaxies in separate DM halos: dominant on large scales, linearly follows the DM

$$\begin{aligned} \xi_{gg}^{2h}(r) &= \xi_{mm}^{\text{lin}}(r) \bar{n}_g^{-2} \int n(M_1) b_h(M_1) \langle N \rangle_{M_1} dM_1 \\ &\quad \times \int n(M_2) b_h(M_2) \langle N \rangle_{M_2} \lambda(r|M_1, M_2) dM_2 \end{aligned}$$

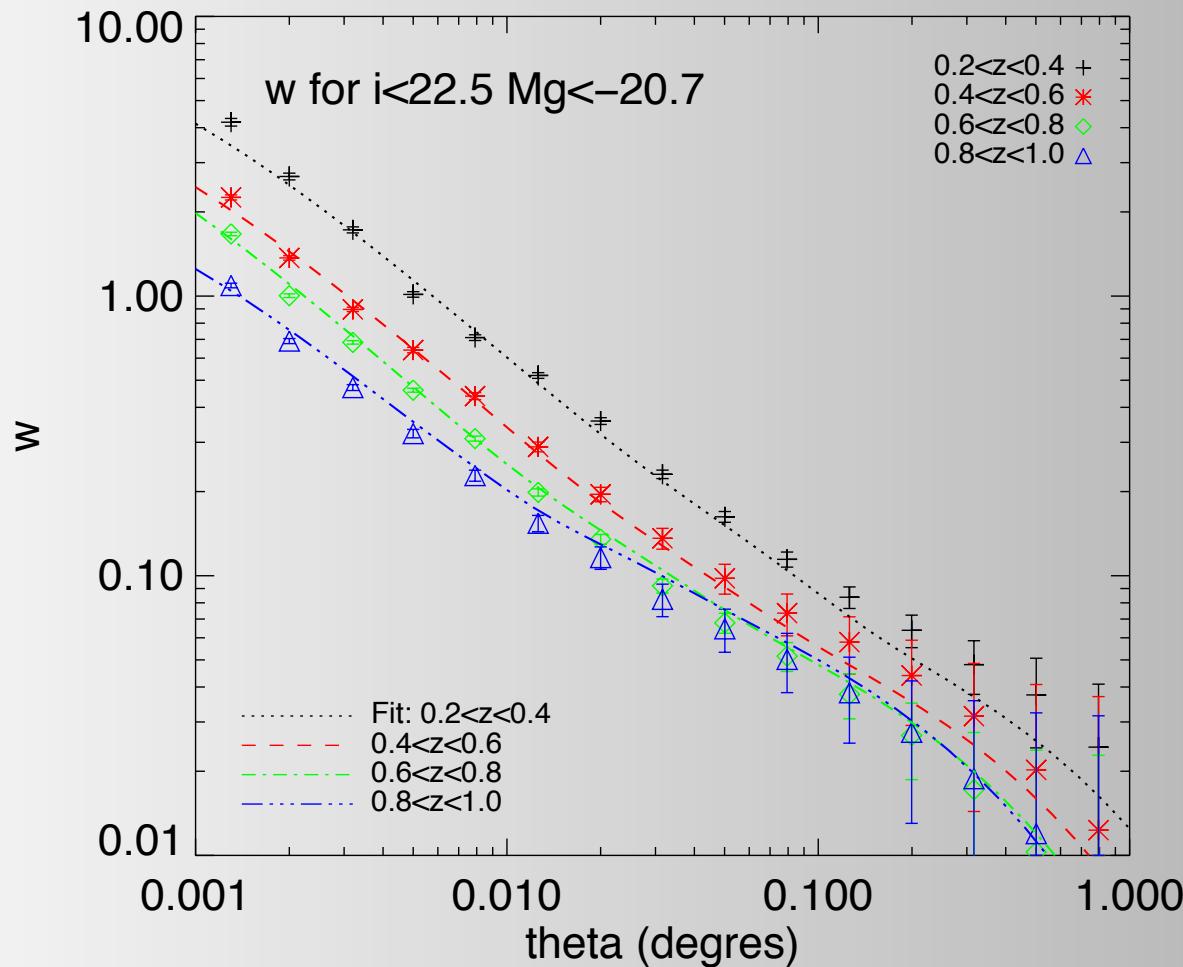


$$N(M) = N_c(M) \times [1 + N_s(M)]$$

$$N_c(M) = \frac{1}{2} \left[ 1 + \text{erf} \left( \frac{\log M - \log M_{\min}}{\sigma_{\log M}} \right) \right],$$

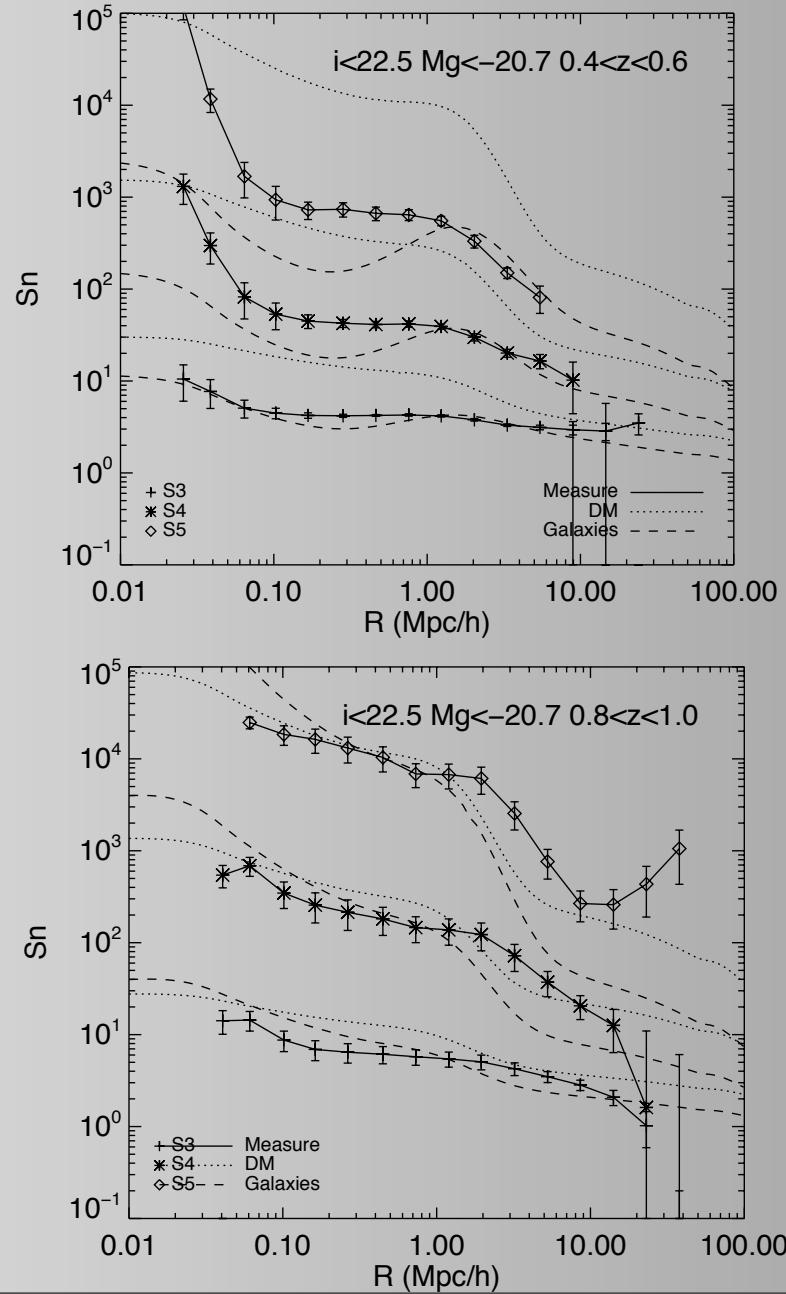
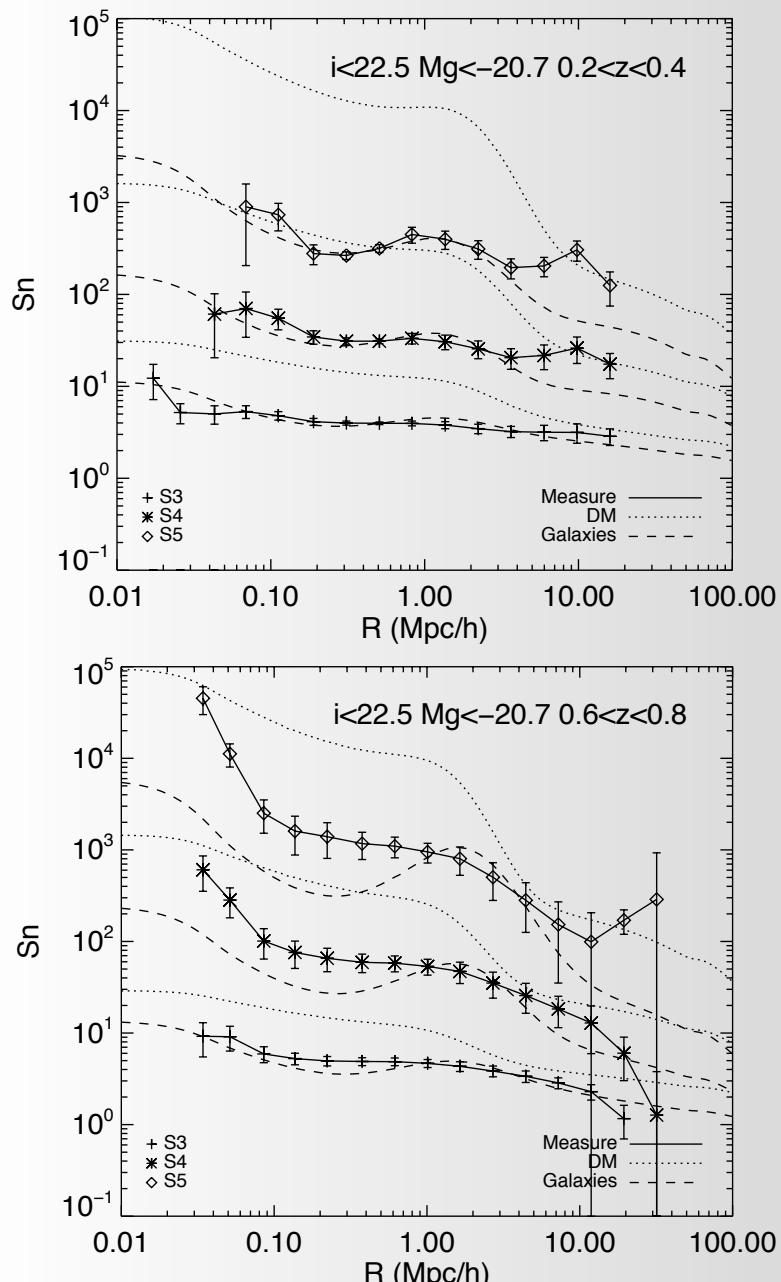
$$N_s(M) = \left( \frac{M - M_0}{M_1} \right)^\alpha.$$

# Fit HOD



$z$	$M_{min}$	$M_{max}$	$\alpha$
$0.2 < z < 0.4$	$12.30^{+0.10}_{-0.15}$	$14.63^{+0.24}_{-0.42}$	$1.1637^{+0.03}_{-0.03}$
$0.4 < z < 0.6$	$12.29^{+0.05}_{-0.07}$	$14.87^{+0.37}_{-0.70}$	$1.076^{+0.03}_{-0.05}$
$0.6 < z < 0.8$	$12.28^{+0.03}_{-0.04}$	$15.05^{+0.30}_{-0.35}$	$1.1337^{+0.02}_{-0.03}$
$0.8 < z < 1.0$	$11.99^{+0.02}_{-0.03}$	$14.94^{+0.8}_{-0.6}$	$1.4406^{+0.05}_{-0.03}$

# Prediction SNS



# Conclusion

In this study we were able:

- to measure the high order cumulants in the CFHTLS Wide
- to see the evolution of the SNs with the redshift

In a future work, we plan to:

- directly fit the halomodel parameters on the SNs
- add constraints from S3 to our HOD fitting to better adjust the transition between the one-halo and the two-halo term
- look at the evolution of the high order clustering on different populations of galaxies